

maybe a paper could be based on finding all of these automatically

# Visual Interaction with Dimensionality Reduction: A Structured Literature Analysis

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**Abstract**— Dimensionality Reduction (DR) is a core building block in visualizing multidimensional data. For DR techniques to be useful in exploratory data analysis, they need to be adapted to human needs and domain-specific problems, ideally, interactively, and on-the-fly. Many visual analytics systems have already demonstrated the benefits of tightly integrating DR with interactive visualizations. Nevertheless, a general, structured understanding of this integration is missing. To address this, we systematically studied the visual analytics and visualization literature to investigate how analysts interact with automatic DR techniques. The results reveal seven common interaction scenarios that are amenable to interactive control such as specifying algorithmic constraints, selecting relevant features, or choosing among several DR algorithms. We investigate specific implementations of visual analysis systems integrating DR, and analyze ways that other machine learning methods have been combined with DR. Summarizing the results in a “human in the loop” process model provides a general lens for the evaluation of visual interactive DR systems. We apply the proposed model to study and classify several systems previously described in the literature, and to derive future research opportunities.

**Index Terms**—Interactive visualization, machine learning, visual analytics, dimensionality reduction

## 1 INTRODUCTION

Dimensionality Reduction (DR) is one of the major data abstraction techniques in Visual Analytics (VA). In a typical setup, data is processed by a DR algorithm, and the output is visualized and presented to the analyst (Figure 1). DR aims at representing multidimensional data in low-dimensional spaces, while preserving most of its relevant structure, such as outliers, clusters, or underlying manifolds [36]. DR is commonly applied to map data from many dimensions down to just 3 or 2, so that salient structures or patterns can be perceived while exploring data visually, for example distances between data points in a scatterplot. It is also used as preprocessing for other algorithms, to improve performance by mitigating the curse of dimensionality [15].

Faced with a plethora of existing DR methods [54], it can be difficult for analysts to choose a good one, interpret the results, and apply DR to the best advantage in a broader VA process. A common approach to overcome this challenge is to involve analysts more closely, enabling them to investigate and adapt standard methods through interactive visualizations [39]. In such situations, tight integration of algorithmic techniques and visualizations is essential. Contributing tools that support this duality is one of the major goals of VA [34]. Indeed, many VA



Fig. 1: A basic DR pipeline maps data to a DR algorithm. The results are visualized and presented to the analyst. Interaction feeds back to the pipeline components.

applications have been proposed that offer solutions for specific DR methods and analysis problems. In these examples, the goal is usually to support the analyst in steering the underlying algorithms through effective interactions in a visual interface (e.g., [6]), a concept that has become known as “semantic interaction” [18].

Despite these efforts, more general solutions that blend machine learning and VA still do not exist. Yet, it is these more general tools that are needed to deal successfully with real-world challenges [21, 48]. Aiming at a more general understanding of how to integrate algorithmic and visual components, a wide variety of theoretical VA models and frameworks have been proposed [12, 20, 34, 47, 48]. These models, however, often focus on high-level, abstract views, and fail to successfully characterize how a strong interplay between algorithms and visualizations would be realized and exploited.

To better understand the integration of DR and visual user interfaces, we formed an interdisciplinary group of VA and machine learning researchers. The motivating questions considered were “Exactly how do analysts interact with the DR pipeline?” and “How can we incorporate our findings into the interactive DR process?”. To answer these questions, we conducted a semi-automated review of 1850 papers from the visualization and VA literature. In the first step, 377 relevant papers were selected and subsequently reviewed to identify specific examples of how DR interactions are realized, and to get a comprehensive, well-grounded understanding of the overall area. We summarize our main findings in the form of seven guiding scenarios that describe ways of combining DR with visualization (to an extent, inspired by previous work on guiding scenarios for visualization evaluation [35]) (Section 4). We also present some relevant statistics about DR and interaction techniques (Section 5). To relate our work to existing theoretical models in VA, we incorporate the findings of the literature study in a conceptual process for interactive DR [47]. We illustrate how such models describe and support reasoning about dedicated systems, and enumerate five open research opportunities derived from our analysis (Section 6). Finally, we consider limitations of our work, and outline topics we plan to address in the future (Section 7 and 8).

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## 2 RELATED WORK

This study is related to previous work in several ways: it is concerned with general theoretical models of VA and their relationship to machine learning; it makes use of DR methods; it adopts basic ways of interacting with data visualizations; and it is related to the general idea of self-reflection in the visualization and VA community.

### 2.1 Theoretical Models

In the standard VA model [34], the discovery process is characterized by interaction between data, models of the data, visualizations, and the analyst. User interaction in this framework is aimed at model building and parameter refinement. Sacha et al. [48] extended it to describe the human knowledge generation process. The extended model clarifies the role of the analyst in knowledge generation, and highlights the importance of tight integration of human and machine by enabling interaction with the system. The previous models apply to VA in a generic manner. In contrast, the study presented here focuses specifically on interacting with DR methods. Another framework describes the problem of DR as a two-stage process [12]: it first maps high-dimensional data to a lower-dimensional space, then allows another stage to reduce it to 2D for visualization. While this framework generalizes specific DR methods, it focuses on a specific application to clustered data and is limited to the two-stage process as described. The framework for observation-level interaction with statistical models [20] focuses on interaction by direct manipulation of visualization by different projection techniques. Therefore, it yields a generic approach toward interacting with the output of DR methods, which is one part of our human-in-the-loop process model; i.e., observation-level interaction directly fits in our proposed process of interaction with DR methods. Another general model is semantic interaction [18], taking acquired interaction data as a means to build user models and guide the VA system.

### 2.2 Surveys of DR and Interaction Techniques

DR maps data into fewer dimensions aiming to preserve structure like cluster gaps or local manifold continuity. In linear DR output axes are linear combinations of original features, for example directions of largest variation in principal component analysis (PCA), maximally statistically independent directions in independent component analysis (ICA) [26], directions of maximal between-class and minimal within-class variation in linear discriminant analysis (LDA), or directions of maximal correlation between feature subsets in canonical correlation analysis (CCA). Nonlinear DR finds either a mapping function or only output coordinates for the data set, interpreted through proximities or distances of output data; for example, mappings are sought to preserve pairwise data distances in multidimensional scaling (MDS), small distances in Sammon mapping, distances along a neighborhood graph in Isomap, or neighborhood relationships in neighbor embedding methods [54, 55]. Some methods seek mappings onto a regular grid of units as in self-organizing maps (SOMs) or generative topographic mapping (GTM). Details on PCA, MDS, Sammon mapping, Isomap, SOM, and GTM are available in books such as [36] and for LDA and CCA in [1].

