

- Resistencias serie, paralelo
- Aislante crítico en tuberías
- Resistencias de contacto.

$$q = UA \Delta T$$

$$q = \frac{\Delta T}{R_{eq}}$$

$$R_{eq} = \frac{1}{UA}$$

$$q = h A \Delta T$$

$$UA = \frac{1}{R_{eq}}$$

$$U = h$$

$$U = \frac{1}{AR_{eq}}$$

$$R = \frac{1}{hA}$$

$$q = k A \frac{\Delta T}{L}$$

$$U = \frac{k}{L}$$

$$R = \frac{L}{kA}$$

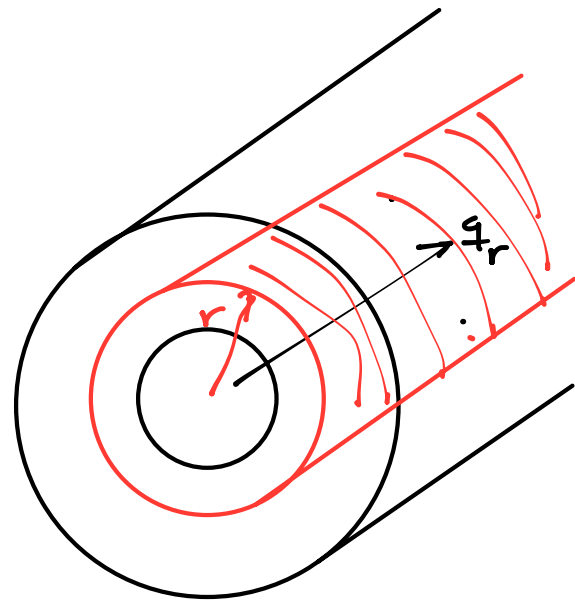
$$q = -k(T)A(x) \frac{dT}{dx}$$

$$\int_{T_0}^{T_L} \frac{-k(T)dT}{q} = \int_0^L \frac{dx}{A(x)}$$

$$-\frac{1}{q} \int_{T_0}^{T_L} k(T)dT = \int_0^L \frac{dx}{A(x)}$$

$$q = \frac{-\int_{T_0}^{T_L} k(T)dT}{\int_0^L \frac{dx}{A(x)}}$$

$$A(r) = 2\pi r L$$



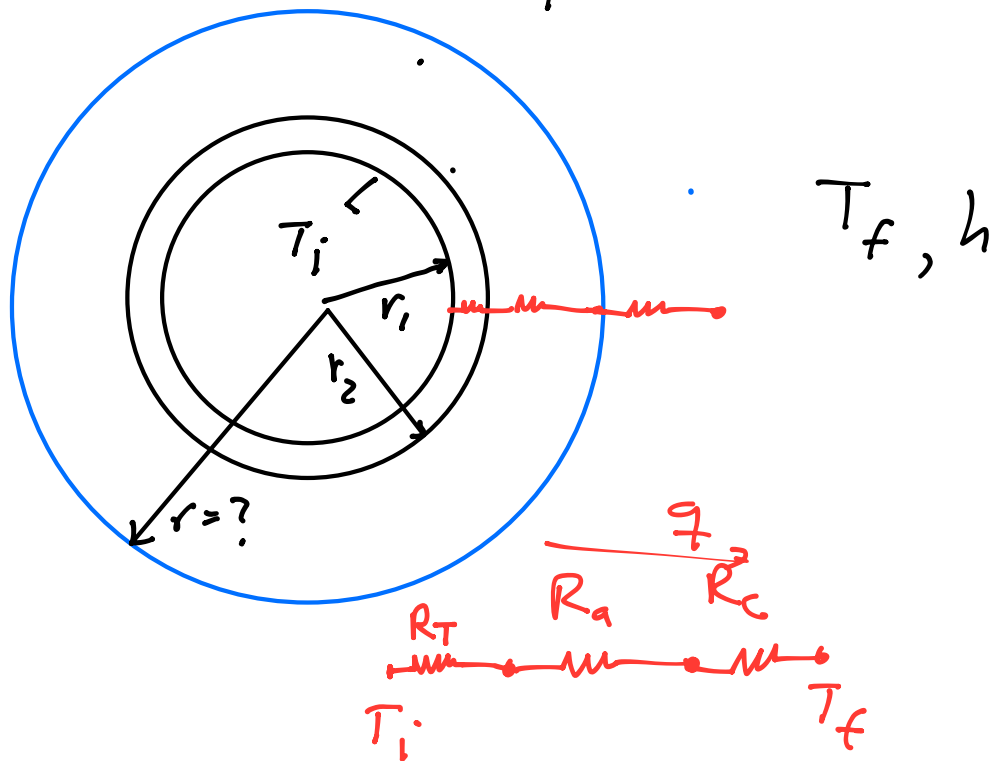
$$q = \frac{-\int_{T_0}^{T_L} k(T)dT}{\int_{r_i}^{r_o} \frac{dr}{2\pi r L}} = \frac{-\int_{T_i}^{T_o} k(T)dT}{\frac{1}{2\pi L} \ln\left(\frac{r_o}{r_i}\right)}$$

