

Midterm Examination of [Signals and Systems]

2021-2022 Spring-term

Southern University of Science and Technology

Name: _____ Class: _____ Student ID: _____
Collaboration and Plagiarism are Not Allowed!

PART 1:

Choose the correct answer(s) or fill in the blank. (2'x 10=20')

- Choose all correct statements: _____
 - A system with input-output relation $y(t)=2+x(t)$ is not a linear system, where x and y are the input and output signals, respectively.
 - A causal system is a memoryless system.
 - If the input signal to a LTI system is periodic, then the output is also periodic with the same period.
 - The system $y(t)=x(t) \sin(t+1)$ is a causal system.
- For a CT LTI system, if the linear-constant-coefficient differential equation connecting input $x(t)$ and output $y(t)$ is given, we can also have _____.
 - The system function of the LTI system
 - Frequency response of the LTI system
 - The Unit impulse response of the LTI system
 - System output $y(t)$ when the input signal $x(t)$ is given
- For signal $x(t) = \delta(t)$, its Fourier transform $X(j\omega) =$ _____, and for signal $x(t) = 2\delta(t - 1)$, its Fourier transform $X(j\omega) =$ _____
- Please 1) describe the frequency response of an ideal lowpass filter, and 2) discuss whether it is a causal system and why:

- For a CT, time-limited (aperiodic) signal, its Fourier transform is _____.
 - discrete
 - continuous
 - not sure
- Please describe the steps to get the Fourier transform of a periodic signal.

The Fourier transform of a CT periodic signal is a _____ spectrum.

- a) discrete b) continuous c) Depends on the input signal

7. For a LTI system with unit impulse response $h(t)$ and input signal $x(t)$, please describe at least 2 ways to determine the output signal $y(t)$.

8. $\int_{-\infty}^3 (2t^2 + 3t) \delta\left(\frac{1}{2}t - 2\right) dt = (\quad)$

- A. 0 B. 27 C. 44 D. 88

9. The Fourier transform of $f(t)$ is $F(j\omega)$, then the Fourier transform of $f'(2t)$ is ()

- A. $j4\omega F(j2\omega)$ B. $j\frac{\omega}{4} F(j\frac{\omega}{2})$
C. $j\frac{\omega}{2} F(j\frac{\omega}{2})$ D. $j2\omega F(j2\omega)$

10. For a DT LTI system S, the shape of the frequency response of

$y[n] = (x[n] + x[n-1] + x[n-2] + x[n-3]) / 4$ is _____; while the shape of the frequency

response of $y[n] = x[n] - x[n-1]$ is _____.

- a) Low-pass filtering b) High-pass filtering
c) Band-pass filtering d) Dependent on the spectrum of the input signal $x[n]$

PART 2:

P1 (15'=10'+5')

(1) Calculate the convolution of the following two signals:

$$x(t) = \begin{cases} 1, & 0 < t < 2 \\ 0, & \text{otherwise} \end{cases}, \text{ and } h(t) = \begin{cases} t, & 0 < t < 4 \\ 0, & \text{otherwise} \end{cases}.$$

and plot the waveform of $y(t) = x(t) * h(t)$

(2) Describe a different method to compute $y(t) = x(t) * h(t)$. Elaborate the procedure without computation.

P2 (10'=2'+4'+4')

For a CT periodic signal $x(t) = \sin(\pi \cdot t / 4) + 3 \sin(\pi \cdot t / 2)$,

- (1) What is the fundamental period (T)?
(2) Represent the signal $x(t)$ in the form of Fourier series.
(3) Plot its Fourier series and Fourier transform, respectively.

P3 (20'=5'+5'+5'+5')

Consider an LTI system with impulse response $h[n]=0.3^n u[n]$, and with an periodic input

$$x[n] = \cos\left(\frac{\pi n}{4}\right) + 3\cos\left(\frac{\pi n}{2}\right)$$

- (1) Represent the input signal $x[n]$ in the form of Fourier series.
- (2) Determine the Fourier series coefficients from a_{-5} to a_2 , and a_{32} , a_{47} .
- (3) What is the frequency response of this system?
- (4) Express the system output $y[n]$ in the form of Fourier series.

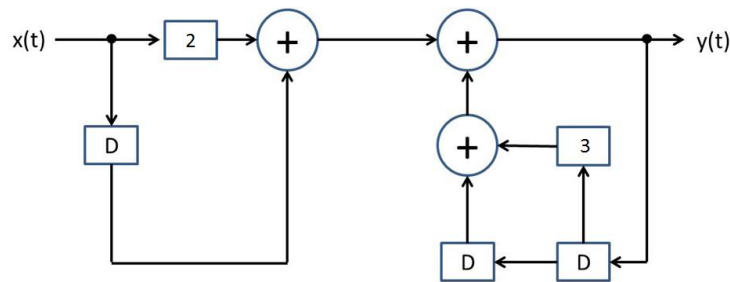
Note:

$$H(e^{j\omega}) = \sum_{n=-\infty}^{+\infty} h[n]e^{-j\omega n}$$

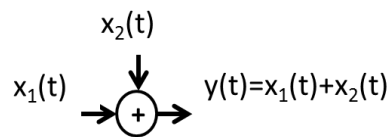
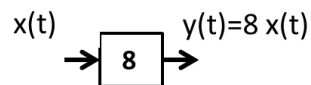
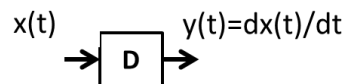
P4 (15'=10'+5')

Consider the following block diagram of an CT LTI system.

- 1) Write a differential equation relating the input $x(t)$ and output $y(t)$
- 2) Write the frequency response $H(j\omega)$ of this LTI system..



Note:

**P5 (20'=5'+5'+10')**

A causal and stable LTI system S has the frequency response of

$$H(j\omega) = \frac{Y(j\omega)}{X(j\omega)} = \frac{2j\omega + 2}{15 - \omega^2 + 8j\omega}$$

- (1) Determine a differential equation relating the input $x(t)$ and output $y(t)$ of S .
- (2) Determine the impulse response $h(t)$ of S .
- (3) What is the output of S when the input is $x(t) = e^{-t}u(t)$?