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### Functions: as Mapping Rules

The function constructor defines a function's \_\_\_\_\_ (i.e., it's domain- and range-sets), but not its \_\_\_\_\_ (i.e., indicate the domain-to-range element mappings).

Behavior can be defined via a *domain-to-range mapping rule*:

Example: In C++, we can *specify* that:  $abs(int) \rightarrow int$  but to define the *behavior* of abs(), we need a rule:

A *mapping rule* must specify the range-value for each domain-value for which the function is defined.

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## Functions: as Algorithms

An alternative way to specify behavior is to specify:

- •the function's \_\_\_\_\_•the function's \_\_\_\_\_
- •a \_\_\_\_\_ for computing the result, using the parameters.

"Lisp"

```
(defun abs (val)
  (if (>= val 0)
    val
     (- 0 val) ))

"Smalltalk (Number method)"
abs
  self >= 0
```

abs
self >= 0
ifTrue: ^self
ifFalse: ^(0 - self).

Some like to view a HLL as a \_\_\_\_

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#### **Functions and Operators**

Most *functions* can be defined as *operators*, and vice versa.

Example: Ada provides an exponentiation operator \_\_\_\_\_ where C++ provides an exponentiation function \_\_\_\_\_.

So a 3rd-order polynomial can be expressed in C++ as y = a \* pow(x,3) + b \* pow(x,2) + c \* x + d; or in Ada as:

y = a \* x \*\* 3 + b \* x \*\* 2 + c \* x + d;

Superficially, functions and operators are *equivalent*:

- The \_\_\_\_\_ of a function ≡ the \_\_\_\_\_ of an operator.

- A *function* can be thought of as a \_\_\_\_\_\_.

#### Functions: as Abstractions

Others prefer to view functions as an abstraction mechanism:

- the ability to \_\_\_\_\_\_...

Example: If a library provides a *summation()* function, it might use any of these algorithms:

```
// iterative algorithm
int summation(int n) {
  int result = 1;
  for (int i = 2; i <= n; i++)
    result += i;
  return result;
}</pre>
```

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```
// recursive algorithm
int summation(int n) {
  if (n >= 2)
    return n + summation(n-1);
  else
    return 1;
}
```

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```
// using Gauss' formula
int summation(int n) {
  return n * (n+1) / 2;
}
```

The name *summation()* is an *abstraction* that hides the details of the particular algorithm it uses.

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#### Functions: as Subprograms Imperative HLLs divide functions into two categories: $\_$ : subprograms that map: $(P_1 \times P_2 \times ... \times P_n) \rightarrow \emptyset$ \_: subprograms that map: $(P_1 \times P_2 \times ... \times P_n) \rightarrow R \neq \emptyset$ There are no standard names for these categories: $(D) \rightarrow \emptyset$ $(D) \rightarrow R$ HLL C/C++ void function function Fortran subroutine function **Pascal** procedure function Modula-2 proper procedure function procedure procedure Ada function We will describe subprograms mapping (D) $\rightarrow$ R as functions, and describe subprograms mapping (D) $\rightarrow \emptyset$ as procedures. © Joel C. Adams. All Rights Reserved. Dept of Computer Science Calvin College

Functions: as Messages				
OO languages view for	unctions as	·		
The receiver of a message executes its				
- The result is controlled by the, not the <i>sender</i> .				
Different OO languages use different syntax for messages				
Example: To find the length of anArray, we send it a message:				
// C++ anArray->length()	// Java anArray.length	// Smalltalk anArray size		
Example: To find the length of <i>aString</i> , we send it a message:				
<pre>// C++ aString-&gt;length()</pre>	// Java aString.length()	// Smalltalk aString size		
Messages are something like				
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nuage must provide: pecifying its behavior); activating it).
ning is to:; and
ion(int n) { * (n+1) / 2;
; and
Idress in that storage.