Van der Maaten et al. [54] offer a comparative review of the state of the art in DR techniques, focusing on the performance of nonlinear techniques from the machine learning perspective. Similarly, Wismüller et al. [57] survey nonlinear DR, manifold and topological learning techniques. Bengio et al. [3] give an overview on representation learning in the context of deep learning. However, all the aforementioned works do not take into account VA or user interaction. A survey by Liu et al. [39] covers visualization of high-dimensional data, including DR as one of the main techniques. They include a short discussion of interaction, and embed examples into the traditional visualization pipeline. However, they focus on general interaction techniques and not specifically how users interact with DR. Furthermore, they enumerate interactive model manipulation as a future research opportunity. Similarly, Buja et al. [9] review interaction techniques in the general setting of high-dimensional data visualization. Hoffman and Grinstein [24] and Bertini and Lalanne [4] discuss visualization methods for high-dimensional

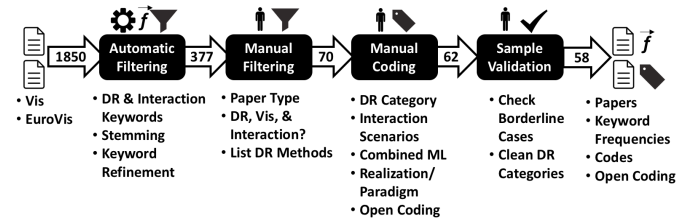


Fig. 2: Our four stage analysis process: 1. Automated filtering, 2. Manual filtering, 3. Manual coding, 4. Manual sample validation.

data mining, including projection and interaction methods. Keim [33] structures such visualization approaches according to the type of data to be visualized, the actual visualization technique, and the interaction and distortion method. However, none of these surveys performed a systematic exploration of the existing literature, nor did they focus on interaction techniques for DR.

### 2.3 Interaction Taxonomies

Our study addresses interaction in the context of DR. Therefore, related work includes general models of interaction for visualization. For example, Yi et al. [58] identify seven interaction method categories: select, explore, reconfigure, encode, abstract/elaborate, filter, and connect. Brehmer and Munzner [7] provide a comprehensive description of visualization tasks, leading to a multi-level typology of abstract tasks (which includes the ones by Yi et al.). However, model interactions only arise in tasks they call “aggregate” or “derive” tasks. Von Landesberger et al. [56] define an interaction taxonomy that is suitable for tracking and analyzing user actions in VA, and provides two types of data processing interactions: data changes, such as editing or selecting data, and processing changes, such as scheme or parameter changes. In contrast, our work focuses less on a general description of user tasks, but rather on the process of interacting with DR methods.

### 2.4 Self-Reflection in the Visualization and VA Community

Because our study is based on a systematic review, coding, and analysis of previous work in the visualization and VA community, it is also related to previous work on self-reflection of empirical studies in information visualization [35], evaluation in visualization research in general [28], or affordance in human computation and human-computer interaction [14]. While we adopt the methodology of systematic analysis of previous work, our paper has a very different focus.

## 3 METHODS

To obtain a general understanding of visual interactive DR systems, we systematically reviewed the IEEE InfoVis, IEEE VAST, TVCG, and EuroVis literature. We first automatically identified a relevant subset of papers from these conferences and journals. Then, we carried out a qualitative in-depth analysis of the relevant papers, iteratively extracting and refining visual DR interaction characteristics. Our overall approach to this analysis was inspired by *Grounded Theory* [11], in which data is systematically analyzed until meaningful categories emerge (see Section 4). This methodological approach is based on identifying and refining categories from a representative set of qualitative data, here papers, which are then used to incrementally build up a theoretical model (Section 6). This approach has been used in visualization research [28, 35, 51] and related areas such as HCI before [25], and its importance for building up the much needed theoretical foundation in visualization has been recognized [45, 51]. We next describe our method, followed by more detailed sub-sections on our analysis procedure and findings.

### 3.1 Methodological Choices

We began our endeavor with a curated list of landmark publications in interactive machine learning and visualization. Using these candidate papers, we first tried an open coding approach to identify “interesting” aspects at the intersection of VA and machine learning in general. This approach turned out to be very time consuming, and, ultimately,

impractical. While it led to a **high level framework** [47], our initial goals of thoroughly and systematically depicting how the VA and machine learning can be combined were largely unsatisfied. Hence we decided to analyze a much larger set of sample papers, resulting in three implications for our methodological choices. (1) **We realized the need to focus on a specific machine learning problem** (in our case, DR) to make the analysis more concrete, relevant, and actionable. (2) We needed automated methods to reduce the set of potentially interesting papers. (3) We opted for crisp, clear criteria for manual coding and filtering of papers. During this process, we refined the process, filtering criteria, and coding options several times. Our final workflow was then composed of four major steps, shown in Figure 2: 1.) *Automated keyword-based paper filtering*, 2.) *Manual paper filtering*, 3.) *Manual paper coding*, and 4.) *Manual sample validation*.

### 3.2 Sample Set of Papers

Our overall goal was to identify which DR methods are used, and how interaction is implemented in the VA and visualization communities. We decided to take a representative sample of papers, constituted of all IEEE VIS papers (1221) and EuroVis papers (629) from 2005 to 2015, for a total of **1850 papers**. From EuroVis we included all full and short papers, as well as EuroVA publications. The IEEE VIS papers included all InfoVis, VAST and TVCG papers. Our main focus was abstract, multi-dimensional data; consequently we did not include IEEE SciVis/Vis papers in the analysis, which generally focus on 3D spatial data (e.g., flow and volume rendering).

### 3.3 Automated Keyword-Based Filtering

We implemented a basic NLP pipeline to analyze the initial set of papers. The pipeline parses the full text of each paper, applying a tokenizer and a snowball stemmer implemented from StanfordNLP components<sup>1</sup>. The same was done with keyword lists, one list for DR and another for interaction keywords. From this, a feature vector of all keyword occurrences was derived. Papers without any keyword occurrences were deemed irrelevant and filtered out, and the remaining papers were listed in a csv file with associated keyword counts. This file was the basis for the subsequent manual filtering and coding steps.

