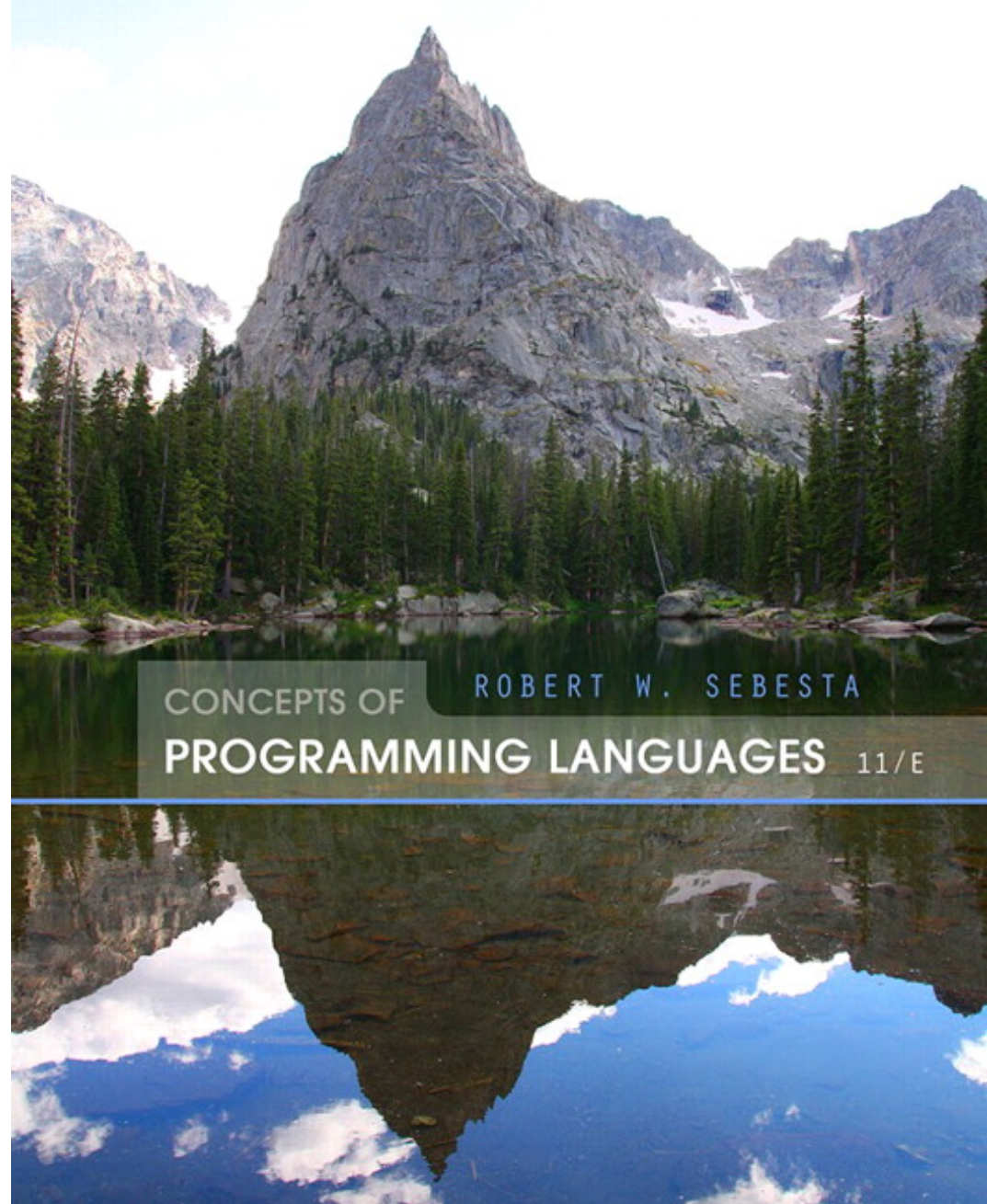


# Chapter 15

## Functional Programming Languages



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# Chapter 15 Topics

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- Introduction
- Mathematical Functions
- Fundamentals of Functional Programming Languages
- The First Functional Programming Language: Lisp
- Introduction to Scheme
- Common Lisp
- ML
- Haskell
- F#
- Support for Functional Programming in Primarily Imperative Languages
- Comparison of Functional and Imperative Languages