Definitions vs. Declarations			
Where a <i>definition</i> binds a rate a binds a rate a	<i>3</i> ,		
Example: This is a C++ declaration:  because it tells the compile	er this about summation:		
	ype-check calls to the function.		
For a <i>variable</i> , declaration and definition are			
int result:	nt reserves a word of memory, and ame <i>result</i> to the address of that word.		
For subprograms, declaration	on and definition		
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C/C++ Function Pointers			
Implication of a function <i>definition</i> :			
a C/C++ function's name is a	·		
Example: If <i>summation</i> and <i>factorial</i> are two functions:			
	<pre>int summation(int n) { return n * (n+1) / 2; } int factorial(int n) { definition of factorial }</pre>		
then we can declare a pointer type:	<pre>typedef int * fptr(int);</pre>		
use it to define a pointer array:	<pre>fptr fTable[2];</pre>		
initialize our array:	<pre>fTable[0] = summation; fTable[1] = factorial;</pre>		
and then call either function:	<pre>cout &lt;&lt; fTable[i](n);</pre>		
Classes use a similar table for			
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	Subprogram Definitions		
To alloc	ate a subprogram's storage, 4 items are needed:		
1. Its _	(data storage for values sent by the caller);		
2. Its _	s (data storage for the return value);		
3. Its _	s (data storage for local variables); and		
4. Its _	or statements (executable code storage).		
These ar	re all provided by a subprogram's definition.		
By contr	rast, a subprogram's declaration requires only:		
1. Its	(i.e., its domain-set <i>D</i> ); and		
2. Its	(i.e., its range-set <i>R</i> )		
This _	$f(D) \rightarrow R$		
lets th	e compiler check <i>calls</i> to the function for correctness.		
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#### Imperative Examples

Consider these imperative function definitions:

```
// C++
void swap(int & a, int & b) {
  int t = a; a = b; b = t;
}

-- Ada
procedure swap(a, b: in out integer) is
integer t;
begin
  t := a; a := b; b := t;
end swap;
```

In each case, we have:

This allows the compiler to check that in calls: swap(x, y); the arguments x and y are compatible with the parameters.

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## Subprograms: Lisp and Smalltalk

A Lisp subprogram definition uses the \_\_\_\_\_ function:

```
"Lisp"
(defun factorial (n)
   if (< n 2)
    1
    (* n (factorial (- n 1) )) )
```

When evaluated, *defun* parses the function that follows it and (assuming no errors) creates a symbol table entry for it.

A Smalltalk subprogram must be

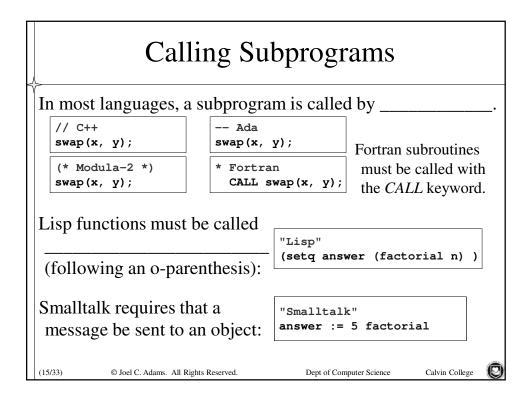
On an *accept event*, Smalltalk parses the method and (assuming no errors) creates a symbol table entry for it.

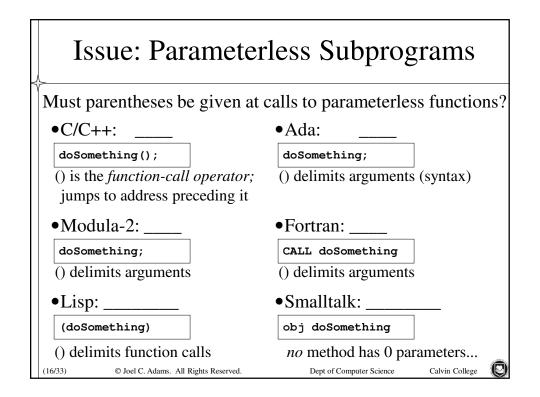
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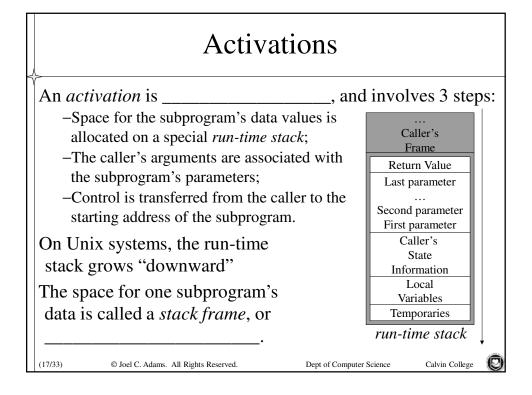
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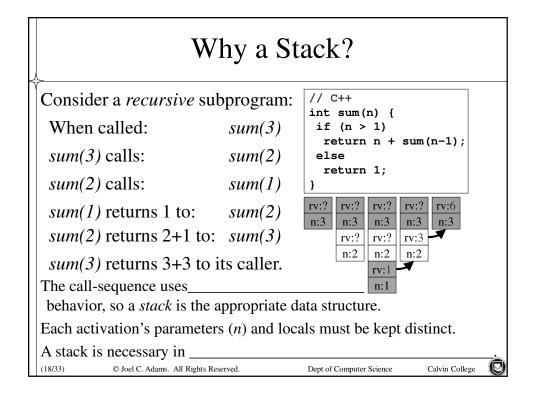
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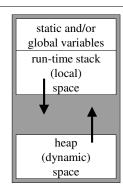




#### Memory Layout

On Unix systems, a program's data space is laid out something like this:

- Space for static/global variables
- •The *run-time stack* for locals, parameters, etc.
- The *heap* for dynamically allocated variables.