For the keyword definition, we examined previously published surveys and taxonomy papers in related fields, and formed a set of primary papers in DR and interactive visualization. The keywords of these papers were extracted and processed using the NLP pipeline. A manual validation process then followed to refine the keyword lists. For example, ambiguous abbreviations (such as, *LLC*), or words that become ambiguous after stemming (such as *projection*, which stems to *project*, or *some*, which stems to *SOM*) were removed. The final keyword lists and statistics from the automated filtering process are provided as supplemental material.

After the automated process, the initial set of 1850 papers was filtered to 382 relevant papers based on DR keywords, then reduced to 377 papers (108 EuroVis, 247 VIS) based on interaction keywords. Figure 3 illustrates a histogram of the keyword frequencies in a logarithmic scale. DR keywords are colored green and interaction keywords are shown in light blue. *Interact* is the outlier with the maximum occurrence in interaction keywords, while *MDS* and *PCA* are the most frequently occurring DR methods.

### 3.4 Manual Expert Filtering

The remaining 377 papers were manually checked using the following criteria. First, we checked if the paper is a **visualization application or technique paper**, and if it handles “abstract data.” (We intended to exclude theory and evaluation papers, as well as papers focused on unrelated or tangential topics such as volume rendering or physical flow data). Second, we checked if the paper addresses the combination of **visualization, DR and interaction**, and if the interaction feeds back to the DR. For example Joia et al. [32] present an interesting technique for sampling and feature selection. However, there is no interaction that causes a recalculation of the DR. **Given our focus on interactive DR,**

<sup>1</sup> <http://nlp.stanford.edu/software/>

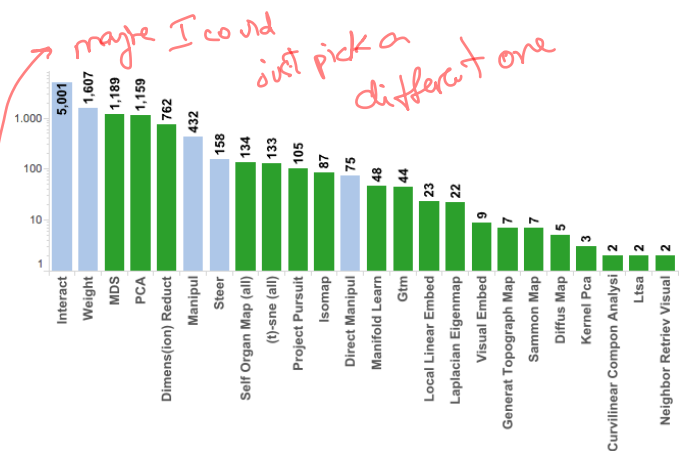


Fig. 3: The top keyword occurrences in the automatically identified papers shown in a log-scale histogram. DR keywords are colored in green and interaction keywords are colored in light blue.

we excluded interactions that do not feed back to the analysis pipeline, such as exploration/navigation/DoD (Details on Demand) interactions. Finally, we listed the DR techniques employed. Based on this, we obtained a candidate set of 70 relevant papers.

### 3.5 Manual Paper Coding

We next analyzed these 70 papers in detail, by open coding the “interesting” aspects of interaction described in each paper. For each paper, we extracted a brief description of the proposed interaction, including how interaction is performed and which parts of the DR pipeline are affected. In addition, we iteratively identified and refined a set of criteria. A **more general model** [47] and the different components of the DR pipeline (data, preprocessing, DR) served as initial set of criteria to encode which parts are affected by the analysts feedback. However, we had to adapt, split, and refine these criteria several times. As a result we arrived at seven scenarios for DR interaction, encoding “**how the DR pipeline is changed**” (see Section 4), the interaction paradigm (“how the interaction is performed”, see Section 5), the *DR Method(s) or Algorithm(s)*, and combined machine learning techniques such as *clustering or classification*. During our process we had to discard several aspects that we initially were interested in. We started, for example, to encode “who” is expected to perform the actual interaction (e.g., DR expert or novice user), and “why” the human input is needed. However, investigating these aspects turned out to be challenging as the necessary information was not provided in many cases. A more detailed description of the final criteria and options is provided in the following sections. 8 more papers were filtered out in this iteration.

### 3.6 Manual Sample Validation

In a final validation iteration, we aimed at more detailed analysis of borderline cases and ended up removing 4 more papers. Our **final corpus included 58 relevant papers, with the encoded information and the corresponding feature vector of keyword occurrences**. We “cleaned” the encoded information and grouped the identified DR methods into higher-level categories (see Section 5.2).

## 4 SEVEN GUIDING SCENARIOS FOR DR INTERACTION

We next describe the interaction scenarios that emerged from our literature review. By examining the **interactive machine learning pipeline proposed in [47]**, we identified the **main potential interactions in data analysis, and classified them into seven guiding scenarios**. This categorization is based on the outcome of several iterations of the paper filtering and open coding process, and is one of the major findings of our study. It enables us to evaluate various methods for “how the DR pipeline is controlled through interaction”. In the following, we briefly describe these seven DR interaction scenarios “along the DR pipeline” and illustrate them with examples:



filters and selections

I could apply this

**S1 Data Selection & Emphasis:** This group of interactions affects the data records (or observations) that will be supplied to the actual DR method. We found many examples in which a filter is applied to the data, and the DR pipeline is re-run on the remaining subset. In this scenario, we further identified several realizations. In some situations, analysts select subsets directly in a two-dimensional visual representation. In others, analysts specify conditions or filters through control panels. Furthermore, we identified various preprocessing configurations or parameters that can be adjusted by the analyst. An example is Jäckle et al.'s temporal MDS plot technique [29], where a parameter sets the size of a sliding window. The resulting slices are taken as input for subsequent DR by one-dimensional MDS. *S1 Data Selection & Emphasis* was identified 26 times.

**S2 Annotation & Labeling:** A second group of operations enrich data with annotations or labels on instances. In some systems, data may be enriched with additional information. For example, StarSPIRE [6] allows analysts to annotate documents with additional terms that will be included in the similarity calculation. Other systems enable the analyst to assign classification or cluster labels if the DR is combined with another form of machine learning (e.g. [23]). The cluster or classification labels, as well as data structures (such as a hierarchy obtained from hierarchical clustering) are then translated into constraints for the DR algorithm (e.g., cluster preservation).

