

Answer any five questions from each group

**Group A**

- Q1** a. Write a program which will read the four values corresponding to the x and y axes of two points in the plane, p1 (x1, y1) and p2 (x2, y2) and calculate the distance between them. 5  
 b. Write a program which will read an integer value, which is the duration in seconds of a certain event in a factory, and inform it expressed in hours:minutes:seconds. 5

**Q2** Write a program to print the following pattern where  $3 \leq N \leq 7$ : 10

N=4  

```

****      ****      ****
*          *          *
*          *          *
*          *          *
****      ****      ****
    
```

- Q3** Write a program to calculate the cumulative sum of N integer. You will be given N and in the next line, there will be N numbers. You have to print cumulative sums from 1st to nth number. 10

Input	Output
12	0 8 15 21 22 24 28 25 24 35 36
0 8 7 6 1 2 4 -3 -1 11 0 5	40

- Q4** a) Write C function headings for the following functions described. Note that you need write only the headings, not the body. 4  
 i. `sum_of_digits()` takes a string argument and an int argument, and returns a double.  
 ii. `random()` takes no argument and returns an int. 6  
 b) Consider the variable declaration: `double num[10];`  
 i. How many elements does the array have?  
 ii. What kind of value can be stored in each element?  
 iii. Which of the following is a correct usage of `scanf()` with this array?  
`scanf("%lf", num[2]);` `scanf("%lf", &num[2]);` `scanf("%lf", &num);`

- Q5** a. Write a program that take two integer N and M as input and check if the sum of  $N^{\text{th}}$  and  $M^{\text{th}}$  Prime is even or odd? 5  
 b. Write a program to check where a number is palindromic number or not? [121 is an example] 5

**Q6** Write a program to search a value from the Given N numbers using Binary search 10

Input	Output
5 3	Case 1: Yes, Found at 4 position
0 1 2 3 4	Case 2: No!!!
5 6	
0 1 2 7 9	

- Q7** a) Determine which of the followings are valid identifiers. If invalid, explain why? 3  
 i) `_` (two are given) ii) `$tax` iii) `4t` iv) `while` v) `If` vi) `Abc123xyz`  
 b) What is wrong with this attempted declaration of a character string? 4  
`char name[] = {'p', 'r', 'i', 'm', 'e', 'e'};`  
 c) When should we use pointers in a C program? 3

- Q1 a) Differentiate between pass by value and pass by reference. Describe with proper example 5  
b) Write a program that generates first 20 Fibonacci numbers. (Use recursive technique) 5

Q2 What will be the output of the following programs? 2\*5

```
#include <stdio.h>

int c[10]={11,2,3,4,5,6,7,8,9,110}
main()
{
    int a,b=0;
    for(a=0;a<10;++a)
        if ((c[a]%2)==1) b+=c[a];
    printf("%d",b);
}
```

```
#include <stdio.h>

int main()
{
    int a[10]={2,5,6,3,4,1,3,7,8,9}
    int i;
    for(i=0;i<10;i++)
        a[i] += (a[i] - i);
    for(i=0;i<10;i++)
        printf("%d\n",a[i]);
    return 0;
}
```

- Q3 a) Write a program to count total number of letters, digit, and vowels, consonant and print them all in a line separated by space. 5  
b) Write a program which will take two number as a input and calculate the LCM and GCD of those two number. 5  
Example: input: 4 6 Output: GCD = 2 and LCM = 12

Q4 a. What will be the output of the following program 5

```
#include <stdio.h>
main() {
    int n = CALL(2, 3);
    printf("%d",n);
}
```

```
int CALL(int x, int y) {
    if(x < 0 || y > 5) return 0;
    CALL(x--, y++);
    printf("%d %d",x,y);
    return x;
}
```

b. Write a program to convert - decimal number to a binary number 5

Q5 a) Answer the following questions? 6

- Can a program be compiled without main() function?
- Can we assign a float variable to a long integer variable?
- What is an infinite loop?
- What is typecasting?
- What is a constant?
- What is a unary operator and what are unary operators present in C?

b) Write a program that asks the user to enter the number of days and then converts that value to weeks and days. 4  
For example, it would convert 18 days to 2 weeks, 4 days. Display results in the following format: 18 days are 2 weeks, 4 days.