$$q = \frac{-\bar{k} (T_o - T_i)}{\frac{1}{2\pi L} \ln\left(\frac{r_o}{r_i}\right)} = \frac{T_i - T_o}{\frac{1}{2\pi k L} \ln\left(\frac{r_o}{r_i}\right)} = \frac{\Delta T}{R_{\text{eq}}}$$

$$R_{wall} = \frac{L}{KA}$$

$$R_{cil} = \frac{1}{2\pi kL} \ln\left(\frac{r_o}{r_i}\right)$$

$$q = \frac{\Delta T}{R_{eq}}$$



$$q = \frac{T_i - T_f}{R_T + R_a + R_c}$$

$$R_{TOT} = \frac{1}{2\pi k_1 L} \ln\left(\frac{r_2}{r_1}\right) + \frac{1}{2\pi k_a L} \ln\left(\frac{r}{r_2}\right) + \frac{1}{h(2\pi r L)}$$

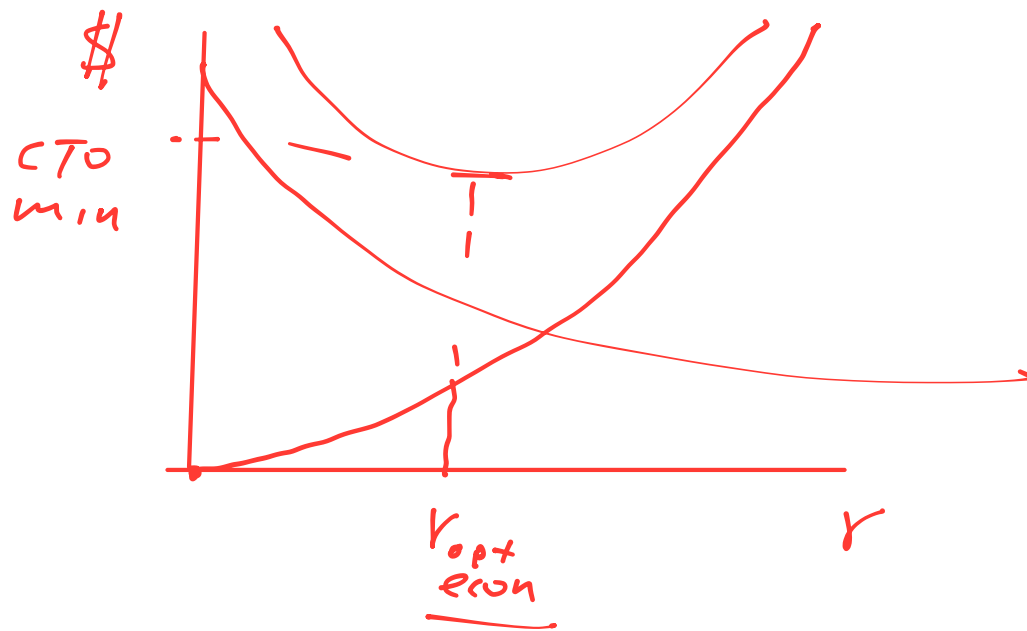
$$R_{TOT}|_{max} \rightarrow \frac{dR_{TOT}}{dr} = 0$$