In the classification case, the analyst provides class labels within the two-dimensional embedding to train a classifier. Labels are provided for data instances, or in some settings, for pairs of instances. The classification result influences subsequent DR (e.g., [22]). In the clustering case, the analyst defines cluster memberships, such as by grouping elements into clusters, by adding or removing elements, or by splitting or merging clusters. Resulting clusters are used by the next iteration of DR. For example, the Bubble Cluster approach [23] lets the analyst re-position points or draw cluster boundaries in a 2D projection of the data, and use the new cluster assignments to update the projection. *S2 Annotation & Labeling* was found in 15 papers.

**S3 Data Manipulation:** Some VA systems let the analyst explicitly manipulate data values by moving points in a spatialization, or by editing data in a table view. This interaction helps analysts to investigate “what if” scenarios. For example the iPCA system [30] allows the analyst to re-position a point in the 2D projection, and see how other values change. Interestingly, Jeong et al. reported that adjusting data values could be counter-intuitive to some of the subjects in their study. However, they argued that these interactions are still useful for revealing relationships in the data that might otherwise not be recognized. *S3 Data Manipulation* was only rarely used (7 times).

**S4 Feature Selection & Emphasis:** We found many interaction examples that feed back to the initial data space by adapting the metric for calculating similarities or dissimilarities between data instances. Many DR applications adopt a “default” metric such as Euclidean distance. However, the default metric may not correspond well with the analyst’s “notion” of dissimilarity, and the metric needs to be adapted to the application. One way to do this is to associate adjustable weights with each data dimension. Distances can be calculated accordingly, giving more influence to relevant dimensions. For example, iPCA [30] provides the analyst with weighting sliders for each dimension. Another possibility is to infer the dimension loadings from direct manipulation interactions of visual elements. An example can be found in [43] where the analyst rearranges points serving as control points for a subsequent optimization of the projection matrix. Similarly in Dis-Function [8], an analyst drags and selects points on a 2D scatterplot, and a compatible distance function is learned by the system. When the user is finished with manipulations, a button is pressed to learn the distance function and re-render the result. Other systems such as [44] provide analysts with drop-down menus to select a distance metric. Further options are to let the analyst determine interesting features in combination with subspace clustering (e.g., [41]) or quality metrics (e.g., [31]). *S4 Feature Selection & Emphasis* was

the most frequently implemented interaction scenario (37).

**S5 DR Parameter Tuning:** Some DR algorithms contain specific parameters that can be tuned, such as LDA regularization in [13]. An approach proposed by Schreck et al [49] allows the analyst to set the grid dimensions of a self-organizing map (number of neurons, DR structure). Some systems have parameters related to quality and accuracy, such as thresholds or level-of-detail parameters. Garg et al. [22] provide a similarity cutoff parameter that determines edges with low similarity to be removed from a graph layout. Others have parameters affecting visual appearance. For example, [16] allows adjusting node padding or forcing strength in a force-directed embedding. We also found examples where the analyst can define algorithmic variants (by setting parameters), that animate or show transitions between multiple DR results. In [43] a transition parameter (slider) is set to compare and track changes. Finally, parameter sets or configurations can be set indirectly, such as when the analyst is offered several visualization recommendations or previously defined parameter sets, and may compare them to select the most appropriate one. However, we did not identify any mature, ready-to-use system incorporating this kind of parameter tuning. *S5 DR Parameter Tuning* was found in 20 papers.

**S6 Defining Constraints:** Interactions can be translated directly to DR algorithm constraints. We identified several examples in which an analyst directly arranges points in the visualization. These modified points are interpreted as anchor points in the subsequent DR iteration, in which their positions should remain fixed to help the analyst track other changes. For example, Endert et al. [20] introduced Guided MDS, where user-defined anchor points are used to fix positions and adjust similarities for maintaining consistency in visualization. A similar example can be found in [6], where nodes representing objects are marked as “fixed” and subsequently not rearranged by a force-directed algorithm. Constraints such as region or containment, as well as visual constraints have also been proposed. For example the technique introduced by [17] allows analysts to group points and define regions that should not be split or overlap with others. In addition, constraints for the edges may be defined, such as pointing edge downward. Note, that in combination with another ML method, the ML output can be thought of as a constraint for DR, e.g., items that belong to the same cluster or classification should be placed close to each other, or a hierarchy obtained from hierarchical clustering should be preserved. In some systems, these constraints can also be interactively controlled (providing labels, setting parameters for the clustering, etc.). *S6 Defining Constraints* was described in 15 papers.

**S7 DR Type Selection:** Visual embeddings of high-dimensional data can be generated by various DR algorithms and vary in terms of layout and quality. For example, linear methods project data to new axes, such as directions of maximal variance in PCA, whereas methods such as MDS aim to preserve distances or neighborhoods of data records. While some systems, such as iPCA and StarSPIRE, focus on one DR technique, others implement multiple algorithms so the analyst can select and compare their results while analyzing data. A system by Rieck and Leitte [46] visualizes and ranks embeddings from several DR algorithms according to quality measures. Another system by Liu et al. [40] lets the analyst select DR algorithms and compare them based on visualization of distortion measures. We can even envision approaches for indirect *S7 DR Type Selection*. Although we did not find examples, it seems potentially useful to infer an appropriate DR Type from user inputs automatically, on the fly. We elaborate on this idea in Section 6. *S7 DR Type Selection* had the lowest occurrence (4) among the seven scenarios.

Note that some of the seven guiding scenarios overlap. For example, S1-S3 affect data items, and S5-S7 involve the choice of DR algorithm. However, we identified these particular scenarios as useful descriptions of the papers we studied. We found it useful to distinguish scenarios based on the way interaction affects the DR pipeline. For example, to

clustering

I think this is what we want

x

Table 1: Result of the proposed coding process. Blue, orange, yellow and green setups appear more frequently. Red points denote papers implementing 4 different interaction scenarios. The three main column groups specify interaction scenarios, combinations with other machine learning methods, and interaction paradigms.

