

## CSCI317 Database Performance Tuning

# Quantitative Analysis of Indexing

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# Quantitative Analysis of Indexing

## Outline

Cost model ? What is it ?

Storage organization and models

Tables with randomly ordered rows

Tables with clustered B\*-tree index

Tables with not clustered B\*-tree index

# Cost model ? What is it ?

A model used for estimation of the cost of various database operations

Notation

- $b$  => the total number of fully packed blocks
- $r$  => an average number of rows per block
- $f$  => fanout of B\*-tree index
- $k$  => number of keys in an index

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# Storage organizations and models

Tables with the randomly ordered rows

Tables with the clustered B\*-tree indices

Tables with the unclustered B\*-tree indices

# Quantitative Analysis of Indexing

## Outline

Cost model ? What is it ?

Storage organization and models

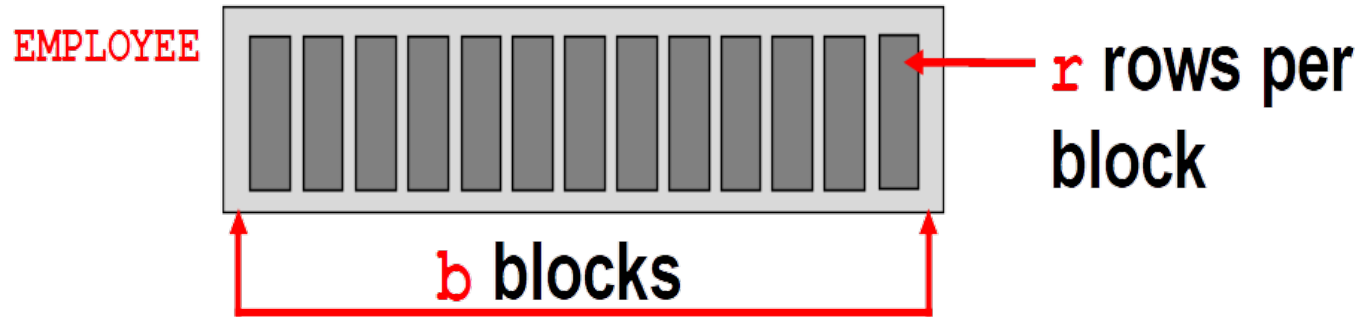
Tables with randomly ordered rows

Tables with clustered B\*-tree index

Tables with not clustered B\*-tree index

# Tables with randomly ordered rows

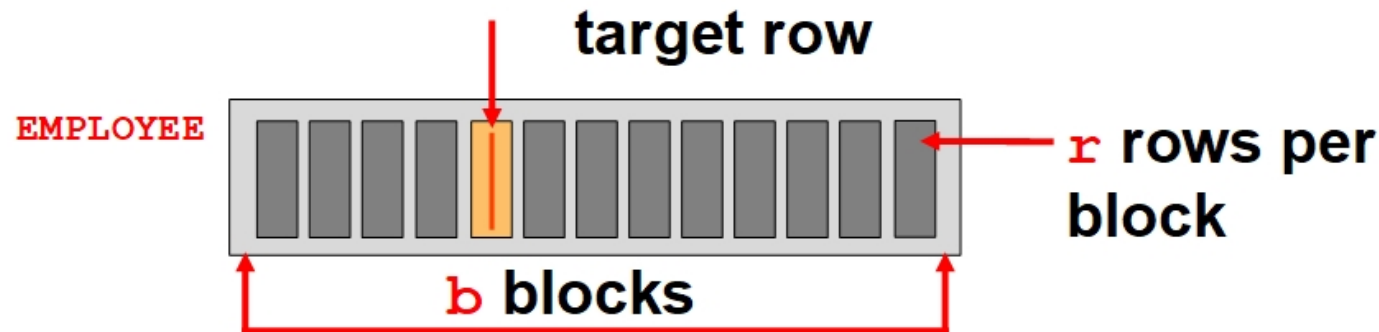
Full scan



Cost =  $b$  read block operations

# Tables with randomly ordered rows

Full scan with an equality condition on a key

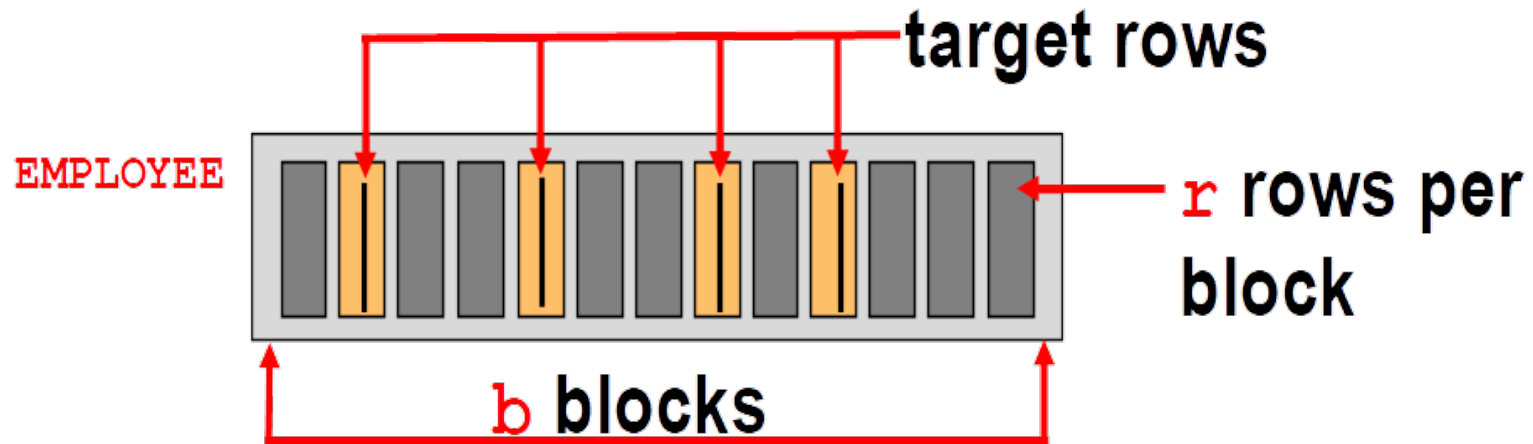


Cost =  $(1 + b) / 2$  read block operations



# Tables with randomly ordered rows

Full scan with a range condition



Cost =  $b$  read block operations

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Cost model ? What is it ?