$$\frac{1}{2\pi k_a L} \frac{r_2}{r} - \frac{1}{2\pi h L r^2} = 0$$

$$\frac{1}{K_a} = \frac{1}{h r}$$

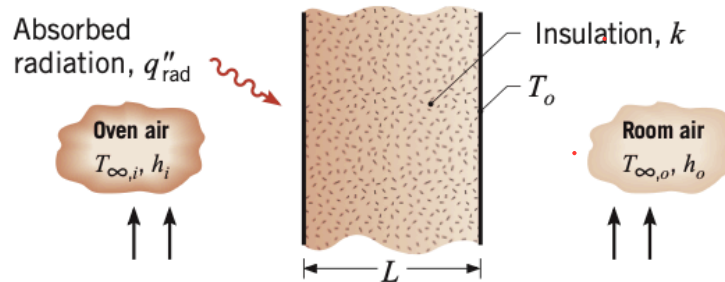
$$r_{cr} =$$

$$\frac{K_a}{h}$$

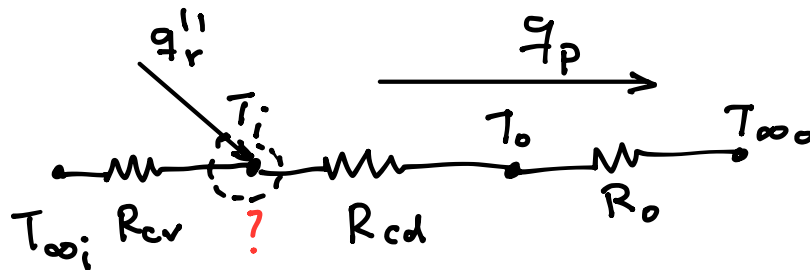




- 3.19 The wall of a drying oven is constructed by sandwiching an insulation material of thermal conductivity  $k = 0.05 \text{ W/m} \cdot \text{K}$  between thin metal sheets. The oven air is at  $T_{\infty,i} = 300^\circ\text{C}$ , and the corresponding convection coefficient is  $h_i = 30 \text{ W/m}^2 \cdot \text{K}$ . The inner wall surface absorbs a radiant flux of  $q''_{\text{rad}} = 100 \text{ W/m}^2$  from hotter objects within the oven. The room air is at  $T_{\infty,o} = 25^\circ\text{C}$ , and the overall coefficient for convection and radiation from the outer surface is  $h_o = 10 \text{ W/m}^2 \cdot \text{K}$ .



- (a) Draw the thermal circuit for the wall and label all temperatures, heat rates, and thermal resistances.