Q6 a) Write the output of the code block code-1: 5

```
int X[10]={8,5,6,0,4,2,3,7,1,9};
for (int i=0; i<10; i++){
    if(X[i]&1)
        X[i]++;
    X[i] = X[i] * i;
    printf("%d %d\n", i, X[i]);
}
```

code -1

```
int main(){
    int i, n = 20;
    for (i = 0; i < n; i--)
        printf("*");
    return 0;
}
```

code -2

b) Change/add only one character and print "\*" exactly 20 times for the code block code-2. 5

Q7 a) Write a program to reverse a string. 4

b) Which of the following "for" loops declaration in C is valid and why? 6

- for (i < 10; i = 0; i++)
- for (i < 10; i++; i = 0)
- for (i = 0; i < 10; i++)
- for (i = 0; i++; i < 10)
- for (i++; i = 0; i < 10)
- for (i++; i < 0; i = 10)

$$y = x^2$$

$$y = \sqrt{x}$$

6

(c) State Green's theorem in the plane. Verify Green's theorem in the plane

$\oint_C (2xy - x^2)dx + (x + y^2)dy$ , where  $C$  is the closed curve of the region bounded by  $y = x^2$  and  $x = y^2$ .

7/ (a) Transform the equation  $11x^2 + 24xy + 4y^2 - 20x - 40y - 5 = 0$  to rectangular axes through the point  $(2, -1)$  and inclined at angle  $\tan^{-1}(4/3)$ . 5

(b) Find the condition that the general equation of second degree  $ax^2 + 2hxy + by^2 + 2gx + 2fy + c = 0$  may represent a pair of straight lines. 4

(c) Show that the equation  $2x^2 - 2xy + x + 2y - 3 = 0$  represents a pair of straight lines. Also find their point of intersection and the angle between them. 5

8. (a) Define direction cosines of a line. Find the direction cosines of the line which is equally inclined to the axes. 3

(b) Find the equation of the plane through the points  $(2, 2, 1)$  and  $(9, 3, 6)$  and perpendicular to the plane  $2x + 6y + 6z = 9$ . 5

(c) Find the equations of the line perpendicular to both line  $\frac{x-1}{1} = \frac{y-1}{2} = \frac{z+2}{3}$ ,  $\frac{x+2}{2} = \frac{y-5}{-1} = \frac{z+3}{2}$  and passing through their intersection. 6



Time: 03 hours

Full Marks: 70

Answer FIVE questions taking at least TWO from each group.

**Group A**

1. (a) If  $A$  and  $B$  are orthogonal matrices, each of order  $n$ , then show that the matrices  $AB$  and  $BA$  are also orthogonal. 4
- (b) Show that every square matrix can be uniquely expressed as the sum of a symmetric matrix and a skew-symmetric matrix. 5
- (c) Solve the following system of linear equations by using matrix inversion method: 5

$$2x - 3y + 4z = 1,$$

$$3x + 4y - 5z = 10,$$

$$5x - 7y + 2z = 3.$$

2. (a) For what values of  $\lambda$  and  $\mu$  the following system of linear equations has (i) no solution, (ii) more than one solution, (iii) a unique solution: 5

$$x + y + z = 6,$$

$$x + 2y + 3z = 10,$$

$$x + 2y + \lambda z = \mu.$$

- (b) Define rank of a matrix. Find rank of the matrix  $A = \begin{bmatrix} 1 & 2 & 0 & -1 \\ 3 & 4 & 1 & 2 \\ 2 & 3 & 2 & 5 \end{bmatrix}$ . 4

- (c) Determine whether the vectors  $u_1 = (1, \frac{1}{2}, \frac{1}{4})$ ,  $u_2 = (-2, -4, -8)$ ,  $u_3 = (3, 9, 27)$  generate  $\mathbb{R}^3$ . 5

