Project Report

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1 Introduction

Brief description of the problem, its significance, the main message of the paper, and briefly mention the key results.

2 Background

Contains some history about online coloring problem. Historical notes and references at the end of Chapter 5 can be helpful for this, but you should go beyond what's just written there.

3 New Algorithm

This is where you describe your algorithm that you propose that is different from FirstFit and CBIP. You will evaluate this algorithm alongside FirstFit and CBIP.

The Algorithm that we have implemented for this project isn't a greedy based algorithm, thus it is different from FirstFit. The algorithm's computation procedure is similar to the CBIP algorithm except that at the end it uses **randomization**.

The Psuedocode for the is Algorithm is presented below.

```
1: procedure MYALGORITHM(G, \sigma)
2:
       Initialize List L.
       Compute C_v - connected component of v
3:
       Compute bipartition of C_v = S_v \cup S_v
4:
          v \in S_v \text{ and } N(v) \subseteq \overline{S_v}
       L= colors not in \widetilde{S_v} but present in S_v
6:
       Let i be a color Randomly selected out
7:
   of L.
8:
       Color v with i
9: end procedure
```

The Breadth First Search Algorithm is used to separate all the vertices that are in the S_v and $\widetilde{S_v}$. A set of all the vertices/colors that are not in $\widetilde{S_v}$ but are in S_v is created. A color is selected from the set and assigned to the vertex.

In CBIP, we select color with the minimum color value from the set. But in our algorithm, the color is selected randomly from the set.

4 Implementation Details

The implementation details of the code can be broken down into the following sections.

Graph Representation:

The graphs that can be successfully read by the program, should be in the same format as mentioned in the project.pdf (i.e MMC format). The code uses and adjacency matrix of boolean type to read the graphs that are inputted. The cells in the matrix are set to true if an edge exists between the nodes. The use of an adjacency matrix helps making sure that the graphs that are being read are automatically converted to Bipartite Graphs (i.e Duplicating method). A disadvantage of this method is that a lot of memory is wasted and this method may not be optimal for larger graphs or for machines with low memory.

Important Methods and Variables:

ReadNetworkRepoGraphs(): Reads all the graphs downloaded from the Network Repository website. The extension of the files are "NetworkRepoGraph1.txt", "NetworkRepoGraph2.txt"... You can change the number of graphs to read to check the result by running the inner loop once instead of 5 times. If it is changed to 1, then it will read only "NetworkRepoGraph1.txt" and you can check the results of 1 graph with the lowest number of nodes more carefully.

ReadRandomGraphs(): Reads all the graphs downloaded from the Random Graphs created by the class "RandomGraphs.java". The extension of the files are "RandomGraph1.txt", "RandomGraph2.txt"... You can change the number of graphs to read to check the result by running the inner loop once instead of 5 times. If it is changed to 1, then it will read only "NetworkRepoGraph1.txt" and you can check the results of 1 graph with the lowest number of nodes more carefully.

createGraph():In the class "RandomGraphs.java", the createGraph() method, has an array with different integer values (number of nodes). An adjacency matrix is created and as we iterate through the

2D-boolean array. Initailly all values are False(no edge exist between nodes) by default. There is an in-built Java random function that produces integer values in the interval [1,11]. While being on a cell if the randomizer spits out an even number, the cell value is turned True (edge exists). Thus, $P(edge) = \frac{2}{5}$ and $P(edge) = \frac{3}{5}$.

RandomOrderInput(): It fills up an array with all integer values in the interval [1,numberOfVertices], and then all the values in the array are randomly shuffled using the Java randomizer.

Data(): Prints the average of the number of colors used by each algorithm for each graph by using respectively. A graphical representation of this data is shown in the Result section of this report.

Iterations: This global variable can be changed, depending upon how many times the user want to run all 3 algorithms for all the inputted graphs and see what the averaged out values of the number of colors used by all algorithms for all the graphs will be. We ran 100 iterations and the average values computed are in a table in the result section of this report.

Challenges:

The most challenging part of this project was the coding of CBIP algorithm. The algorithm took some time to understand properly, but thanks to the Professor Pankratov and his Teaching Assistant(Ali Mohammed) we were able to grasp the concept. Coding the Breadth-First-Search(BFS) and keeping alternating depth level vertices in different sets was the most challenging, algorithmically speaking.

Some other challenges we faced in this program were due to extensive use of arrays in our program, we had to be really careful as most of the errors came from ArrayIndexOutOfBoundsException because array indices start from 0 while the vertices in the graphs start from 1.

Initially the code was tested with small graphs containing 5 to 10 nodes, as computing solutions of these graphs by hand was feasible to compare with the answers computed by the code. These small graphs were created to try and get the most number of colors from the FirstFit and CBIP algorithms (Adversarial Input). These graphs are also submitted with code.