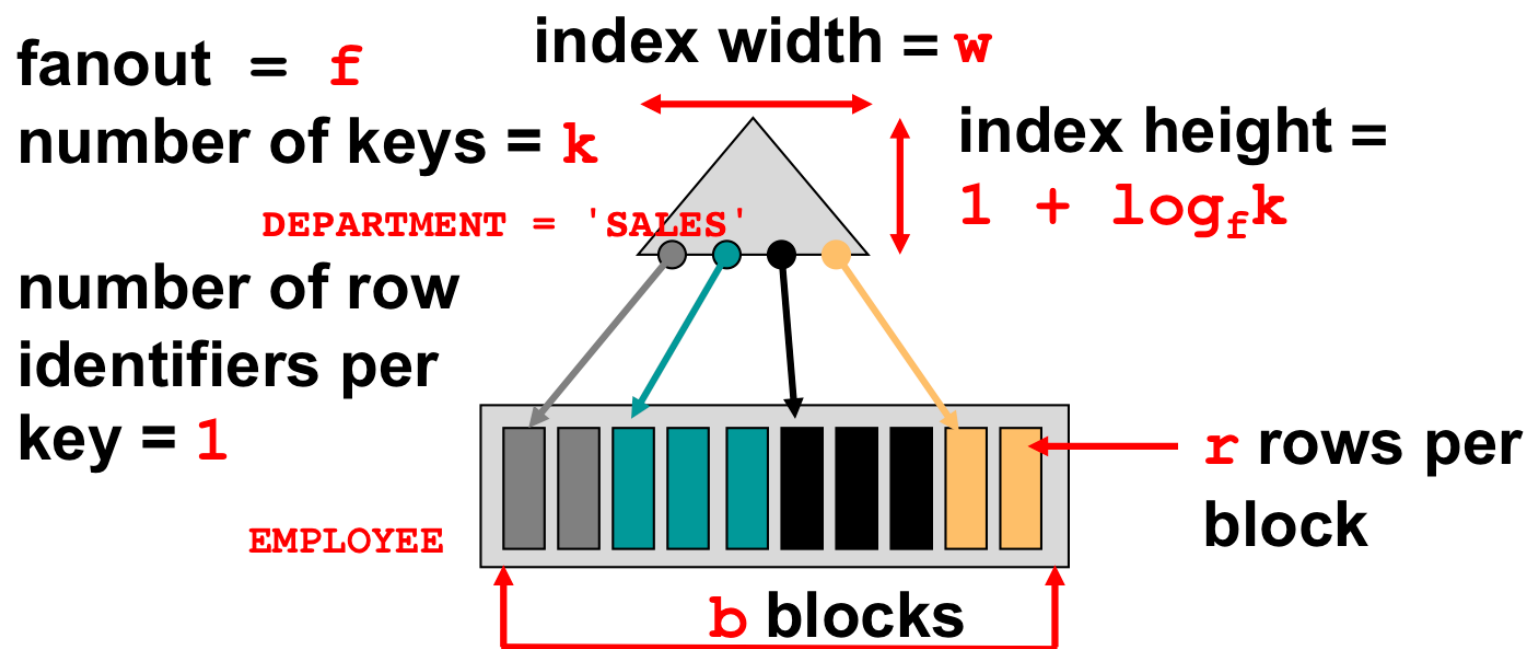
Storage organization and models

Tables with randomly ordered rows

Tables with clustered B\*-tree index

Tables with not clustered B\*-tree index