# Introduction

---

- The design of the imperative languages is based directly on the *von Neumann architecture*
  - Efficiency is the primary concern, rather than the suitability of the language for software development
- The design of the functional languages is based on *mathematical functions*
  - A solid theoretical basis that is also closer to the user, but relatively unconcerned with the architecture of the machines on which programs will run

# Mathematical Functions

---

- A mathematical function is a *mapping* of members of one set, called the *domain set*, to another set, called the *range set*
- A *lambda expression* specifies the parameter(s) and the mapping of a function in the following form

$$\lambda (x) \quad x * x * x$$

for the function  $\text{cube}(x) = x * x * x$

# Lambda Expressions

---

- Lambda expressions describe nameless functions
- Lambda expressions are applied to parameter(s) by placing the parameter(s) after the expression

e.g.,  $(\lambda (x) \ x * x * x) (2)$

which evaluates to 8

# Functional Forms

---

- A higher-order function, or *functional form*, is one that either takes functions as parameters or yields a function as its result, or both

# Function Composition

---

- A functional form that takes two functions as parameters and yields a function whose value is the first actual parameter function applied to the application of the second

Form:  $h \equiv f \circ g$

which means  $h(x) \equiv f(g(x))$

For  $f(x) \equiv x + 2$  and  $g(x) \equiv 3 * x$ ,

$h \equiv f \circ g$  **yields**  $(3 * x) + 2$

# Apply-to-all

---

- A functional form that takes a single function as a parameter and yields a list of values obtained by applying the given function to each element of a list of parameters

Form:  $\alpha$

For  $h(x) \equiv x * x$

$\alpha(h, (2, 3, 4))$  yields (4, 9, 16)



# Fundamentals of Functional Programming Languages

---

- The objective of the design of a FPL is to mimic mathematical functions to the greatest extent possible
- The basic process of computation is fundamentally different in a FPL than in an imperative language
  - In an imperative language, operations are done and the results are stored in variables for later use
  - Management of variables is a constant concern and source of complexity for imperative programming
- In an FPL, variables are not necessary, as is the case in mathematics
- *Referential Transparency* – In an FPL, the evaluation of a function always produces the same result given the same parameters

# Lisp Data Types and Structures

---

- *Data object types*: originally only atoms and lists
- *List form*: parenthesized collections of sublists and/or atoms  
e.g., (A B (C D) E)
- Originally, Lisp was a typeless language
- Lisp lists are stored internally as single-linked lists

# Lisp Interpretation

---

- Lambda notation is used to specify functions and function definitions. Function applications and data have the same form.

e.g., If the list (A B C) is interpreted as data it is a simple list of three atoms, A, B, and C

If it is interpreted as a function application, it means that the function named A is applied to the two parameters, B and C

- The first Lisp interpreter appeared only as a demonstration of the universality of the computational capabilities of the notation

# Origins of Scheme

---

- A mid-1970s dialect of Lisp, designed to be a cleaner, more modern, and simpler version than the contemporary dialects of Lisp
- Uses only static scoping
- Functions are first-class entities
  - They can be the values of expressions and elements of lists
  - They can be assigned to variables, passed as parameters, and returned from functions

# The Scheme Interpreter

---

- In interactive mode, the Scheme interpreter is an infinite read–evaluate–print loop (REPL)
  - This form of interpreter is also used by Python and Ruby
- Expressions are interpreted by the function `EVAL`
- Literals evaluate to themselves

# Primitive Function Evaluation

---

- Parameters are evaluated, in no particular order
- The values of the parameters are substituted into the function body
- The function body is evaluated
- The value of the last expression in the body is the value of the function