This flexible design uses memory efficiently: A typical program only runs out of memory if

- its stack overruns its heap (\_\_\_\_\_\_), or
- its heap overruns its stack (\_\_\_\_\_\_).

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### Parameter Passing

Parameters are allocated space \_\_\_\_\_

on the run-time stack.

Before control is transferred to the subprogram, the call's arguments are "associated with" these parameters.

Return Value

Last parameter
....
Second parameter
First parameter
Caller's
State
Information
Local
Variables
Temporaries

Exactly how arguments get associated with parameters depends on the *parameter passing mechanism* being used.

There are *four* general mechanisms: \_\_\_\_\_

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# Call-by-Value Parameters

.. are \_\_\_\_\_ into which their arguments are \_\_\_

- Changing a parameter doesn't affect its argument's value.
- This is the *default* mechanism in most languages.
- This is the *only* mechanism in C, Lisp, Java, Smalltalk, ...

```
// C++
int summ (int a, int b) {
  return (a+b) * (b-a+1) / 2;
}
```

```
"Lisp"
(defun summ (a b)
(/ (* (+ a b) (+ (- b a) 1))
2) )
```

"Smalltalk Integer method"
summ: b
^(self+b) \* (b-self+1) / 2

In Ada, *in* is optional, but is considered good programming style.

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# When function *summ()* is called

// C++ total = summ(x, y);

- An activation record for *summ()* containing space for *a* and *b* is pushed onto the run-time stack.
- The arguments are evaluated and copied into their parameters.
- Control is transferred to summ()
   which executes and computes its return-value.

- *summ()*'s AR is popped, and control returns to the caller which retrieves the return-value from just "above" its stack-frame.

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#### Call-by-Reference Parameters

.. are \_\_\_\_\_ storing

that are auto-dereferenced whenever they are accessed.

- The parameter is an *alias* for the argument.
- Changing the parameter's value changes the argument's value.

```
// C++
void swap (int& a, int& b) {
  int t = a; a = b; b = t;
}
```

```
-- Ada
procedure swap (a, b: in out integer)
is t: integer;
begin
   t:= a; a:= b; b:= t;
end swap;
```

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Smalltalk and Lisp *implicitly* provide call-by-reference, because "variables" are actually pointers to dynamic objects.

Java is complicated...

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x(0x1000)

y (0x1004)

Caller's State information

#### When *swap()* is called

// C++ swap(x, y);

- An activation record for *swap()* containing space for *a* and *b* is pushed onto the run-time stack.
- The addresses of the arguments are stored into their parameters.
- Control is transferred to *swap()* which executes, automatically dereferencing accesses to *a* and *b*.
- The RTS is popped, control returns to the caller, and the original values of *x* and *y* have been overwritten with new values.

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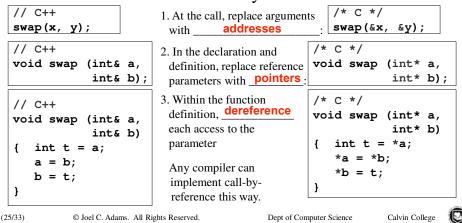
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#### Implementing Call-by-Reference?

Stroustrup's first C++ "compiler" just produced C code, so if C only provides the call-by-value mechanism, how can it handle the C++ call-by-reference mechanism?