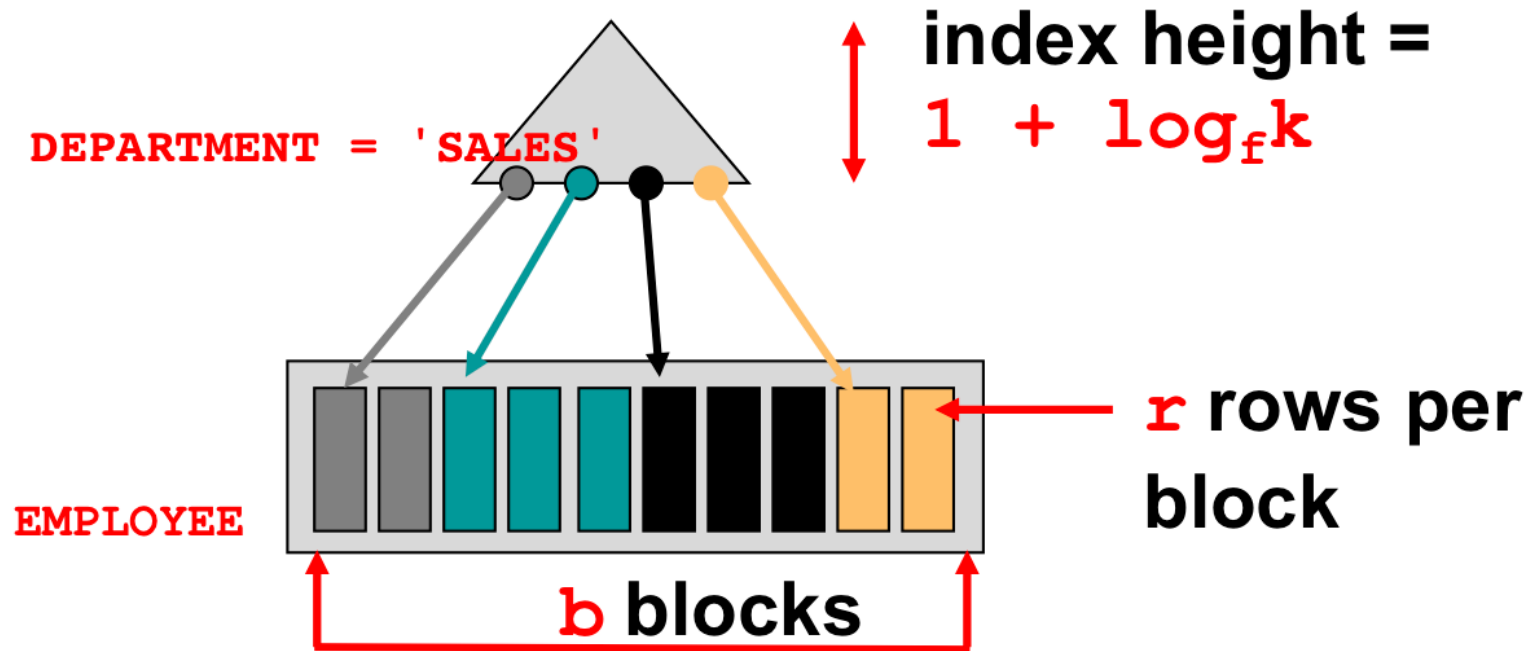
# Table with clustered B\* tree index



Average number of blocks that contain all rows with the same value of index key =  $b/k$