# Primitive Functions & LAMBDA Expressions

---

- **Primitive Arithmetic Functions:** `+`, `-`, `*`, `/`, `ABS`, `SQRT`, `REMAINDER`, `MIN`, `MAX`  
e.g., `(+ 5 2)` yields 7
- **Lambda Expressions**
  - Form is based on  $\lambda$  notation  
e.g., `(LAMBDA (x) (* x x))`  
`x` is called a bound variable
- Lambda expressions can be applied to parameters  
e.g., `((LAMBDA (x) (* x x)) 7)`
- LAMBDA expressions can have any number of parameters  
`(LAMBDA (a b x) (+ (* a x x) (* b x)))`

# Special Form Function: DEFINE

---

- DEFINE – Two forms:

1. To bind a symbol to an expression

e.g., `(DEFINE pi 3.141593)`

Example use: `(DEFINE two_pi (* 2 pi))`

These symbols are not variables – they are like the names bound by Java's `final` declarations

2. To bind names to lambda expressions (`LAMBDA` is implicit)

e.g., `(DEFINE (square x) (* x x))`

Example use: `(square 5)`

- The evaluation process for `DEFINE` is different! The first parameter is never evaluated. The second parameter is evaluated and bound to the first parameter.



# Output Functions

---

- Usually not needed, because the interpreter always displays the result of a function evaluated at the top level (not nested)
- Scheme has `PRINTF`, which is similar to the `printf` function of C
- Note: explicit input and output are not part of the pure functional programming model, because input operations change the state of the program and output operations are side effects

# Numeric Predicate Functions

---

- $\#T$  (or  $\#t$ ) is true and  $\#F$  (or  $\#f$ ) is false (sometimes  $()$  is used for false)
- $=$ ,  $<>$ ,  $>$ ,  $<$ ,  $>=$ ,  $<=$
- `EVEN?`, `ODD?`, `ZERO?`, `NEGATIVE?`
- The `NOT` function inverts the logic of a Boolean expression

# Control Flow

---

- Selection– the special form, `IF`

`(IF predicate then_exp else_exp)`

```
(IF (<> count 0)
    (/ sum count)
)
```

- Recall from Chapter 8 the `COND` function:

```
(DEFINE (leap? year)
  (COND
    ((ZERO? (MODULO year 400)) #T)
    ((ZERO? (MODULO year 100)) #F)
    (ELSE (ZERO? (MODULO year 4)))
  ))
```

# List Functions

---

- `QUOTE` – takes one parameter; returns the parameter without evaluation
  - `QUOTE` is required because the Scheme interpreter, named `EVAL`, always evaluates parameters to function applications before applying the function. `QUOTE` is used to avoid parameter evaluation when it is not appropriate
  - `QUOTE` can be abbreviated with the apostrophe prefix operator
    - ' (A B) is equivalent to (`QUOTE` (A B))
- Recall that `CAR`, `CDR`, and `CONS` were covered in Chapter 6

# List Functions (continued)

---

- Examples:

(CAR ' ( (A B) C D) ) **returns** (A B)

(CAR 'A) **is an error**

(CDR ' ( (A B) C D) ) **returns** (C D)

(CDR 'A) **is an error**

(CDR ' (A) ) **returns** ()

(CONS ' () ' (A B) ) **returns** ( () A B)

(CONS ' (A B) ' (C D) ) **returns** ( (A B) C D)

(CONS 'A 'B) **returns** (A . B) (*a dotted pair*)

# List Functions (continued)

---

- `LIST` is a function for building a list from any number of parameters

`(LIST 'apple 'orange 'grape)` returns

`(apple orange grape)`

# Predicate Function: EQ?

---

- EQ? takes two expressions as parameters (usually two atoms); it returns #T if both parameters have the same pointer value; otherwise #F