## Call-by-Copy-Restore Parameters

```
... store _
                     both the value and address of their arguments

    Within the subprogram, parameter accesses

                                                       use the local value
   - When the subprogram terminates, the local value is
     into the corresponding argument.
   – More time-efficient then call-by-reference for heavily-used
     parameters (avoids slow pointer-dereferencing).
   - Ada's <u>in-out</u> parameters may use copy-restore...
 procedure get (str: in out ubString; length in out integer) is
    ch: character;
 begin
    length:= 0; str:= ""; get(ch);
    while not End_Of_Line loop
       str:= str + ch;
       length:= length + 1;
       get (ch);
 end get;
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```

#### When *get()* is called

-- Ada
get(st, n);

- An activation record for get()
   containing space for the data and address of both str and length is pushed onto the run-time stack.
- Argument values and addresses are written to their parameters.
- Control is transferred to get() which executes, accessing only local values str and length.
- The original values of arguments *st* and *n* are overwritten with the values of parameters *str* and *length*, the RTS is popped, and control returns to the caller.

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'Hi"

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st (0x1000)

n(0x1004)

str address

length address length value

Caller state

information

str value



### Aliasing

Copy-restore parameters behave the same as reference parameters, so long as the parameter is not an <u>alias</u> for a non-local that is accessed within the same subprogram.

Example: procedur

Suppose we have this subprogram: end get;

procedure aliasExample (param: in out integer) is
begin
 param:= 1;
 a:= 2;
 and we execute:

a = 0;
aliasExample(a);
put(a);

What is output, if *param* uses:

- call-by-reference?
- call-by-value-restore?

To avoid this, Ada <u>forbids aliasing</u>

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#### Call-by-Name Parameters

- 1. Copy the body of the subprogram;
- 2. In the copy, *substitute the arguments for the parameters*;
- 3. Substitute the resulting copy for the call;

The result is the *call-by-name* mechanism (aka <u>macro-substitution</u>

```
#define SWAP (a, b) { int t = a; a = b; b = t; }

// C++
inline void swap (int& a, int& b) { int t = a; a = b; b = t; }
```

- Call-by-name originated with *Algol-60*.
- By replacing the function-call with the altered body, call-by-name:
  - o <u>improves time-efficiency</u> by eliminating the call and the RTS overhead; but
  - o <u>decreases space-efficiency</u> by increasing the size of the program.

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#### At each call to *swap()*

```
// C++ call to swap()
swap(w, x);
```

// C++ call to swap()
swap(y, z);

• The compiler makes a *copy* of the body of the function.

```
{ int t = a; a = b; b = t; }
```

{ int t = a; a = b; b = t; }

• In it, the compiler substitutes arguments for parameters.

{ int t = w; w = x; x = t; } { int t = y; y = z; z = t; }

• The compiler *substitutes the resulting body for the call*.

```
// C++ call to swap()
{ int t = w; w = x; x = t; }

// C++ call to swap()
{ int t = y; y = z; z = t; }
```

The resulting code is <u>larger</u>, but without the overhead of pushing a stack-frame, setting parameters, ... it runs <u>faster</u>.

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#### **Macro-Substitution Anomaly** Suppose we have defined this C macro: #define SWAP (a, b) { int t = a; a = b; b = t; } *a* 11 22 33 44 55 a and i are as follows: $i \mid 2$ and we call: SWAP(i, a[i]); $a \mid 11 \mid 22$ 44 55 What we expect is: but what we get is: bus error: core dumped What happened? Our call: SWAP(i, a[i]); $\{int \ t = i; \ i = a[i]; \ a[i] = t; \ \}$ is replaced by: $a[i] \rightarrow \underline{\quad 33 \quad} \rightarrow \text{bus error}$ Tracing, we see: Because of such unexpected results, the use of macrosubstitution (#define) for call-by-name is discouraged.

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```
What About inline?
Suppose we have defined this C++ inline function:
 inline void swap (int& a, int& b) { int t = a; a = b; b = t; }
                                         a 11 22 33 44 55
                                 i \mid 2
  a and i are as follows:
  and we call:
                                 swap(i, a[i]);
                                         a 11 22 2
                                 i 33
                                                         55
 What we expect is:
   and we get:
 What happened? Our call:
                                 swap(i, a[i]);
  is replaced by:
                           {int* t1 = &i; int* t2 = &a[i];
                            int t = *t1; *t1 = *t2; *t2 = t;
 Since a[i] has a reference parameter, its address is computed
  and stored (in t2), and _____
                                   changes to i do not affect t2
 Call-by-name (via inline) is __safe_ in C++.
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```

#### **Summary**

There are two broad categories of subprograms:

- <u>procedures</u>: that map:  $(P_1 \times P_2 \times ... \times P_n) \rightarrow \underline{\text{null}}$
- <u>functions</u>: that map:  $(P_1 \times P_2 \times ... \times P_n) \rightarrow \mathbb{R}$  not equal to null

When a subprogram is *called*, an <u>activation record</u> containing space for its variables is pushed onto the <u>runtime stack</u>.

The four parameter-passing mechanisms are: Call-by-\_\_\_\_

- <u>value</u> stores a copy of the argument.
- <u>reference</u> stores the address (reference) of the argument and auto-dereferences all accesses to the parameter.
- <u>copy-restore</u> stores a copy and the address of the argument, and replaces the argument's value with the copy's value on termination.
- <u>name</u> makes a copy of the function, replaces the parameter in the copy with the argument, and then replaces the call with that copy.

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