# Table with clustered B\* tree index

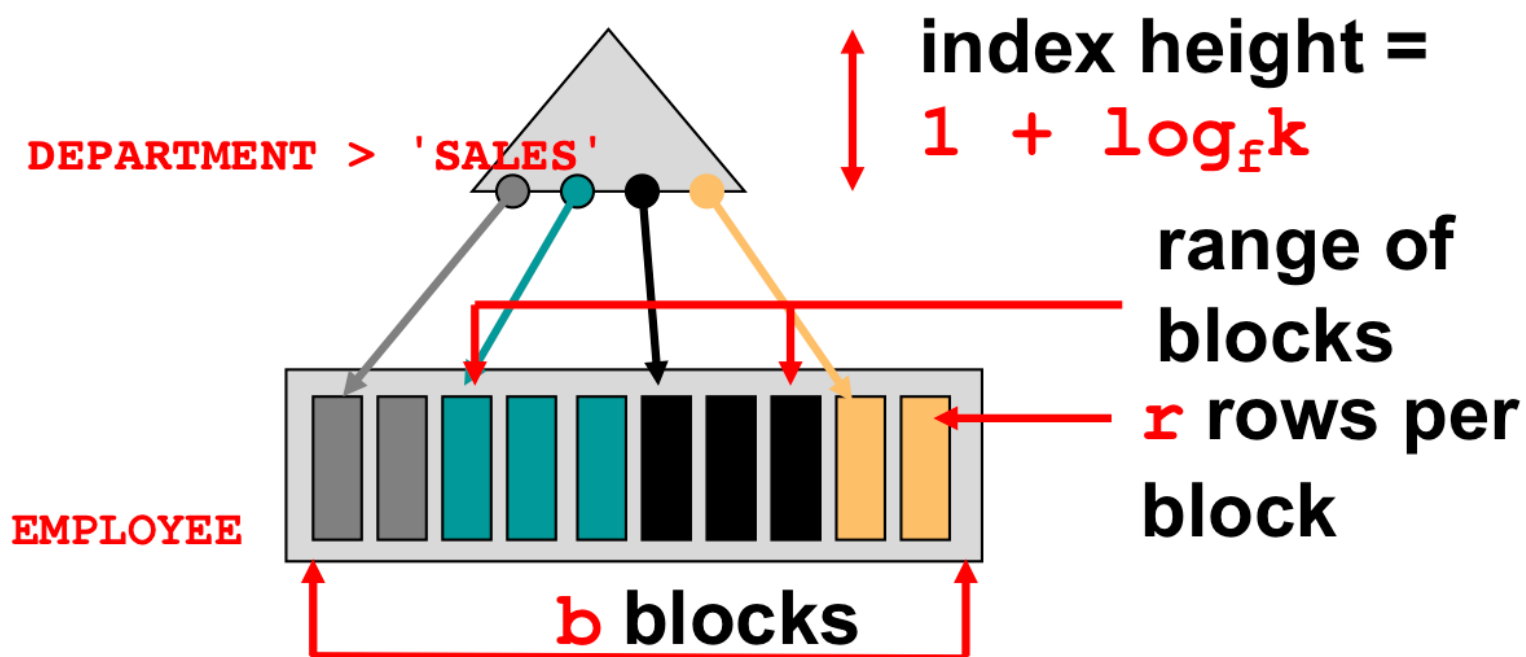
Full scan with an equality condition on a cluster key



$$\text{Cost} = 1 + \log_f k + b/k \text{ read block operations}$$

# Table with clustered B\* tree index

Full scan with a range condition on a cluster key where  $n$  is a number of cluster keys that satisfy the range condition



$$\text{Cost} = 1 + \log_f k + n \cdot b / k \text{ read block operations}$$

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Cost model ? What is it ?