(EQ? 'A 'A) yields #T

(EQ? 'A 'B) yields #F

(EQ? 'A '(A B)) yields #F

(EQ? '(A B) '(A B)) yields #T or #F

(EQ? 3.4 (+ 3 0.4)) yields #T or #F

# Predicate Function: EQV?

---

- EQV? is like EQ?, except that it works for both symbolic and numeric atoms; it is a value comparison, not a pointer comparison

(EQV? 3 3) yields #T

(EQV? 'A 3) yields #F

(EQV 3.4 (+ 3 0.4)) yields #T

(EQV? 3.0 3) yields #F (floats and integers are different)



# Predicate Functions: LIST? and NULL?

---

- **LIST?** takes one parameter; it returns #T if the parameter is a list; otherwise #F  
`(LIST? ' ( ) )` yields #T
- **NULL?** takes one parameter; it returns #T if the parameter is the empty list; otherwise #F  
`(NULL? ' ( ( ) ) )` yields #F

# Example Scheme Function: `member`

---

- `member` takes an atom and a simple list; returns `#T` if the atom is in the list; `#F` otherwise

```
DEFINE (member atm a_list)
  (COND
    ((NULL? a_list) #F)
    ((EQ? atm (CAR lis)) #T)
    ((ELSE (member atm (CDR a_list))))
  ))
```

# Example Scheme Function: `equalsimp`

---

- `equalsimp` takes two simple lists as parameters; returns `#T` if the two simple lists are equal; `#F` otherwise

```
(DEFINE (equalsimp list1 list2)
  (COND
    ((NULL? list1) (NULL? list2))
    ((NULL? list2) #F)
    ((EQ? (CAR list1) (CAR list2))
      (equalsimp (CDR list1) (CDR list2)))
    (ELSE #F)
  ))
```

# Example Scheme Function: `equal`

---

- `equal` takes two general lists as parameters; returns `#T` if the two lists are equal; `#F` otherwise

```
(DEFINE (equal list1 list2)
  (COND
    ((NOT (LIST? list1)) (EQ? list1 list2))
    ((NOT (LIST? list2)) #F)
    ((NULL? list1) (NULL? list2))
    ((NULL? list2) #F)
    ((equal (CAR list1) (CAR list2))
     (equal (CDR list1) (CDR list2)))
    (ELSE #F)
  ))
```

# Example Scheme Function: `append`

---

- `append` takes two lists as parameters; returns the first parameter list with the elements of the second parameter list appended at the end

```
(DEFINE (append list1 list2)
  (COND
    ((NULL? list1) list2)
    (ELSE (CONS (CAR list1)
                  (append (CDR list1) list2)))
  ))
```

# Example Scheme Function: LET

---

- Recall that `LET` was discussed in Chapter 5
- `LET` is actually shorthand for a `LAMBDA` expression applied to a parameter

```
(LET ((alpha 7)) (* 5 alpha))
```

is the same as:

```
((LAMBDA (alpha) (* 5 alpha)) 7)
```

# LET Example

---

```
(DEFINE (quadratic_roots a b c)
  (LET (
    (root_part_over_2a
      (/ (SQRT (- (* b b) (* 4 a c))) (* 2 a)))
    (minus_b_over_2a (/ (- 0 b) (* 2 a)))
    (LIST (+ minus_b_over_2a root_part_over_2a)
          (- minus_b_over_2a root_part_over_2a))
  ))
```

# Tail Recursion in Scheme

---

- Definition: A function is *tail recursive* if its recursive call is the last operation in the function
- A tail recursive function can be automatically converted by a compiler to use iteration, making it faster
- Scheme language definition requires that Scheme language systems convert all tail recursive functions to use iteration



# Tail Recursion in Scheme – continued

---

- Example of rewriting a function to make it tail recursive, using helper a function

Original:

```
(DEFINE (factorial n)
  (IF (<= n 0)
      1
      (* n (factorial (- n 1)))
  ))
```

Tail recursive:

```
(DEFINE (facthelper n factpartial)
  (IF (<= n 0)
      factpartial
      facthelper((- n 1) (* n factpartial)))
  ))

(DEFINE (factorial n)
  (facthelper n 1))
```