Num	Name	S1	S2	S3	S4	S5	S6	S7	Clust	Class	Dir-Man.	Contr	CLI	Other	NA
1	garg_vast_08														
2	yuan_infovis_09														
3	bremm_eurovis_11														
4	brown_vast_12														
5	boukhelifa_eurovis_13														
6	yu_eurovis_13														
7	hu_vast_13														
8	liu_eurovis_15														
9	kim_vis_2015														
10	wang_vast_06														
11	brandes_vast_07														
12	vanham_infovis_09														
13	jianu_vis_09														
14	ward_eurovis_11														
15	yuan_vis_10														
16	correll_eurovis_11														
17	turkay_infovis_11														
18	yuan_infovis_13														
19	jaeckle_vis_15														
20	janoos_vast_07														
21	nam_vast_07														
22	peltonen_eurovis_13														
23	gleicher_vast_13														
24	ingram_vast_10														
25	engel_eurovis_11														
26	johansson_infovis_09														
27	paulovich_eurovis_11														
28	drieger_eurovis_12														
29	portesdos_vast_12														
30	joeng_eurovis_09														
31	viau_infovis_10														
32	gou_infovis_09														
33	choo_vast_10														
34	joia_infovis_11														
35	endert_vast_11														
36	cao_infovis_11														
37	paiva_infovis_11														
38	garg_vast_10														
39	cheng_vis_15														
40	mao_infovis_07														
41	riek_eurovis_15														
42	schreck_vast_08														
43	crnovrsanin_vast_09														
44	nam_vis_12														
45	bradel_vast_14														
46	kidwell_infovis_08														
47	vonlandesberger_vast_09														
48	mamani_eurovis_13														
49	poco_eurovis_12														
50	paulovich_infovis_08														
51	dywer_infovis_08														
52	chen_infovis_09														
53	choo_vast_13														
54	liu_eurovis_14														
55	molchanov_eurovis_14														
56	dywer_infovis_06														
57	heine_eurovis_07														
58	ferdosi_vast_10														
SUM		26	15	7	37	20	15	4	28	12	36	33	2	1	12

distinguish *S2 Annotation & Labeling* from *S6 Defining Constraints* interactions, we note that both add information to data items (e.g., a class label vs. a “pinned” information), but *S2 Annotation & Labeling* focuses on information about input data items, while *S6 Defining Constraints* involves information about desired results or outputs of the DR. Note also that the role of the VA system is to translate these similar inputs to different interaction scenarios (see Section 5).

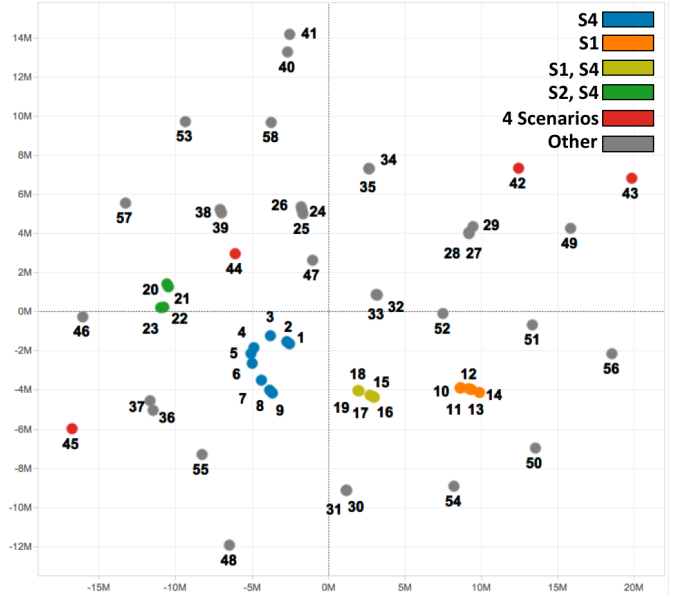


Fig. 4: Embedding of 58 papers based on interaction scenarios. The plot shows a diverse set of interaction combinations. The main interaction scenarios are *S4 Feature Selection & Emphasis* (blue cluster), *S1 Data Selection & Emphasis* (orange cluster), the combination of *S1 & S4* (yellow cluster), and *S4 combined with S2 Data Manipulation* (green cluster). The red cluster contains papers that combine 4 different interaction scenarios.

**Observations:** The final result of our coding process is shown in Table 1 and Figure 4. To provide an overview of the coded results, we created a 2D projection of the papers using *Multiscale Jensen-Shannon Embedding* [37], which aims to place papers with similar codes nearby in the projection. Together with Table 1 we can investigate combinations of interaction scenarios. In total, we identified 29 different combinations. We found a maximum of 4 scenarios per paper (in 4 papers, colored in red). Papers colored blue only cover *S4 Feature Selection & Emphasis*. This was the most frequent “setup” and appeared in 9 papers. The five orange dots denote papers that only include *S1 Data Selection & Emphasis*, and the five yellow dots represent papers with combinations of *S1* and *S4*. Work applying *S2 Annotation & Labeling* and *S4 Feature Selection & Emphasis* occurred 4 times (green dots). We color the rest of the papers gray, as their combinations of interactions occur less frequently. These gray dots generally appear further away from the center of the view. For example, papers including *S5 DR Parameter Tuning* are placed in the upper area, or *S2. Annotation & Labeling* papers are placed near the upper left corner.

We further observe from Table 1 that some interaction scenarios appear more frequently than others. This applies to *S4*, *S1*, and *S5* maybe because they are more general or convenient than others. *S3 Data Manipulation* is used least. One reason might be that manipulating observations—often considered “ground truth”—is not common practice in many domains (e.g., machine learning). Also note that *S3* only appears in combination with other interaction scenarios.

In this respect, it would be interesting to investigate in more detail why some interaction scenarios appear more or less frequently. This naturally raises the question about the *effectiveness* of certain interaction scenarios. In-depth investigation of effectiveness, however, goes beyond the scope of this paper. Previous work has shown that assessing effectiveness of interactive DR solutions depends heavily on context factors, such as users, data, domain, and tasks at hand [50, 52]. A generic comparison of the scenarios’ usefulness and effectiveness is thus a non-trivial endeavor, and further work is needed. The study in this paper is descriptive with the goal to characterize existing interaction scenarios, and can be used as a starting point for such endeavors.

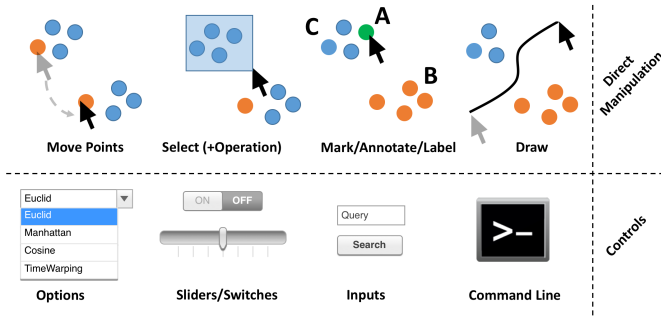


Fig. 5: Different interaction paradigms: Typical *Direct Manipulation* interactions are shown in the upper half. On the bottom, control elements are shown. DR-Interfaces are usually composed of both.