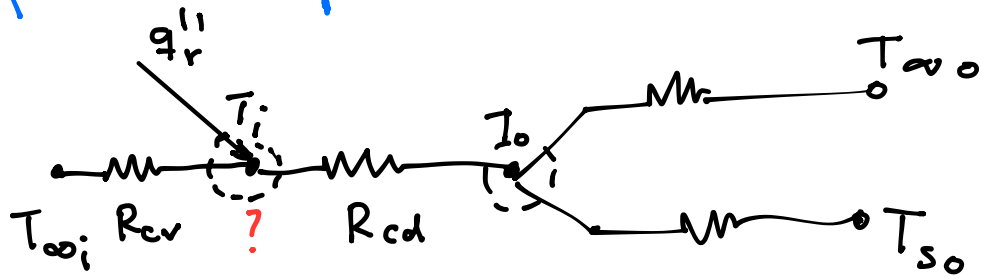
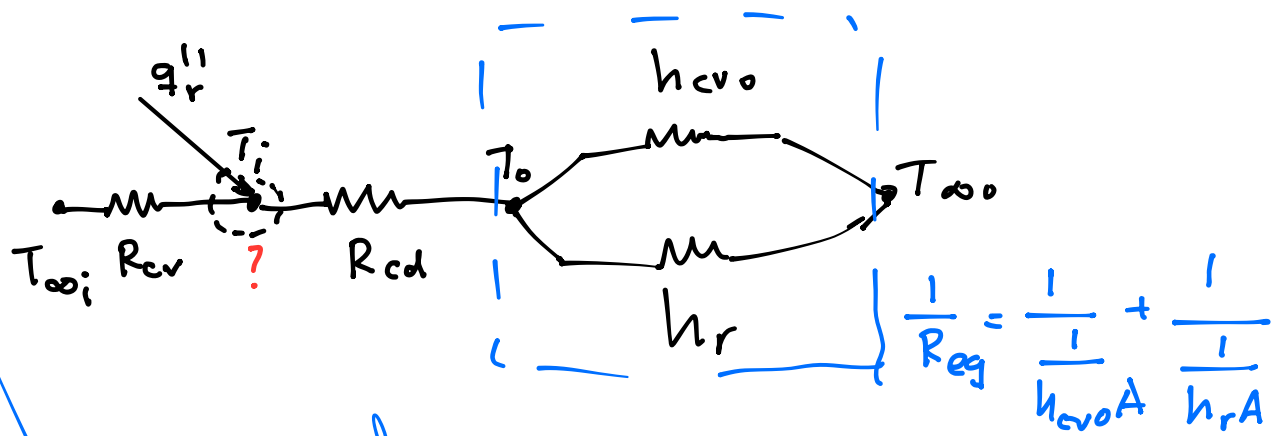
$$R_{cv} = \frac{1}{h_i A} \quad R_{cd} = \frac{L}{k A} \quad R_o = \frac{1}{h_o A}$$

$$\checkmark q''_r A + \frac{\checkmark T_{\infty,i} - \dot{?} T_i}{R_{cv} \checkmark} = \frac{T_i - \checkmark T_{\infty,o}}{R_{cd} + R_o \checkmark} = q_p$$

$$q_p = \frac{\dot{?} T_o - T_{\infty,o}}{R_o} = \frac{\dot{?} T_i - T_o}{R_{cd}}$$

$$T_o = 40^\circ\text{C}$$

?  $\rightarrow T_i, R_{cd}, q_p$



$$\frac{1}{R_{eq}} = h_{cv0}A + h_rA$$

$$R_{eq} = \frac{1}{A(h_{cv0} + h_r)} = \frac{1}{A h_o}$$

$$1) \quad q_r''A + \frac{T_{\infty i} - T_i}{R_{cv}} = \frac{T_i - T_{\infty o}}{R_{cd} + R_o}$$

$$2) \quad q_p = \frac{T_o - T_{\infty o}}{R_o}$$

$$3) \quad \frac{T_o - T_{\infty o}}{R_o} = \frac{T_i - T_o}{R_{cd}}$$

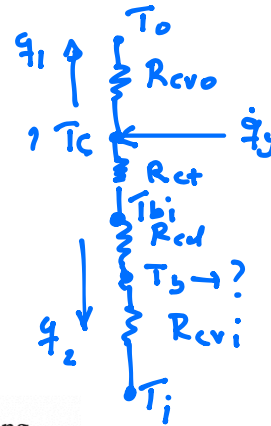
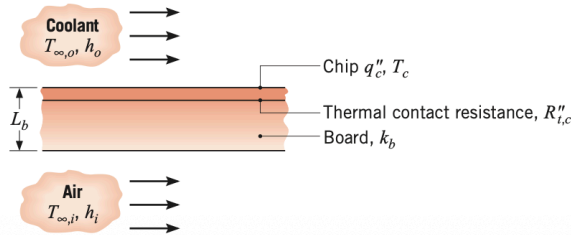
$R_{\text{contacto}}$ .