3. (a) Define eigenvalues and eigenvectors of a matrix. Find the eigenvalues and eigenvectors of the matrix  $A = \begin{bmatrix} 4 & 6 & 6 \\ 1 & 3 & 2 \\ -1 & -4 & -3 \end{bmatrix}$ . 8

- (b) Using Cayley-Hamilton theorem find the inverse of the matrix  $A = \begin{bmatrix} 1 & 2 & 2 \\ 3 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix}$ . 6

4. (a) Define dot product and cross product of two vectors. Find the projection of the vector 4

$$\vec{A} = \hat{i} - 2\hat{j} + 3\hat{k} \text{ on the vector } \vec{B} = \hat{i} + 2\hat{j} + 2\hat{k}.$$

- (b) A particle moves along the curve  $x = 2t^2$ ,  $y = t^2 - 4t$ ,  $z = -t - 5$ , where  $t$  is the time. Find the components of its velocity and acceleration at time  $t = 1$  in the direction  $\hat{i} - 2\hat{j} + 2\hat{k}$ . 6

- (c) Suppose  $\nabla\psi = (y^2 - 2xyz^3)\hat{i} + (3 + 2xy - x^3z^3)\hat{j} + (6z^3 - 3x^2yz^2)\hat{k}$ . Find  $\psi$ . 4

**Group B**

5. (a) Define gradient of a scalar function, divergence and curl of a vector function. Find the unit normal vector to the surface  $\phi(x, y, z) = y^2 - 3yz^2 - 3xz^3 = -2$  at the point  $(0, 1, -1)$ . 6

- (b) If  $\vec{A} = (3x^2 + 6y)\hat{i} - 14yz\hat{j} + 20z^2\hat{k}$ , evaluate  $\int_C \vec{A} \cdot d\vec{r}$  from  $(0, 0, 0)$  to  $(1, 1, 1)$  along the following path  $C$ : (i)  $x = t, y = t^2, z = t^3$  (ii) the straight line joining  $(0, 0, 0)$  and  $(1, 1, 1)$ . 5

- (c) Show that  $\nabla r^n = nr^{n-2}\vec{r}$ , where  $\vec{r} = x\hat{i} + y\hat{j} + z\hat{k}$ . 3

6. (a) Show that the vector  $\vec{r} = (6xy + z^3)\hat{i} + (3x^3 - z)\hat{j} + (3xz^2 - y)\hat{k}$  is not solenoidal. 3

- (b) If  $\vec{F} = 4xz\hat{i} - y^2\hat{j} + yz\hat{k}$ , evaluate  $\iint_S \vec{F} \cdot \hat{n} dS$ , where  $S$  is the surface of the cube bounded by  $x = 0, x = 1, y = 0, y = 1, z = 0, z = 1$ . 5

1. Answer any fifteen questions in one line or less. [15x1]

- Write the truth table of  $p \oplus q$ .
- If  $N(x)$  = "x is the new kid";  $A(x, y)$  = "x is afraid of y"; and Domain x is SUST students. Translate the following quantifiers in English:  $N(\text{Gullu}) \wedge \forall x A(x, \text{Gullu})$ ;
- Find truth value of  $P(1)$  and  $P(-1)$  if  $P(x)$  is  $x = x^2$ , domain is all integer.
- What are relative prime numbers?
- How many primes are in between 10000 and 100000?
- $2^{31} - 1$  is a Mersenne prime. Write the prime number in binary number system.
- True or False?  $23 \equiv 16 \pmod{7}$ ;
- Arrange the following function as increasing complexity:  $\log n, n \log n, b^n, n!$ , constant,  $n^b$
- is the relation  $R = \{(1,1), (1,2), (1,3), (1,4), (2,2), (2,3), (2,4), (3,3), (3,4), (4,4)\}$  symmetric or anti-symmetric?
- Find the value of  $\lfloor 1/2 \rfloor + \lceil 3/2 \rceil + \lfloor 1/2 \rfloor + \lceil 7/2 \rceil$
- Find if the function  $f(a) = b, f(b) = c, f(c) = d, f(d) = a$  from  $\{a, b, c, d\}$  to it self is one to one, onto, both one to one and onto or none.
- Define  $\Theta$  if  $f(x)$  is  $O(g(x))$  and  $f(x)$  is  $\Omega(g(x))$ .
- Find the generating function if  $a_k = \frac{1}{k!}$ ;
- What is the chromatic number of a Bipartite graph.
- True or False: Two graphs are isomorphic if they have same number of vertices, edges and degrees.
- A tree traversed in pre-order, in-order and post-order are ABC, BAC and BCA, draw the tree.
- What are the operations of Boolean Algebra?
- Draw the circuit  $X.Y + Y.Z$ ;