## 5 FURTHER INSIGHTS

In this section, we analyze the interaction scenarios in different contexts, such as the interaction paradigm, the combined DR algorithms or other machine learning methods, as well as a temporal perspective.

### 5.1 Interaction Paradigm & Usability

Each interaction scenario can be realized in multiple ways. Therefore, our analysis also encoded interaction paradigms, including *Direct Manipulation* of visual elements, *Controls* (sliders, buttons, etc.), *Command Line Interface (CLI)*, *Other* (such as gestures or speech input), or *NA* (if interaction was not described in the paper). The results (see Table 1-right side columns) reveal balanced usage of *Direct Manipulation* (36) and *Controls* (33). However, novel interaction paradigms (*Other*) only appeared once (multi-touch in [59]) and another set of papers omits details of how interaction is performed (*NA*, 12). It is also worth mentioning that the amount of provided information about the realization and implementation, as well as discussions about usability of interactions strongly varies between the analyzed papers.

Our results show that analysts interact with DR either directly in the visualization, or using control elements. During our study we noticed, especially in *Direct Manipulation*, similar actions may have different meanings or implementations (see upper half of Figure 5 as an example). An analyst can move points, select data records (followed by an operation such as deletion), mark (label, or annotate) points, or draw borders in a plot. However, the meaning of an action may vary. Data movement can be “translated” to *S2 Annotation & Labeling* if a point is moved outside a cluster, or to *S3 Data Manipulation* if the data value is changed. Alternatively, the movement can be “translated” to *S4 Feature Selection & Emphasis* by deriving (dis)similarities from user defined distances between data points, or *S6 Defining Constraints* if a data point being moved is interpreted as an anchor point. In such cases visualization has to act as a “mediator” between human and machine and translate the interactions to appropriate DR pipeline components. In contrast, control elements (Figure 5-bottom) are usually directly coupled to specific DR pipeline components. The UI provides, for example, sliders to directly control dimension loading or DR parameters, drop-down menus to select metrics, or buttons to trigger specific operations. There are also cases where natural language text inputs are accepted. On the other hand, *Command Line Interfaces* offer a powerful, well-specified language for programmers, but they are not always convenient or even accessible to analysts.

The final implementation determines the “complexity” of performing an interaction scenario, which depends on user and task characteristics though. DR experts, for instance, might require a large set of directly steerable parameters, and accept a more complex interface. Other users, however, might require less flexibility, but simple ways to provide feedback based on their domain knowledge.

Table 2: Identified DR techniques shown with interaction scenarios.

	Distance Based	Linear Projection	Graph/Force-Dir.	General	LP & DB	Neural Network	DB & GraphFD	LP & GraphFD	General, NN	Other	SUM
# Papers	17	12	10	5	4	3	3	2	1	1	58
Data Selection & Emphasis	9	5	6	2	1	2		1			26
Annotation/Labeling	4	5	4				2				15
Data Manipulation	2	2				2		1			7
Feature Selection & Emphasis	11	11	3	3	2	2	2	1	1	1	37
DR Parameter Tuning	5	3	3	2	1	3	1	1		1	20
Defining Constraints	5	2	4	1		1	2				15
DR Type Selection		1		2	1						4

Table 3: Temporal statistics of interaction and DR Techniques.

	2006	2007	2008	2009	2010	2011	2012	2013	2014	2015
#Papers	1	5	5	9	6	10	5	8	3	5
Data Selection & Emphasis	1	1	4	6	2	4	3	1	2	1
Annotation/Labeling		3	2	1	1	2	1	3	1	1
Data Manipulation			1	3	1		1	1		
Feature Selection & Emphasis		2	2	4	5	8	2	7	2	4
DR Parameter Tuning		1	1	4	4	4	3	1		2
Defining Constraints			2	1		5	3	1	2	
DR Type Selection		1					1		1	1
SUM Interaction Types	1	8	12	19	13	23	14	14	8	9
AVG Interactions/Paper	1	1,6	2,4	2,11	2,17	2,3	2,8	1,75	2,67	1,8

### 5.2 DR & Machine Learning Algorithms

The interaction scenarios appeared with several different DR algorithms. Each algorithm was assigned to a higher-level category of *Distance Based (DB)*, *Linear Projection (LP)*, *Graph/Force-Directed (FD)*, *Neural Network (NN)*, *General*, or *Other* (one approach did not match any others – “data driven feature selection”). Table 2 lists these DR algorithms as columns and interaction scenarios as rows. We see that *Distance Based* methods (mainly MDS) were used alone most frequently (17), followed by *Linear Projections* (mainly PCA) alone (12) and *Graph/Force-Directed* methods alone (10). *General* approaches appear in 5 papers, whereas *Neural Networks* were used 3 times (all self organizing maps). The other columns show examples where various DR algorithms are used in combination. Note that only one of the mixed approaches (other than *General* approaches) lets the analyst switch between DR algorithms. Interestingly, *S4 Feature Selection & Emphasis* was used in all of these DR algorithm combinations. We can further derive from Table 1 that *Clustering* and *Classification* appeared in 31 papers. *Clustering* was used 28 and *Classification* 12 times, while in 9 papers both of them are used in combination.

### 5.3 Temporal Perspective

We did not find any relevant papers on interactive DR in 2005. As shown in Table 3, in the corpus we studied, published work on visual interactive DR first appeared in 2006, with one paper that reported work in *S1 Data Selection & Emphasis*. This was followed by 5 related papers published in 2007, where a wider range of interaction techniques such as *S4 Feature Selection & Emphasis*, *S2 Annotation & Labeling*, and *S5 DR Parameter Tuning* were included. These four interaction scenarios appear to be more “established” than the others, as work was continuously reported in these areas in the following years, whereas the development of other interaction techniques have breaks in between. For example *S7 DR Type Selection* first appeared in 2007, but then there is a gap until 2012, after which it appears consistently. We admit these trends may not be fully representative due to the limited number of papers and scenarios in our study. One obvious pattern is the number of papers published by year. Years 2009 (9) and 2011 (10) are peaks. Of course, a larger number of papers does not necessarily describe a richer set of interaction scenarios (as shown in the “AVG Interaction/Paper” row where large paper counts do not strongly correspond to large average interaction counts).





