

Group – A
(Answer Any Two Questions)

1.

- a. Find the equation of the straight line which passes through the intersection of $2x + 5y - 1 = 0$, $x - 3y + 2 = 0$ and makes equal intercept on the axes. 4
- b. Find the angle between the line $3x - y + 3 = 0$ and the line perpendicular to $\frac{1}{2}x - \frac{1}{3}y + 1 = 0$. 5
- c. Find the equation of the circle passing through the intersection of the circle $x^2 + y^2 = 2by$ and having its center on the line $\frac{x}{a} - \frac{y}{b} = 2$. 4
- d. Find the equation of the parabola whose focus is at $(-1, 2)$ and directrix $x - 2 = 0$. What is the vertex of the parabola? Sketch the graph of it. 5
- e. Find the center, vertices, foci and length of the minor axis of the ellipse. 4
- $2x^2 + 5y^2 = 10$
- f. Find the eccentricity of the hyperbola $\frac{x^2}{5} - \frac{y^2}{4} = 1$. 3

2.

- a. Find the standard equation of the conic $2xy = 9$ by rotating the axes through an angle $\frac{\pi}{4}$ radians about the origin. Identify the conic. 4
- b. Find the rotation α so that the equation $2x^2 + \sqrt{3}xy + y^2 - 10 = 0$, has no xy term and hence identify the curve. 4
- c. Define direction cosines and direction ratios of a straight line. P and Q are $(1, -5, 7)$ and $(-3, 6, -2)$. Find the direction cosines of OP, OQ, and PQ. 4
- d. Find the direction cosines of the line which is equally inclined to the axes. 3
- e. Find the angle between the planes $2x - 3y + 5z + 1 = 0$ and $x - 3y + z + 2 = 0$. 3
- f. Find the centre and radius of sphere $x^2 + y^2 + z^2 + 3x - 6y + 1 = 0$. 3
- g. Identify the surfaces- 4

i. $\frac{x^2}{4} + \frac{y^2}{6} - \frac{z}{6} = 0$	ii. $\frac{x^2}{3} + \frac{y^2}{5} - \frac{z^2}{4} = 0$
iii. $\frac{x^2}{9} + \frac{y^2}{8} - \frac{z^2}{3} = 1$	iv. $x^2 - y^2 - z = 0$

3.

- a. Define function, domain and range of a function. Find the domain and range of following functions: 8

i. $y = \sqrt{4 - x^2}$	ii. $y = \frac{ x }{x}$
iii. $y = \ln(2x - 1)$	

Also sketch the graph of the function.

- b. Find the left hand limit and right hand limit and limit of the function $f(x) = \sqrt{1 - x^2}$ at $x = 1$. 3
- c. Test the continuity of the step function- 3

$$f(x) = \begin{cases} e^x & \text{if } x < 0 \\ 1 & \text{if } x \geq 0 \end{cases}$$

at $x = 0$

- d. Find the derivative of the functions: 6

i. $f(x) = \ln(x^2 + 1) \sin^2 2x$	ii. $f(x) = x^x$
------------------------------------	------------------

- e. Find the n^{th} derivative of $\tan^{-1} \frac{x}{a}$. 5

Group – B
(Answer Any Two Questions)

4.

a. State the Rolle's theorem and the Mean Value Theorem. Deduce the Rolle's Theorem from the Mean Value Theorem. 4

b. Find the maximum and minimum values of the function $f(x) = x^4 - 5x^3 + \frac{9}{2}x^2 - 1$ 5

c. Define the Tylor series and Maclaurin series generated by a function. Find the Tylor series of the function $f(x) = \ln(1+x)$ at $x = 1$ 6

d. Let $f(x, y) = \frac{2y}{y + \cos x}$. Then find- 6

i. f_{xx}	ii. f_{xy}
-------------	--------------

e. If the resistors of R1, R2 and R3 ohms are connected in parallel to make an R-ohm resistor, the value of R can be found from the equation- 4

$$\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$$

Find the value of $\partial R / \partial R_2$ when $R_1 = 30$, $R_2 = 45$ and $R_3 = 90$ ohms.