2. Answer any three questions. [3x5]

- Proof that: for  $n \geq 1, 2 + 2^2 + 2^3 + 2^4 + \dots + 2^n = 2^{n+1} - 2$ .
- Show that the Tower of Hanoi problem can be solved in  $2^n - 1$  moves.
- Generate pseudo-random numbers using  $x_{i+1} = (ax_i + c) \pmod{m}$  where  $a = 7, c = 4$  and  $x_0 = 3$ . Find a suitable  $m$  which will generate a reasonably long sequence.
- Write the adjacency matrix of the given graph (Fig. 1). Using this adjacency matrix find the total number of paths of length 1, 2, 3 and 4 between a to c and a to d.

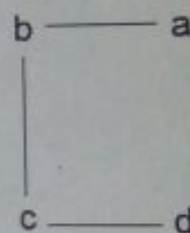


Fig.1

3. Answer any two questions. [2x10]

- Find Minimum Spanning Tree from the following graph (Fig. 2) using Kruskal's algorithm. Use Prim's algorithm to find a minimal spanning tree different from the previous one, if exists.

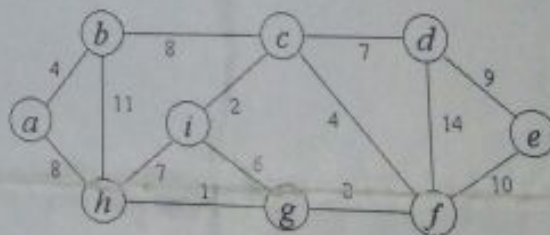


Fig.2

- Express the mathematical expression

$\sqrt{\left(\frac{x}{2} + 1\right)^2 + (2 \times y - 1)^2}$  in a binary tree using leaves as variables and internal vertices as operators using only 5 operations,  $+$ ,  $-$ ,  $*$ ,  $/$  and  $\uparrow$ . Traverse the tree in pre-order, in-order and post order. Evaluate the value using pre-order, in-order and post-order traversal for  $x = 6$  and  $y = 2$  showing each step.

- Design a digital circuit which will produce HIGH output only when the prime numbers from 0 to 9 are applied using four inputs as binary sequence. Follow the following steps: (i) use sum of products for selecting the given numbers between 0 and 9 (ii) Use Karnaugh map for minimizing the sum of products (iii) If possible minimize more using the don't-care terms (iv) draw the circuit using two input gates.



(Answer every question)

Group A

1. Answer any fifteen questions in one line or less. [15x1]

- (a) Is  $x + 3 = 2$  a proposition?
- (b) If  $C(x)$ : "x had coffee" and  $T(x)$ : "x had tea" then Express the proposition: "Every student either had coffee or had tea" using proper Quantifier.
- (c) Find the truth value of  $\exists n(5n = 7n)$  if  $n$  is integer.
- (d) A, B and C are sets then find  $(A - C) \cap (C - B)$ .
- (e) Express decimal 769 in base 13.
- (f) Find LCM of 95256 and 144.
- (g) Find GCD of 112651 and 121121.
- (h) Find the pseudo random numbers using  $x_{n+1} = (7x_n + 4) \bmod 8$  for  $x_0 = 3$ ;
- (i) Find if the Relation R is Reflective, Symmetric, Anti-Symmetric, Transitive or none.  
 $R = \{(2, 1), (3, 1), (3, 2), (4, 1), (4, 2), (4, 3)\}$ ;
- (j) Given  $f(x) = 4x + 2$  and  $g(x) = 3x + 7$ . Now, find the value of  $f \circ g$  and  $g \circ f$ .
- (k) Determine if the function from  $\mathbb{Z}$  to  $\mathbb{Z}$  is one-to-one, onto, both or none:  $f(n) = n^2 + 1$ ;
- (l) Find C and k for  $f(x)$  is  $O(x)$   $f(x) = 3x + 7$ .
- (m) What is the sequence of the generating function,  $f(x) = \frac{1}{1-ax}$ ?
- (n) A map is drawn with 23 vertices and 79 edges, how many countries are there?
- (o) Will you be able to draw the Olympic Symbol without lifting your pen?
- (p) What is the difference between a tree and a graph?
- (q) Which set of operators are functionally complete in Boolean algebra?
- (r) Design an OR gate using only NAND gates.