We cannot be completely sure that this program is bug free. The input graph formats and graph naming conventions have to be correct, for the code to function as intended. We may have missed some edge cases. But because of extensive testing we are confident that the algorithmic executions are correct.

5 Experimental Details

This program was coded in Java. The version of Java used was Java version 14.

The system where this code was written used the Windows operating system, had 16 Gigabytes of RAM and with an i5 processing chip.

The code was written in the Eclipse IDE.

The Network Repository Graphs used:

Network Repository Graphs				
Graph Name	File Name	Nodes	Edges	
$dwt_{-}66^{[1]}$	NetworkRepoGraph1.txt	66	193	
GD06_theory ^[2]	NetworkRepoGraph2.txt	101	190	
$can_{-}144^{[3]}$	NetworkRepoGraph3.txt	144	720	
cat_ears_3_1 ^[4]	NetworkRepoGraph4.txt	204	542	
$ash219^{[5]}$	NetworkRepoGraph5.txt	219	438	

The Random Graphs used:

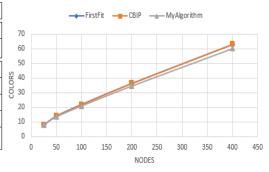
Random Graphs				
Graph Name	File Name	Nodes	Edges	
RandomGraph1	RandomGraph1.txt	25	137	
RandomGraph2	RandomGraph2.txt	50	603	
RandomGraph3	RandomGraph3.txt	100	2,307	
RandomGraph4	RandomGraph4.txt	200	8,989	
RandomGraph5	RandomGraph5.txt	400	36,317	

6 Results

This section of the report is divided into 2 sections: Network Graph Data and Random Graph Data.

Random Graph Data: Selected Random Graphs and their details are mentions in the previous section of this report. The following table and graph represent the data that was collected. These results were generated after 100 iterations on same graphs but using different random input order.

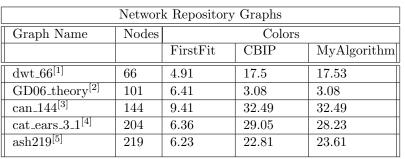
Random Graphs Graph Name Nodes Colors FirstFit CBIP MyAlgorithm 25 7.89 8.03 7.99 RandomGraph1 RandomGraph2 50 14.02 14 13.58 RandomGraph3 100 21.94 21.93 21.04 RandomGraph4 36.2534.59 200 36.41 RandomGraph5 400 62.88 63.19 60.16

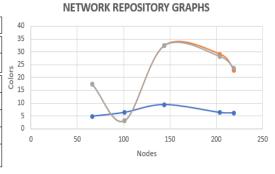


RANDOM GRAPHS

We can observe from the following data that, all three algorithms have a very similar performance. MyAlgorithm has performed a little better than FirstFit and CBIP, so can see that use of Randomness has helped. We can observe that the introduction of Randomness benifitted us. The CBIP and FirstFit have almost similar results.

Network Graph Data: Selected Network Graphs and their details are mentions in the previous section of this report. The following table and graph represent the data that was collected. Similarto the Random Graphs, the results were generated after 100 iterations on same graphs but using different random input order.





We can observe from the following data that, FirstFit usually performs better and is more stable than CBIP and MyAlgorithm. The CBIP and MyAlgorithm performance is very similar. We can observe that the introduction of Randomness hasn't benifitted us. The greedy based approach works well for the Network Repository Graphs.

We also observe that 2 major factors affect the performance of these algorithms i.e Input Order and Graph Density.

Input Order: We can easily show that with use of an adversarial input, CBIP will perform better than FirstFit, but since we use a Random input order, it seems to work towards the advantage of FirstFit.

Graph Density: Intuitively, the denser the graph (more edges between nodes), the worst FirstFit should perform. While CBIP should perform better than FirstFit, but due to a Random Input Order in our experiment FirstFit does better if not the same.

MyAlgorithm seems to perform better, if not the same as CBIP. This shows that Randomness does help, if not in all cases.

7 Future Directions

In the future we would like to use additional graph parameters such as average degree of vertices in our experimental set up. We can extend these coloring techniques to planar graph coloring problems(eg. 3D Coloring) as well. We also would like to continue and see where else we can use randomness in color selection. Initially, we wanted to implement a randomized online graph coloring algorithm proposed by Sundar Vishwanathan in "Randomized online graph coloring" [6], but due inability to get the paper we couldn't produce it.

One of the major limitations for this project is that we used a very limited sample space. We could have used larger graphs (with more number of vertices), and the creation of Random Graphs in our project had produced very dense graphs probably because the probability was set at 0.4 to an edge to be added. This caused very dense graphs to be created, we would like to test our code with sparse graphs by reducing the probability.

8 Bibliography

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