## 6 THE INTERACTIVE DR PROCESS

In many VA tools, the analyst has not only the ability to visually inspect and validate the data, but also the ability to provide interactive feedback to control the analysis through the interface. As discussed previously, this feedback is usually in the form of controls and direct manipulation interactions, such as setting positions, selecting, or grouping data items; other interaction paradigms such as command line scripts, gestures and speech input are also possible. The VA system maps user inputs to the specified interaction scenario(s), providing an instance of a typical continuous and iterative process, as it is usually targeted in VA [34, 47]. Note that the ability of the analyst to provide useful feedback depends on the interpretability of visual observations but also

StarSPIRE (S1, S2, S4, S6) [Bradel et al. \[6\]](#) extends the ForceSPIRE system proposed by Endert et al. [19]. Their extension offers a richer set of interaction scenarios. A modified force-directed layout

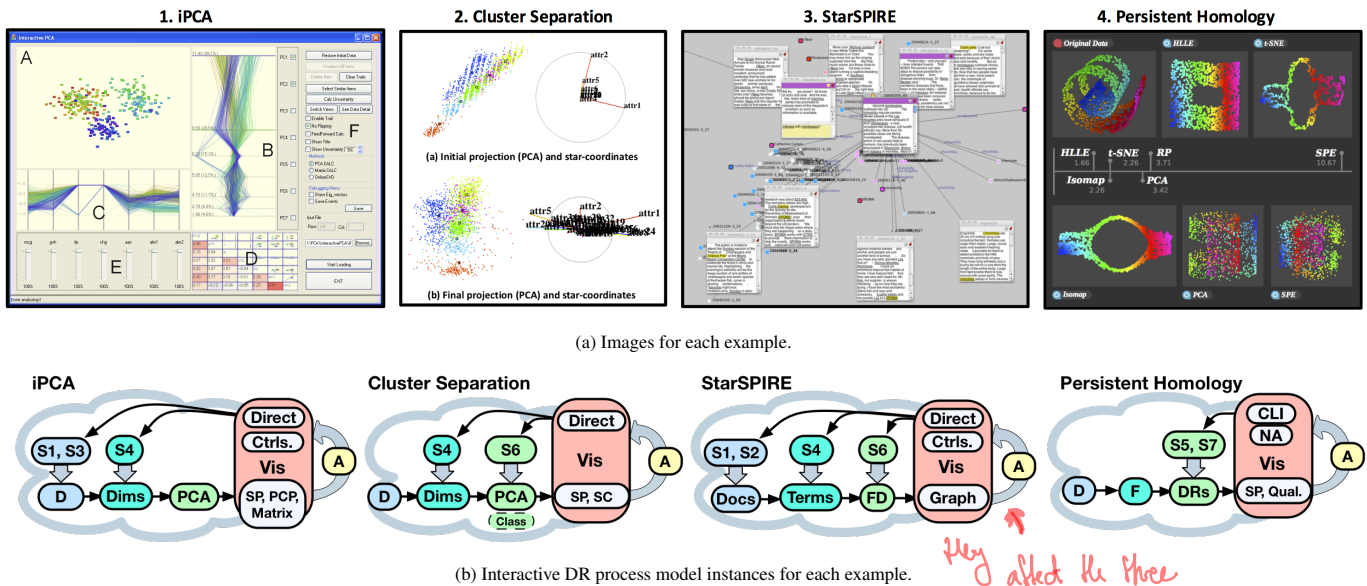


Fig. 7: Analyzed examples for DR interaction: 1.) iPCA, 2.) Interactive cluster separation, 3.) StarSPIRE, and 4.) Persistent Homology.

algorithm visualizes text documents under a computed similarity metric (Figure 7a-3). They extend ForceSPIRE with an additional model for relevance-based document retrieval that performs *S1 Data Selection & Emphasis* inferred from user interactions. The analyst can also *S2 Annotate* text documents with further information (terms) that update the similarity calculation and cause a change to the document layout. *S4 Feature Selection & Emphasis* is inferred from user interaction by adjusting the weightings of document terms. This is done in conjunction with annotation, but also by re-sizing elements, searching, highlighting and overlapping documents. In addition it is possible to rearrange and pin document nodes in the spatialization. The pinned document serves as a *S6 Defined Constraint* for the force-directed layout.

**Persistent Homology (S5, S7)** Rieck and Leitte [46] describe an approach to comparing DR parameter settings across various DR types, such as PCA, t-SNE, HLLE and Isomap. Quality measures are computed to validate and rank the DR setup configurations. The proposed approach visualizes various DR embeddings together with additional quality information (Figure 7a-4). Their study does not explain in detail how an analyst would create the different combinations of *S5 Parameter Settings* and *S7 DR Type Selections* (we encoded this work as NA). However, several examples illustrate different DR algorithms and parameterizations created by the authors (we assume using CLI).

**Comparison** Figure 7b shows interactions supported by the above-mentioned systems. For instance, while iPCA offers the ability to *S3 manipulate* data items, StarSPIRE allows the analyst to *S2 annotate* documents with additional terms. iPCA, Cluster Separation, and StarSPIRE allow *S4 Feature Selection & Emphasis*, however, in different ways. iPCA offers slider controls directly coupled to dimension loading. Cluster Separation and StarSPIRE infer *S4 Feature Selection & Emphasis* from direct manipulation, through optimization and term weighting. Cluster Separation and StarSPIRE allow the analyst to *S6 Define Constraints* for the DR process, by positioning and pinning data items. The Persistent Homology approach focuses on the validation and comparison of different DR setups by choosing among several *S7 DR Type Selections* and *S5 Parameter Settings*.

The examples and their comparison illustrate the applicability of the proposed interactive DR process model. It supports evaluating systems with respect to the identified interaction scenarios and their implementations, and can be used to derive further interaction scenarios and implementations not present in current VA systems. We next detail **5 opportunities for research in visual interactive DR systems**.