$$q = \frac{\Delta T}{R_{\text{cont.}}}$$

$$R_{\text{cont}} = \frac{\Delta T}{q}$$



3.27 Approximately  $10^6$  discrete electrical components can be placed on a single integrated circuit (chip), with electrical heat dissipation as high as  $30,000 \text{ W/m}^2$ . The chip, which is very thin, is exposed to a dielectric liquid at its outer surface, with  $h_o = 1000 \text{ W/m}^2 \cdot \text{K}$  and  $T_{\infty,o} = 20^\circ\text{C}$ , and is joined to a circuit board at its inner surface. The thermal contact resistance between the chip and the board is  $10^{-4} \text{ m}^2 \cdot \text{K/W}$ , and the board thickness and thermal conductivity are  $L_b = 5 \text{ mm}$  and  $k_b = 1 \text{ W/m} \cdot \text{K}$ , respectively. The other surface of the board is exposed to ambient air for which  $h_i = 40 \text{ W/m}^2 \cdot \text{K}$  and  $T_{\infty,i} = 20^\circ\text{C}$ .



- Sketch the equivalent thermal circuit corresponding to steady-state conditions. In variable form, label appropriate resistances, temperatures, and heat fluxes.
- Under steady-state conditions for which the chip heat dissipation is  $q_c'' = 30,000 \text{ W/m}^2$ , what is the chip temperature?

$$? \rightarrow T_c, T_{bi}, T_b, q_1, q_2$$

$$1) \quad q_g = q_1 + q_2$$

$$2) \quad q_1 = \frac{T_c - T_o}{R_{cvo}}, \quad [A] \begin{bmatrix} T_c \\ T_{bi} \\ T_b \\ q_1 \\ q_2 \end{bmatrix} = \begin{bmatrix} \end{bmatrix}$$

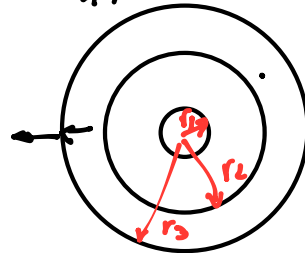
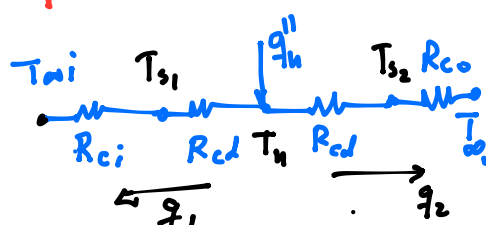
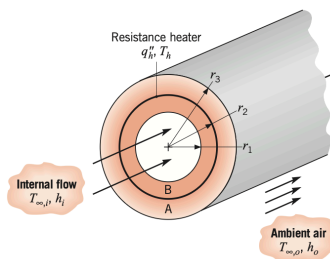
$$3) \quad q_2 = \frac{T_c - T_i}{R_{ct} + R_b + R_{cvi}}$$

$$4) \quad q_2 = \frac{T_c - T_{bi}}{R_{ct}}$$

$$5) \quad q_2 = \frac{T_{bi} - T_b}{R_{cb}}$$

3.57 A composite cylindrical wall is composed of two materials of thermal conductivity  $k_A$  and  $k_B$ , which are separated by a very thin, electric resistance

heater for which interfacial contact resistances are negligible.