# Functional Form – Composition

---

- **Composition**

- If  $h$  is the composition of  $f$  and  $g$ ,  $h(x) = f(g(x))$

```
(DEFINE (g x) (* 3 x))
```

```
(DEFINE (f x) (+ 2 x))
```

```
(DEFINE h x) (+ 2 (* 3 x))) (The composition)
```

- In Scheme, the functional composition function `compose` can be written:

```
(DEFINE (compose f g) (LAMBDA (x) (f (g x))))
```

```
((compose CAR CDR) '((a b) c d)) yields c
```

```
(DEFINE (third a_list)
```

```
((compose CAR (compose CDR CDR)) a_list))
```

**is equivalent to** `CADDR`

# Functional Form – Apply-to-All

---

- Apply to All – one form in Scheme is `map`
  - Applies the given function to all elements of the given list;

```
(DEFINE (map fun a_list)
  (COND
    ((NULL? a_list) '())
    (ELSE (CONS (fun (CAR a_list))
                  (map fun (CDR a_list))))
  ))
```

```
(map (LAMBDA (num) (* num num num)) '(3 4 2 6)) yields
(27 64 8 216)
```

# Functions That Build Code

---

- It is possible in Scheme to define a function that builds Scheme code and requests its interpretation
- This is possible because the interpreter is a user-available function, `EVAL`

# Adding a List of Numbers

---

```
((DEFINE (adders a_list)
  (COND
    ((NULL? a_list) 0)
    (ELSE (EVAL (CONS '+ a_list))))
))
```

- The parameter is a list of numbers to be added; `adders` inserts a `+` operator and evaluates the resulting list
  - Use `CONS` to insert the atom `+` into the list of numbers.
  - Be sure that `+` is quoted to prevent evaluation
  - Submit the new list to `EVAL` for evaluation

# Common Lisp

---

- A combination of many of the features of the popular dialects of Lisp around in the early 1980s
- A large and complex language--the opposite of Scheme
- Features include:
  - records
  - arrays
  - complex numbers
  - character strings
  - powerful I/O capabilities
  - packages with access control
  - iterative control statements

# Common Lisp (continued)

---

- Macros
  - Create their effect in two steps:
    - Expand the macro
    - Evaluate the expanded macro
- Some of the predefined functions of Common Lisp are actually macros
- Users can define their own macros with `DEFMACRO`

# Common Lisp (continued)

---

- Backquote operator (```)
  - Similar to the Scheme's `QUOTE`, except that some parts of the parameter can be unquoted by preceding them with commas

``(a (* 3 4) c)` evaluates to `(a (* 3 4) c)`

``(a , (* 3 4) c)` evaluates to `(a 12 c)`



# Common Lisp (continued)

---

- Reader Macros

- Lisp implementations have a front end called the *reader* that transforms Lisp into a code representation. Then macro calls are expanded into the code representation.
- A reader macro is a special kind of macro that is expanded during the reader phase
- A reader macro is a definition of a single character, which is expanded into its Lisp definition
- An example of a reader macro is an apostrophe character, which is expanded into a call to `QUOTE`
- Users can define their own reader macros as a kind of shorthand

# Common Lisp (continued)

---

- Common Lisp has a symbol data type (similar to that of Ruby)
  - The reserved words are symbols that evaluate to themselves
  - Symbols are either bound or unbound
    - Parameter symbols are bound while the function is being evaluated
    - Symbols that are the names of imperative style variables that have been assigned values are bound
    - All other symbols are unbound

# ML

---

- A static-scoped functional language with syntax that is closer to Pascal than to Lisp
- Uses type declarations, but also does *type inferencing* to determine the types of undeclared variables
- It is strongly typed (whereas Scheme is essentially typeless) and has no type coercions
- Does not have imperative-style variables
- Its identifiers are untyped names for values
- Includes exception handling and a module facility for implementing abstract data types
- Includes lists and list operations