## 6.2 Generative Use of the Process Model – Opportunities

We can apply our study and process model to better understand and reason about research opportunities. We recommend these directions:

**Semantic Interaction Design** One challenge in the design of interactive DR systems is the semantic translation of front-end interactions. Section 5.1 illustrates that the same front-end interaction can be mapped to several different back-end computations. Ideally, intuitive interactions would direct back-end computation and correctly express the intention of the analyst. For example in StarSPIRE, by moving points closer to each other in the visualization the analyst can have the similarity measures and the layout updated accordingly. While many systems provide good examples of semantic interaction design, the translation only applies to a subset of interaction scenarios (e.g., feature weighting, similarity computation). Consistently mapping user inputs to more complex actions covering the entire pipeline is an open challenge. Especially in DR, interaction designers have to consider that DR concepts and algorithms are often hard to understand and interpret. Therefore, interaction needs to be accessible and interpretable for end users, enabling them to work with distances and neighborhoods, clusters and class memberships, or importance of dimensions. Scalability of computation will play a crucial role in such interactive systems, as delaying responses hinders usability [10].

**Guidance on DR Type Selection** Our study revealed that *S7 DR Type Selection* has rarely been implemented. Furthermore, semantic interactions derived from direct manipulation interactions are mostly limited to DR pipeline adaptations of the feature space or DR parameters and constraints. We envision future systems that can also infer an appropriate DR algorithm from user inputs. Such VA systems would probably need to implement, calculate and compare various DR types, to identify the “best” results on the fly. Work proposed by Rieck and Leitte [46] shows a promising step in this direction. However, realization and implementation of direct manipulation interactions and translation to DR type selections is still missing. Such techniques, that balance user flexibility with system automation, have great potential for guiding users through complex data analyses, so this is an important area for further investigation. On the algorithmic side, the challenge is to formulate specific DR algorithms as parametric instances that allow smooth transitions between different DR types. For example, continuous model spaces [37, 55] enable analysts to track and interpret model switching and avoid abrupt and confusing transitions.

**Evaluating DR Interactions** As pointed out in Section 4 we are not aware of studies evaluating the effectiveness of DR interactions in a structured and general setup. It will be a challenge to design and

→ 2017 opportunities

Connecting both could be a record.



conduct a fair comparative assessment of different interaction scenarios, as they depend on many factors, such as implementation, user experience or tasks. However, it would be useful to gather insights about effectiveness of the respective interaction scenarios under certain conditions. This would guide researchers and developers in designing interactive DR systems for their specific domains, tasks and data. Hornbæk provides a comprehensive overview of usability measures from HCI [25] that could be applied to a comparative DR setup.

**Fully Integrated Process** As discussed in Section 4 and illustrated in Figure 7b, existing systems implement only a small subset of possible interactions. While many previous systems have proven useful for specific tasks and problems, more powerful, general-purpose interactive DR tools are needed. An ideal system would provide flexible access to a range of DR algorithms, distance functions, optimization algorithms or quality metrics, and offer many of the interaction types we identified. It will be a challenge to conceptually integrate and steer a wide range of algorithm specific parameters or different combinations of computations. At the same time, the burden of choosing suitable data, features, parameters and models could be mitigated by tightly integrating the DR pipeline with interactive visualization.

**Analytic Provenance** Given the complex nature of many analysis tasks, the analyst often has to go through many steps and even false starts before reaching sound conclusions. Although analytic provenance has been introduced as a research topic in VA, not much work has been reported on recording interactions to support exploratory data analysis for DR. A major task will be to compare and assess different DR results in a sequence of interactions. For example, when switching between different states, the resulting changes have to be observable and measurable to automatically identify impactful actions within an analysis session. Lehmann and Theisel provide a promising approach to measure the (dis)similarity of projections [38]. However, more research considering a larger set of DR types and interactions is needed.

## 7 LIMITATIONS

Our work comes with certain limitations that result from the approach we adopted. To keep the study focused and manageable, we had to limit our literature analysis to a representative set of examples. After many discussions, we decided to focus on the visualization literature. Our goal was to identify papers that include DR, interaction and visualization. We find these mainly in the visualization community. We primarily aimed at actionable and extensible results, and with that at transparency and reproducibility by thoroughly describing our method. Nevertheless, we are confident that we analyzed a representative subset of the literature and that our derived model is stable regarding the interaction scenarios. It would be interesting to evaluate the stability of our results by performing an expanded “cross validation” study that also includes/adds papers from machine learning (e.g., KDD) and human-computer interaction (e.g., CHI). Note that we initially started our analysis with landmark publications from all domains and had to limit the set of papers to keep the work manageable.

In our analysis of the literature, we identified several contributions that offer useful interactions to explore and validate DR results, without directly feeding back to a DR calculation. We had long discussions about including these interactions as another scenario, but finally decided to exclude these papers to keep the work focused. An example is the system proposed by Stahnke et al. [53] that provides interactions to interpret and interrogate DR results. Their system allows an analyst to investigate approximation errors, examine positions of data points, and “overlay” the influence of specific data dimensions. However, these interactions do not feed back to a subsequent DR calculation.

Similarly, other facets may be involved in interactive DR in specific, and interactive machine learning in general. An important facet is DR quality measures. A framework by Bertini et al. [5] describes an enriched VA pipeline with quality-metric-driven automation. Quality is measured at each stage of the pipeline, with the analyst steering the entire process. Quality measures can augment user interaction at these stages with automatic configurations or recommendations. However, quality measures do not interact with the DR pipeline, and can be seen

as an add-on to our proposed scenarios. Considering quality measures was a main concern when we began this study, but as the work matured we decided to focus exclusively on interaction scenarios with DR.

## 8 CONCLUSION AND FUTURE WORK

Giving humans more interactive control over the DR process is a great opportunity for improving exploratory data analysis. It allows the analyst to explore data, feature, parameter and model spaces, taking advantage of their understanding of the data, application domain, and experience in the analysis task at hand.

In this study, we systematically analyzed the visualization literature with the goal of identifying common DR operations amenable to interactive control. We summarized our findings in seven guiding scenarios, which we contextualize in a conceptual process model for visual interactive DR. Our analysis revealed several ways that DR can be enriched by user interaction, how these strategies are supported by current VA systems, and points to future research directions in interactive DR. We hope that our contributions help other researchers investigating, designing and evaluating interactive DR systems.

In future work, we plan to develop a system capable of inferring and adapting its settings in a larger design space than current systems for visual interactive DR. We plan to extend our analysis to papers from related domains, such as machine learning and human-computer interaction. Beyond this, we would like to perform a literature analysis and process modeling study focused on interactive clustering, classification, and regression analysis in VA.

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