Liquid pumped through the tube is at a temperature  $T_{\infty,i}$  and provides a convection coefficient  $h_i$  at the inner surface of the composite. The outer surface is exposed to ambient air, which is at  $T_{\infty,o}$  and provides a convection coefficient of  $h_o$ . Under steady-state conditions, a uniform heat flux of  $q''_h$  is dissipated by the heater.

- Sketch the equivalent thermal circuit of the system and express all resistances in terms of relevant variables.
- Obtain an expression that may be used to determine the heater temperature,  $T_h$ .
- Obtain an expression for the ratio of heat flows to the outer and inner fluids,  $q_o/q_i$ . How might the variables of the problem be adjusted to minimize this ratio?

$$R_{co} = \frac{1}{h_o (2\pi r_3)}$$

$$R_{ci} = \frac{1}{h_i (2\pi r_1)}$$

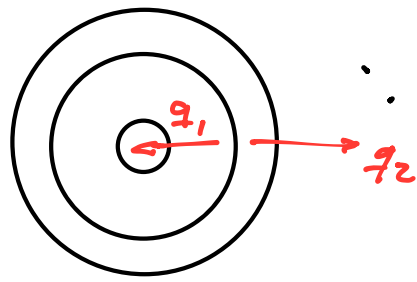
$$R_{cdB} = \frac{\ln\left(\frac{r_2}{r_1}\right)}{2\pi k_B}$$

$$R_{cdA} = \frac{\ln\left(\frac{r_3}{r_2}\right)}{2\pi k_A}$$

$$q_1 = \frac{T_h - T_{\infty,i}}{R_{ci} + R_{cdB}}$$

$$q_2 = \frac{T_h - T_{\infty,o}}{R_{cdA} + R_{co}}$$

$$q_1''(2\pi r_2) = q_1 + q_2$$



$$q_x - q_{x+dx} - dq_{\text{conv}} = 0$$

$$dq = q_{x+dx} - q_x$$

$$-\frac{dq}{dx} - \frac{dq_{\text{conv}}}{dx} = 0$$

$$-\frac{d}{dx} \left( -kA(x) \frac{dT}{dx} \right) - \frac{d}{dx} \left( \overbrace{hP dx}^{dA_s} (T - T_f) \right) = 0$$

$$\frac{d}{dx} \left( kA(x) \frac{dT}{dx} \right) - h \frac{dA_s}{dx} (T - T_f) = 0$$

$$kA(x) \frac{d^2 T}{dx^2} + k \frac{dA(x)}{dx} \frac{dT}{dx} - h \frac{dA_s}{dx} (T - T_f) = 0$$