2. Answer any three questions. [3x5]

(a)  $\neg(p \vee (\neg p \wedge q)) \equiv \neg p \wedge \neg q$  Check if the two statements  $p \vee (q \rightarrow r)$  and  $(p \vee q) \rightarrow (p \vee r)$  are logically equivalent or not.

(b) Plot the function:  $\lceil x/3 \rceil + \lfloor x/3 \rfloor$  for  $-9 < x < 9$ ;

(c) Find  $7^{341} \bmod 679$ .

(d) Draw the graph  $G = (V, E)$  where the seven vertices are given by  $V = \{AB, BC, BF, CD, CE, DE, EB\}$ . The directed edges are given by  $E = \{\text{between the vertices where end letter of one vertex is same as the start letter of the other vertex}\}$ . Does it have Euler circuit? Euler Path? Write all of them.

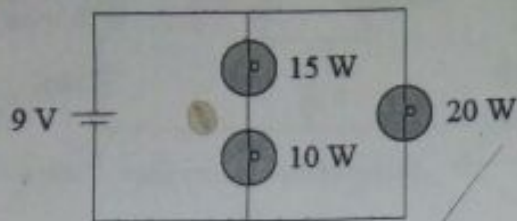
3. Answer any two questions. [2x10]:

(a) Find the solution of the recurrence relation:  $a_n = 2a_{n-1} + a_{n-2} - 2a_{n-3}$  if  $a_0 = 0$ ,  $a_1 = 1$  and  $a_2 = 2$

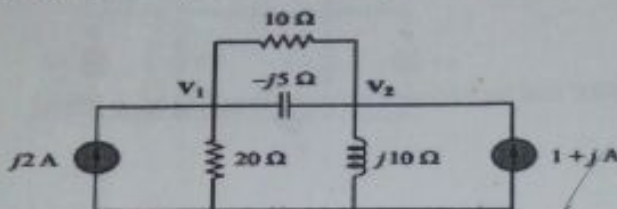
(b) Suppose the letters A, B, D, E, G, H, L, N and S are used 16, 11, 5, 28, 4, 8, 10, 6 and 12 percent of times. (i) Generate prefix codes for these letters using a binary tree using Huffman coding and find out what is written by: 01011100011111100000000110011 (ii) Write BANGLADESH using these codes.

(c) (i) RSA encryption of an integer M is given by  $C = M^e \bmod (pq)$  where p, q are prime numbers. If  $p = 5$  and  $q = 7$ , Find the smallest e and use that to find C for  $M=11$ . (ii) RSA decryption is given by  $M = C^d \bmod (pq)$  find d if  $p = 5$ ,  $q = 11$  and  $e = 3$ . If  $C = 18$  decrypt to find M.

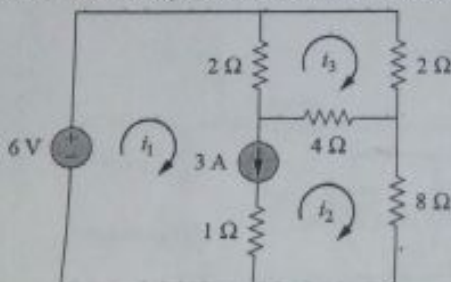
6. (a) Three lightbulbs are connected to a 9-V battery as shown in Fig. 4. Calculate: (a) the total current supplied by the battery, (b) the current through each bulb, (c) the resistance of each bulb.