# ML Specifics

---

- A table called the *evaluation environment* stores the names of all identifiers in a program, along with their types (like a run-time symbol table)
- Function declaration form:

**fun** *name* (*formal parameters*) = *expression*;

e.g., **fun** cube (*x* : **int**) = *x* \* *x* \* *x*;

- The type could be attached to return value, as in  
**fun** cube (*x*) : **int** = *x* \* *x* \* *x*;
- With no type specified, it would default to **int** (the default for numeric values)
- User-defined overloaded functions are not allowed, so if we wanted a `cube` function for real parameters, it would need to have a different name

# ML Specifics (continued)

---

- ML selection

*if expression then then\_expression  
else else\_expression*

where the first expression must evaluate to a Boolean value

- Pattern matching is used to allow a function to operate on different parameter forms

```
fun fact(0) = 1
|   fact(1) = 1
|   fact(n : int) : int = n * fact(n - 1)
```

# ML Specifics (continued)

---

- Lists

Literal lists are specified in brackets

`[3, 5, 7]`

`[]` is the empty list

`CONS` is the binary infix operator, `::`

`4 :: [3, 5, 7]`, which evaluates to `[4, 3, 5, 7]`

`CAR` is the unary operator `hd`

`CDR` is the unary operator `tl`

```
fun length([]) = 0
```

```
| length(h :: t) = 1 + length(t);
```

```
fun append([], lis2) = lis2
```

```
| append(h :: t, lis2) = h :: append(t, lis2);
```

# ML Specifics (continued)

---

- The `val` statement binds a name to a value (similar to `DEFINE` in Scheme)

```
val distance = time * speed;
```

- As is the case with `DEFINE`, `val` is nothing like an assignment statement in an imperative language
- If there are two `val` statements for the same identifier, the first is hidden by the second
- `val` statements are often used in `let` constructs

```
let
```

```
    val radius = 2.7
```

```
    val pi = 3.14159
```

```
in
```

```
    pi * radius * radius
```

```
end;
```

# ML Specifics (continued)

---

- `filter`
  - A higher-order filtering function for lists
  - Takes a predicate function as its parameter, often in the form of a lambda expression
  - Lambda expressions are defined like functions, except with the reserved word `fn`

```
filter(fn(x) => x < 100, [25, 1, 711, 50, 100]);
```

This returns `[25, 1, 50]`



# ML Specifics (continued)

---

- `map`
  - A higher-order function that takes a single parameter, a function
  - Applies the parameter function to each element of a list and returns a list of results

```
fun cube x = x * x * x;
```

```
val cubeList = map cube;
```

```
val newList = cubeList [1, 3, 5];
```

This sets `newList` to `[1, 27, 125]`

- Alternative: use a lambda expression

```
val newList = map (fn x => x * x * x, [1, 3, 5]);
```

# ML Specifics (continued)

---

- Function Composition
  - Use the unary operator,  $\circ$

```
val h = g o f;
```

# ML Specifics (continued)

---

- Currying

- ML functions actually take just one parameter—if more are given, it considers the parameters a tuple (commas required)
- Process of *currying* replaces a function with more than one parameter with a function with one parameter that returns a function that takes the other parameters of the original function
- An ML function that takes more than one parameter can be defined in curried form by leaving out the commas in the parameters

**fun** add a b = a + b;

A function with one parameter, a. Returns a function that takes b as a parameter. Call: add 3 5;

# ML Specifics (continued)

---

- Partial Evaluation

- Curried functions can be used to create new functions by partial evaluation
- Partial evaluation means that the function is evaluated with actual parameters for one or more of the leftmost actual parameters

```
fun add5 x add 5 x;
```

Takes the actual parameter 5 and evaluates the `add` function with 5 as the value of its first formal parameter. Returns a function that adds 5 to its single parameter

```
val num = add5 10;  (* sets num to 15 *)
```

# Haskell

---

- Similar to ML (syntax, static scoped, strongly typed, type inferencing, pattern matching)
- Different from ML (and most other functional languages) in that it is *purely* functional (e.g., no variables, no assignment statements, and no side effects of any kind)