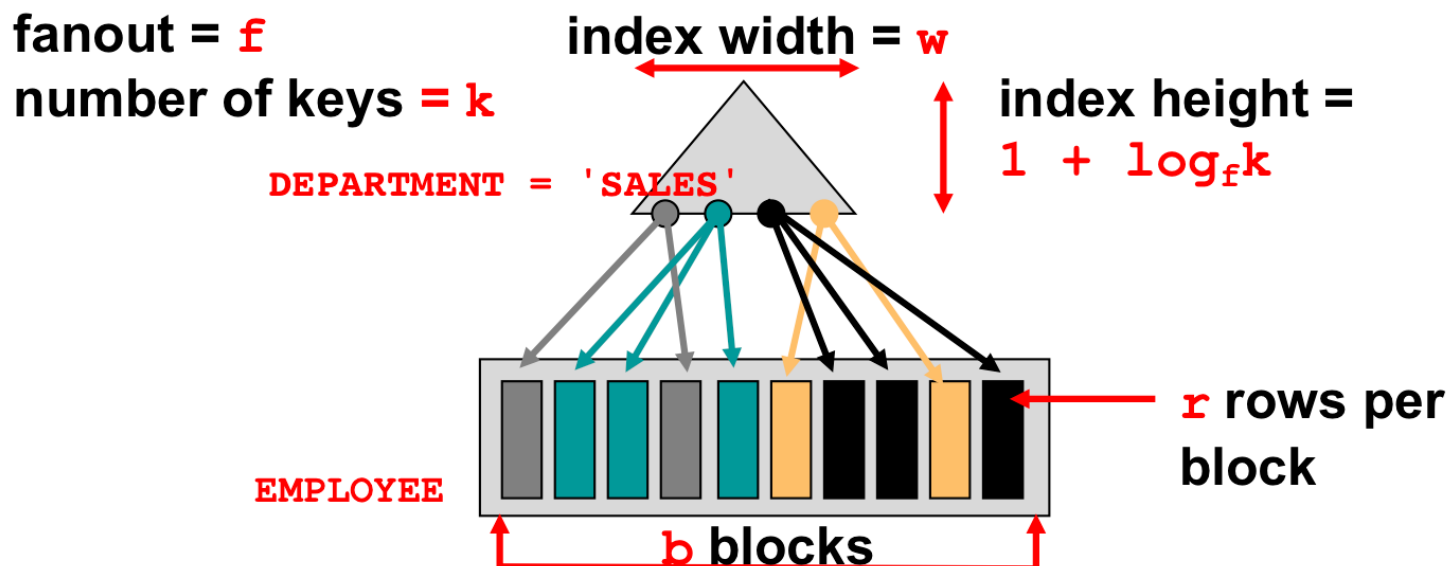
Storage organization and models

Tables with randomly ordered rows

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Tables with not clustered B\*-tree index

# Table with not clustered B\* tree index



Total number of row identifiers per index key =

$$\text{total number of rows} / \text{total number of keys} = b \cdot r / k$$

Average number of read block operations to read  $b \cdot r / k$  rows =

$$(\text{the worst case} + \text{the best case}) / 2 = (b \cdot r / k + (b \cdot r / k) / r) / 2$$

$$= (b \cdot r / k + b / k) / 2 = b \cdot (r + 1) / (2 \cdot k) \approx b \cdot r / (2 \cdot k)$$