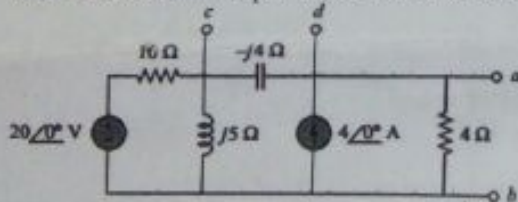
- (b) Using nodal analysis find  $V_1$  and  $V_2$  in the circuit.



- (c) Use mesh analysis to determine  $i_1$ ,  $i_2$  and  $i_3$  in the following figure



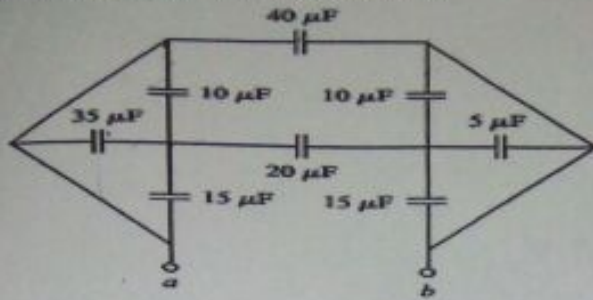
- (d) Find the Thevenin equivalent circuit as seen from a-b.



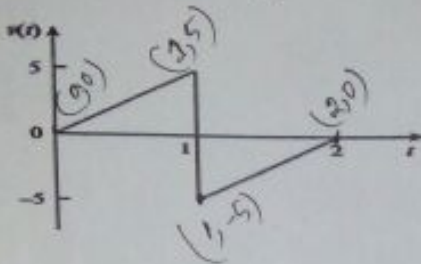
$$i(t) = 1e^{-5t} \text{ A}, \quad t > 0$$

Find the voltage  $v(t)$ .

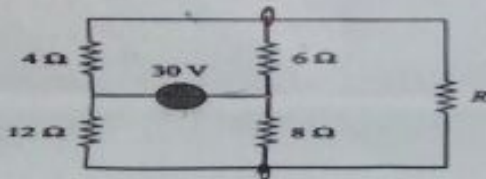
(c) Find the equivalent capacitance for a-b terminals.



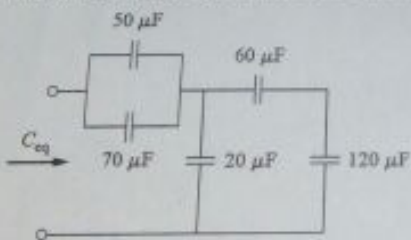
(d) If the voltage waveform is applied to a 10mH inductor find the inductor current  $i(t)$  and assume  $i(0)=0$ .



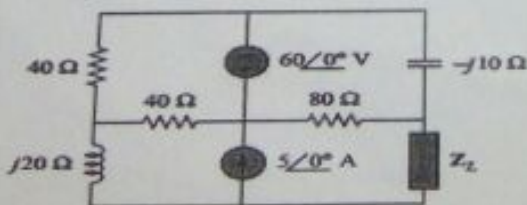
5. (a) For what value of  $R$  is the power dissipated in  $R$  maximum? Calculate that power.



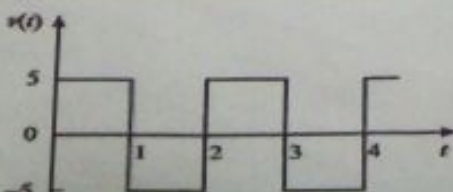
(b) Find the equivalent capacitance seen at the terminals of the following circuit.



(c) Find the value of  $Z_L$  for maximum power transfer.



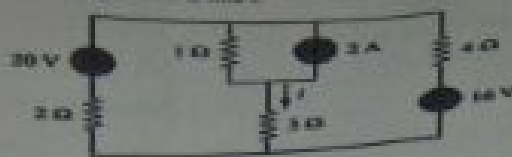
(d) Determine the rms value of the waveform.



