## 1 Introduction

$$\max_{x_{ijk}} \sum_{i,j,k} x_{ijk}$$

$$x_{ijk} \ge 0$$

$$\sum_{i} x_{ijk} \le D_{ik}, \quad \text{for} \quad i = 1, ..., n_i, \quad k = 1, ..., n_k$$

where  $D_{ik}$  is the availability of product k in source i.

$$\sum_{i} x_{ijk} = p_{jm} \sum_{i,k} x_{ijk} \quad \text{for} \quad j = 1, ..., n_j \quad m = 1, ..., n_k - 1$$

where  $p_{jm}$  is the percentage of product k imposed on source j. Note that  $m=1,...,n_k-1$  and not  $m=1,...,n_k$  because the for each sink the sum of all percentages should be equal to 1, therefore once we guarantee or restrict  $n_k-1$  compositions at sink j the  $n_k-th$  composition is a linear combination of the remaining ones.