## Syntax differences from ML

```
fact 0 = 1
```

```
fact 1 = 1
```

```
fact n = n * fact (n - 1)
```

```
fib 0 = 1
```

```
fib 1 = 1
```

```
fib (n + 2) = fib (n + 1) + fib n
```

# Function Definitions with Different Parameter Ranges

---

```
fact n
  | n == 0 = 1
  | n == 1 = 1
  | n > 0 = n * fact (n - 1)
```

```
sub n
  | n < 10      = 0
  | n > 100     = 2
  | otherwise   = 1
```

```
square x = x * x
```

- Because Haskell support polymorphism, this works for any numeric type of  $x$

# Haskell Lists

---

- List notation: Put elements in brackets  
e.g., `directions = ["north", "south", "east", "west"]`
- Length: `#`  
e.g., `#directions` is 4
- Arithmetic series with the `..` operator  
e.g., `[2, 4..10]` is `[2, 4, 6, 8, 10]`
- Catenation is with `++`  
e.g., `[1, 3] ++ [5, 7]` results in `[1, 3, 5, 7]`
- `CONS`, `CAR`, `CDR` via the colon operator  
e.g., `1:[3, 5, 7]` results in `[1, 3, 5, 7]`

# Haskell (continued)

---

- Pattern Parameters

```
product [] = 1
product (a:x) = a * product x
```

- Factorial:

```
fact n = product [1..n]
```

- List Comprehensions (Chapter 6)

```
[n * n * n | n <- [1..50]]
```

The qualifier in this example has the form of a *generator*. It could be in the form of a test

```
factors n = [i | i <- [1..n `div` 2], n `mod` i == 0]
```

The backticks specify the function is used as a binary operator



# Quicksort

---

```
sort [] = []
sort (h:t) =
    sort [b | b <- t; b <= h]
  ++ [h] ++
    sort [b | b <- t; b > h]
```

Illustrates the concision of Haskell

# Lazy Evaluation

---

- A language is *strict* if it requires all actual parameters to be fully evaluated
- A language is *nonstrict* if it does not have the strict requirement
- Nonstrict languages are more efficient and allow some interesting capabilities – *infinite lists*
- Lazy evaluation – Only compute those values that are necessary

- Positive numbers

```
positives = [0..]
```

- Determining if 16 is a square number

```
member [] b = False
```

```
member (a:x) b = (a == b) || member x b
```

```
squares = [n * n | n ← [0..]]
```

```
member squares 16
```

# Member Revisited

---

- The member function could be written as:

```
member b [] = False
member b (a:x)=(a == b) || member b x
```

- However, this would only work if the parameter to squares was a perfect square; if not, it will keep generating them forever. The following version will always work:

```
member2 n (m:x)
  | m < n = member2 n x
  | m == n = True
  | otherwise = False
```

# F#

---

- Based on Ocaml, which is a descendant of ML and Haskell
- Fundamentally a functional language, but with imperative features and supports OOP
- Has a full-featured IDE, an extensive library of utilities, and interoperates with other .NET languages
- Includes tuples, lists, discriminated unions, records, and both mutable and immutable arrays
- Supports generic sequences, whose values can be created with generators and through iteration

# F# (continued)

---

- Sequences

```
let x = seq {1..4};;
```

- Generation of sequence values is lazy

```
let y = seq {0..100000000};;
```

```
Sets y to [0; 1; 2; 3;...]
```

- Default stepsize is 1, but it can be any number

```
let seq1 = seq {1..2..7}
```

```
Sets seq1 to [1; 3; 5; 7]
```

- Iterators – not lazy for lists and arrays

```
let cubes = seq {for i in 1..4 -> (i, i * i * i)};;
```

```
Sets cubes to [(1, 1); (2, 8); (3, 27); (4, 64)]
```

# F# (continued)

---

- Functions

- If named, defined with `let`; if lambda expressions, defined with `fun`

```
(fun a b -> a / b)
```