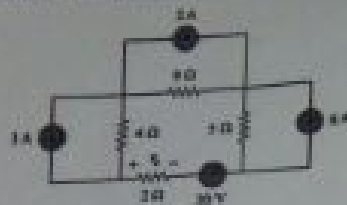
$$= \sqrt{\frac{1}{2} \int_0^1 25 dt + \frac{1}{2} \int_1^2 25 dt}$$



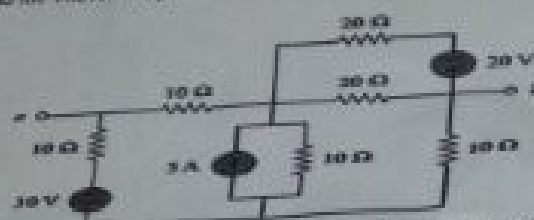
- (b) Use superposition to find  $i$ .



- (c) Obtain  $V_x$  using source transformation.



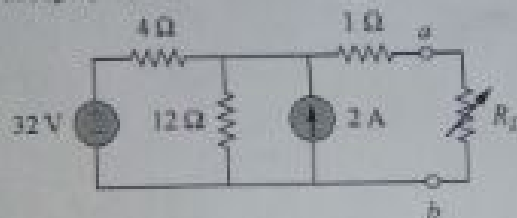
3. (a) Find the Thevenin equivalent circuit between the terminals a and b.



- (b) Obtain the Norton equivalent circuit as viewed from the terminal (I) a-b (II) c-d.



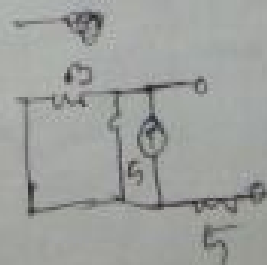
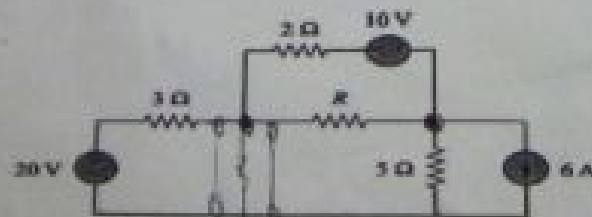
- (c) Find the Thevenin equivalent circuit of the circuit shown in Fig. 10, to the left of the terminals a-b. Then find the current through  $R_L = 6, 16$  and  $36 \text{ ohm}$ .



### Part- B

(Answer any two of the following questions)

4. (a) Find the maximum power that can be delivered in the resistor  $R$ .

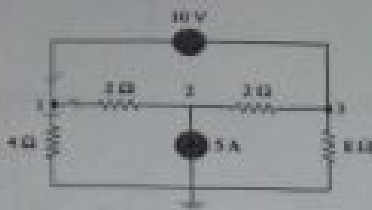


- (b) The current through a 40mH inductor is

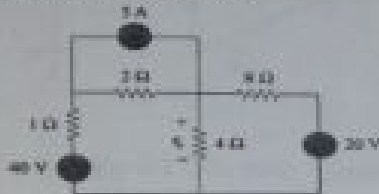
Part - A

(Answer any two of the following questions)

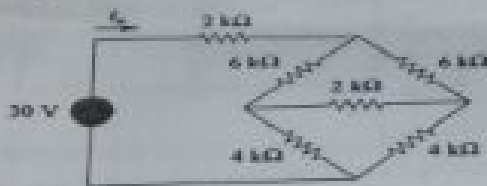
1. (a) Determine the node voltages in the circuit using nodal analysis



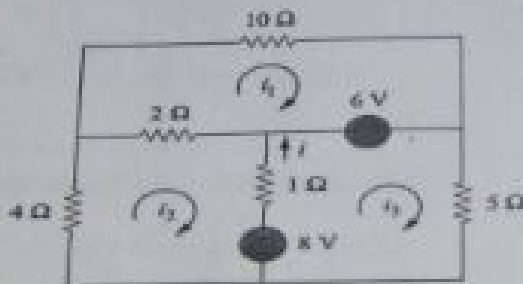
- (b) Using nodal analysis find  $V_x$ .



- (c) Find  $i_x$  using mesh analysis.



- (d) Find  $i$  in the circuit.



2. (a) Determine  $V_x$  using superposition principle.