$$kA_t \frac{d^2 T}{dx^2} - hP(T - T_f) = 0 \quad A_s = Px$$

$$\frac{d^2 T}{dx^2} - \overbrace{\frac{hP}{kA_t}}^{m^2} (T - T_f) = 0$$

$$\frac{d^2 T}{dx^2} - m^2 (T - T_f) = 0 \quad \theta = T - T_f$$

$$\frac{d^2 \theta}{dx^2} - m^2 \theta = 0$$

$$\theta = C_1 e^{-mx} + C_2 e^{mx}$$

1)  $x=0 \quad \theta(0) = \theta_b = T_b - T_f$

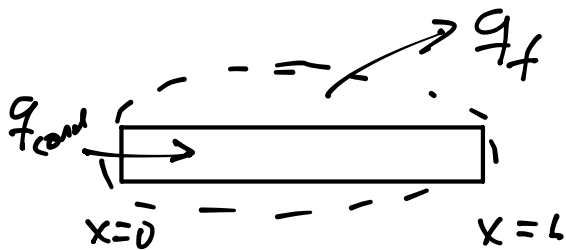
2)  $x=L$



$$-KA_t \left. \frac{d\theta}{dx} \right|_{x=L} = hA_t (\theta_{x=L})$$

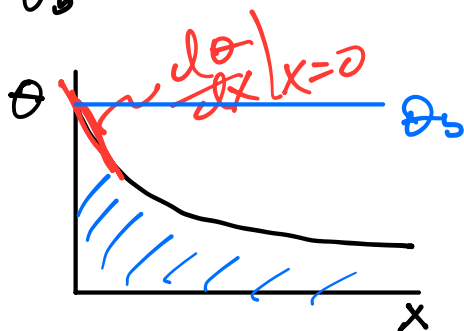
1)  $\theta_b = C_1 + C_2$

2)  $-KA_t (-C_1 m e^{-mL} + C_2 m e^{mL}) = hA_t (C_1 e^{-mL} + C_2 e^{mL})$



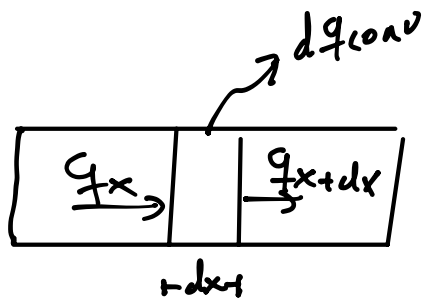
$$q_{conv} = q_f$$

$$-KA_t \left. \frac{d\theta}{dx} \right|_{x=0} = q_f$$



$$\theta = \theta_b \left( \frac{\cosh m(L-x) + (h/mk) \sinh m(L-x)}{\cosh mL + (h/mk) \sinh mL} \right)$$

$$\frac{d\theta}{dx} = \theta_b \left( \frac{m \sinh m(L-x) + (h/k) \cosh m(L-x)}{\cosh mL + (h/mk) \sinh mL} \right)$$



$$q_f = \int_L dq_{conv} = \int h P dx \theta$$

$$q_f = h P \int_0^L \theta dx$$

$$\epsilon = \frac{q_f}{q_{base}} = \frac{q_f}{h A_b \theta_b}$$

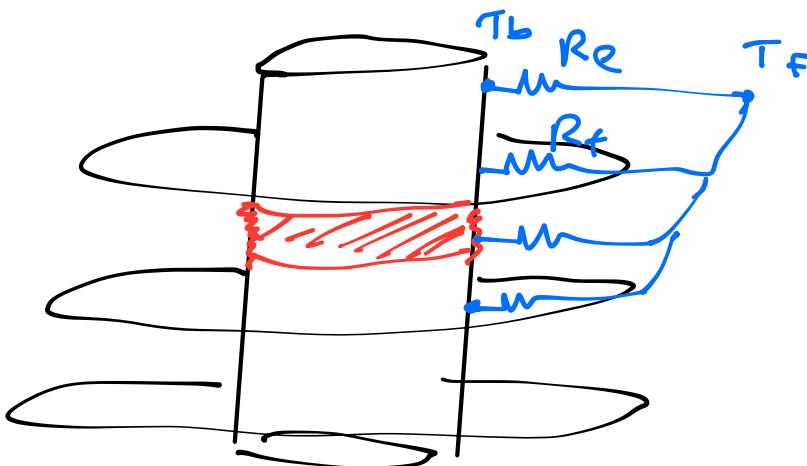
~~$$\epsilon = 1 \quad \epsilon \geq 2$$~~

$$\eta = \frac{q_f}{h A_f \theta_b} \leq 1 = \frac{q_f}{q_{max}}$$

$$q_f = \eta h A_f \theta_b$$

Ej: Aleta anular  $r_1 = 1\text{cm}$   $r_2 = 3\text{cm}$   $\delta = 2\text{mm}$   
 cobre  $h = 10\text{ W/m}^2\text{K}$   $T_\infty = 25^\circ\text{C}$   $T_b = 180^\circ\text{C}$

10 aletas separadas 5 mm  $q_{TOT} = ??$



$$q_f = \eta h A_f \theta_b$$

$$q_f = \frac{\theta_b}{\left( \frac{1}{\eta h A_f} \right)}$$

$$R_f = \frac{1}{\eta h A_f}$$