# Table with not clustered B\* tree index

Full scan with an equality condition on an index key

fanout =  $f$

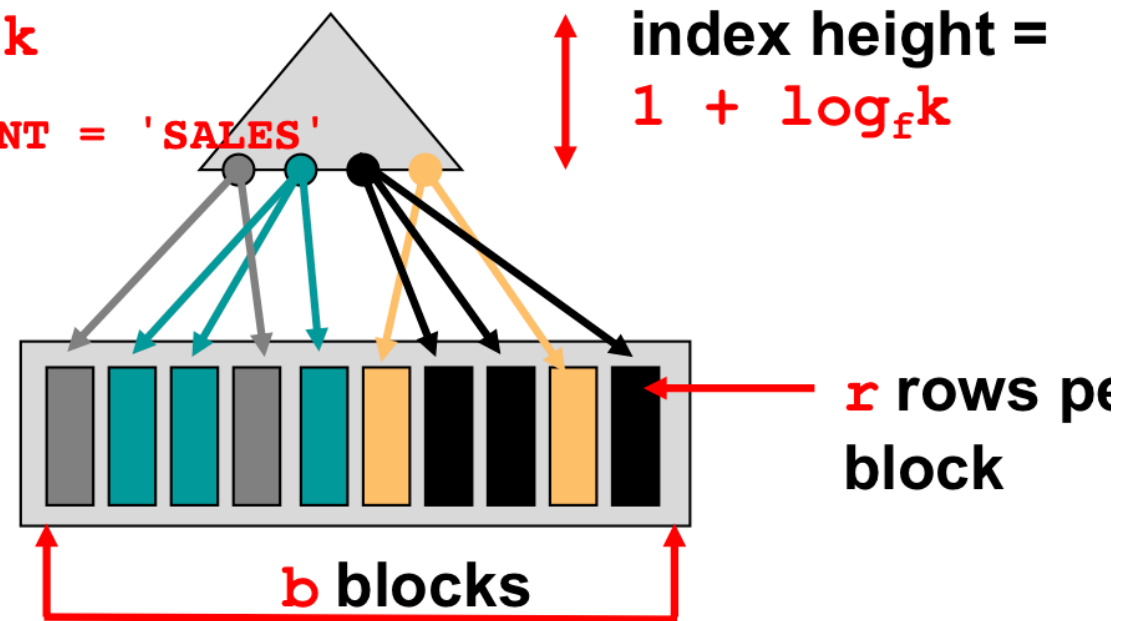
number of keys =  $k$

DEPARTMENT = 'SALES'

average number  
of row identifiers  
per index key =

$b \cdot r / k$

EMPLOYEE



Cost =  $t_{\text{traverse index}} + t_{\text{read data blocks}} =$

$1 + \log_f k + (b \cdot r / k + b / k) / 2$



# Table with not clustered B\* tree index

Full scan with a range condition on an index key where  $n$  is a total number of index keys that satisfy a range condition

fanout =  $f$

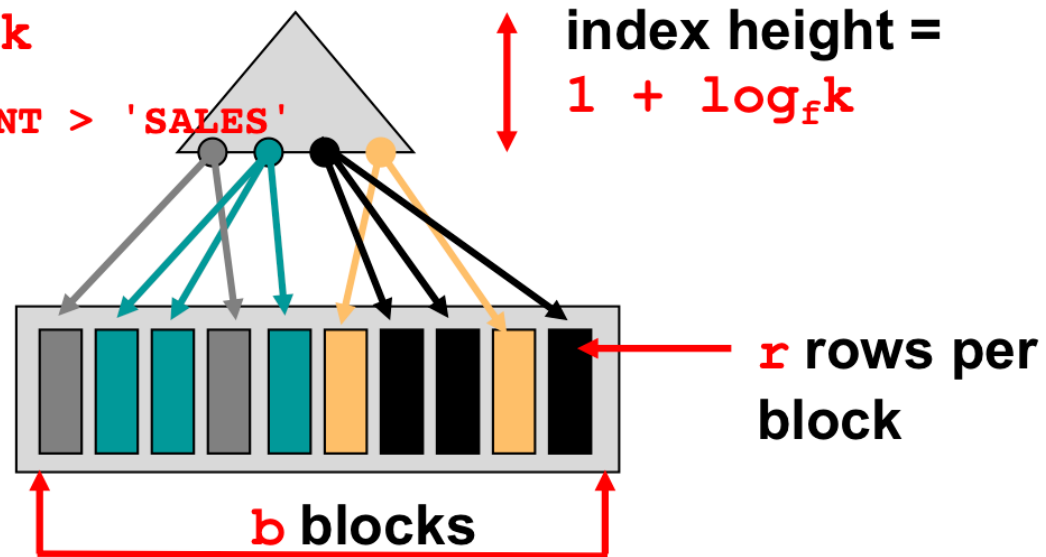
number of keys =  $k$

average number  
of row identifiers  
per index key =

$b \cdot r / k$

DEPARTMENT > 'SALES'

EMPLOYEE



Cost =  $t_{\text{traverse index}} + t_{\text{read data blocks}} =$

$1 + \log_f k + n \cdot ((b \cdot r / k + b / k) / 2)$

# References

Ramakrishnan R., J. Gehrke Database Management Systems, chapters 8.1-8.3

Lightstone, S., Teorey T., Nadeau T., Physical Database Design, The Database Professional's Guide to Exploiting Indexes, Views, Storage, and More, Morgan Kaufmann Publishers, 2007, chapter 4