- No difference between a name defined with `let` and a function without parameters
  - The extent of a function is defined by indentation

```
let f =
```

```
    let pi = 3.14159
```

```
    let twoPi = 2.0 * pi;;
```

# F# (continued)

---

- Functions (continued)

- If a function is recursive, its definition must include the `rec` reserved word
- Names in functions can be outscoped, which ends their scope

```
let x4 =  
    let x = x * x  
    let x = x * x
```

The first `let` in the body of the function creates a new version of `x`; this terminates the scope of the parameter; The second `let` in the body creates another `x`, terminating the scope of the second `x`

# F# (continued)

---

- Functional Operators

- Pipeline (`|>`)
- A binary operator that sends the value of its left operand to the last parameter of the call (the right operand)

```
let myNums = [1; 2; 3; 4; 5]
let evenTimesFive = myNums
    |> List.filter (fun n -> n % 2 = 0)
    |> List.map (fun n -> 5 * n)
```

The return value is `[10; 20]`

||

- `;!kj;`



# F# (continued)

---

- Functional Operators (continued)

- Composition ( $>>$ )

- Builds a function that applies its left operand to a given parameter (a function) and then passes the result returned from the function to its right operand (another function)

The F# expression  $(f \gg g) \ x$  is equivalent to the mathematical expression  $g(f(x))$

- Curried Functions

```
let add a b = a + b;;
```

```
let add5 = add 5;;
```

# F# (continued)

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- Why F# is Interesting:
  - It builds on previous functional languages
  - It supports virtually all programming methodologies in widespread use today
  - It is the first functional language that is designed for interoperability with other widely used languages
  - At its release, it had an elaborate and well-developed IDE and library of utility software

# Support for Functional Programming in Primarily Imperative Languages

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- Support for functional programming is increasingly creeping into imperative languages
  - Anonymous functions (lambda expressions)
    - JavaScript: leave the name out of a function definition
    - C#: `i => (i % 2) == 0` (returns true or false depending on whether the parameter is even or odd)
    - Python: `lambda a, b : 2 * a - b`

# Support for Functional Programming in Primarily Imperative Languages (continued)

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- Python supports the higher-order functions filter and map (often use lambda expressions as their first parameters)

```
map(lambda x : x ** 3, [2, 4, 6, 8])
```

Returns [8, 64, 216, 512]

- Python supports partial function applications

```
from operator import add
```

```
add5 = partial (add, 5)
```

(the first line imports add as a function)

Use: add5(15)

# Support for Functional Programming in Primarily Imperative Languages (continued)

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- Ruby Blocks

- Are effectively subprograms that are sent to methods, which makes the method a higher-order subprogram
- A block can be converted to a subprogram object with `lambda`

```
times = lambda {|a, b| a * b}
```

**Use:** `x = times.(3, 4)` (sets `x` to 12)

- Times can be curried with

```
times5 = times.curry.(5)
```

**Use:** `x5 = times5.(3)` (sets `x5` to 15)

# Comparing Functional and Imperative Languages

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- Imperative Languages:
  - Efficient execution
  - Complex semantics
  - Complex syntax
  - Concurrency is programmer designed
- Functional Languages:
  - Simple semantics
  - Simple syntax
  - Less efficient execution
  - Programs can automatically be made concurrent

# Summary

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- Functional programming languages use function application, conditional expressions, recursion, and functional forms to control program execution
- Lisp began as a purely functional language and later included imperative features
- Scheme is a relatively simple dialect of Lisp that uses static scoping exclusively
- Common Lisp is a large Lisp-based language
- ML is a static-scoped and strongly typed functional language that uses type inference
- Haskell is a lazy functional language supporting infinite lists and set comprehension.
- F# is a .NET functional language that also supports imperative and object-oriented programming
- Some primarily imperative languages now incorporate some support for functional programming
- Purely functional languages have advantages over imperative alternatives, but still are not very widely used