5.

a. Evaluate the integrals- 12

i. $\int \frac{dx}{\sqrt{x^2 - 4x + 3}}$	ii. $\int \frac{dx}{3 + 2 \cos x}$
iii. $\int_0^{2a} \frac{dx}{\sqrt{(2ax - x^2)}}$	

b. State and prove the fundamental theorem of integral calculus. 4

c. Evaluate the integral- 4

$$\int_0^2 x^2 dx$$

- 0.26

As a limit of Riemann sums.

d. Use reduction formula to evaluate the integral- 5

$$\int \sin^2 x \cos^3 x dx$$

6. a. Evaluate the improper integral-

$$\int_0^2 \frac{dx}{(x-1)^{\frac{2}{3}}}$$

5

b. Define Gamma function and hence find $\Gamma(3)$ 4

c. Write the relation between Beta and Gamma function. Use the relation to evaluate $\beta(3, 2)$ 4

d. Find the area of the segment of the parabola $y = (x-1)(4-x)$ cutoff by the x-axis. 4

e. Find the volume of the solid generated by revolving the region bounded by $y = \sqrt{x}$ and the lines $y=1$, $x=4$ about the line $y=1$ 4

f. Find the volume of the washer generated by revolving the region bounded by the curves $y = x^2$ and $y = \sqrt{x}$ about the x-axis. 4

Note: Answer four questions taking any two from each group. Figures at right margin show marks.

Group - A

- 1.a) Explain the basic data types in C with their memory requirement. 4
- b) What is type casting in C? Show with an example. 3
- c) What is escape sequence? Give examples. 3
- d) Identify the purpose of each of the following expressions: 5
 - i) ceil(x), ii) floor(x+y), iii) sqrt(x*x+y*y), iv) pow(2, 3.0) and v) sin(x-y).
- e) Consider the following program fragment. What will be the output? 4

```
int main() {
    int a = 10;
    printf("\n %d %d", a, a++);
    a = 10;
    printf("\n %d %d", a++, a);
    a = 10;
    printf("\n %d %d %d ", a, a++, ++a);
}
```
- f) If a = 10, b = 5 and c = 20, what will be the truth value of the following expressions: 4
 - i) !(a > 10), ii) (a >= 5) && (b == 5), iii) (a + b) > c || (c < 30), iv) (a < 5) || (b > c) && (c > 10)
- g) How are comments used in a C program? Give examples. 2
2. a) For the following **for** statement, write an equivalent **while** statement. 3

```
for (<init-stmnt>; <boolean-expr>; <incr-stmnt>)
{
    <body-statements>
}
```
- b) Distinguish between **while(1)** and **while(0)** with example. 4
- c) What will be the output of the following C code? 3

```
int main(void)
{
    if (printf("Hello World"));
}
```
- d) Write the output of the following program fragments shown in Figs. 1 and 2. 5+5

```
int main(){
    int i,j;
    for(i=0;i<10;i++)
        for(j=0;j<10;j++)
            printf("%d\t%d\n",i,j);

    for(i=0;i<100;i++)
        for(j=0;j<10;j++)
            printf("%d\t%d\n",i,j);
}
```

Fig. 1

```
int main() {
    int i, j;
    for (i = 0; i < 5; i++) {
        for (j = 1; j <= 10; j++) {
            if (j > 3) break;
            printf("*");
        }
        printf("\n");
    }
}
```

Fig. 2
- e) What will be the output of the program in Fig. 2 if the keyword **break** is replaced with **continue**? 5
- 3.a) What are the advantages of structured programming? 2
- b) Rewrite the following program using structured programming approach. 5

```
#include <stdio.h>
double balance = 100000;
int main() {
    double amount;
    printf("Enter amount to deposit:");
    scanf("%lf", &amount);
    balance += amount;
    printf("Enter amount to withdraw:");
    scanf("%lf", &amount);
    balance -= amount;
    printf("Your current balance: %lf", balance);
}
```
- c) Write an appropriate function call for each of the following functions. 4
 - i. void exchange(int &x, int &y)
 - ii. float area(float r) { return 3.14*r*r; }
- d) How is an array name interpreted when it is passed to a function? 2

e) What are the criteria of a recursive program?

f) Let a recursive function R is defined as $R(a, b) = \begin{cases} 0, & \text{if } a < b \\ R(a - b, b) + 1, & \text{if } b \leq a \end{cases}$

What is actually performed by the above function? Find the value of R(16, 3) and R(200, 6).

g) What are the differences between global and local variables? Show with example.

Group - B

4.a) Assume a one dimensional array x[] = {1,2,3,4,5,6,7,8,9,10,11,12}. Write C code to assign the elements to a 2D array y[3][4].

b) Pass the array y[3][4] in (a) to a function and display the elements in matrix form.

c) How do you use variable sized array in C? Show with an example.

d) Describe what values are assigned to the individual array items.

int z[12]={0, 8, 0, 0, 7}, char flag[] = "TRUE", char flag[4] = {'T', 'R', 'U', 'E'}, int p[2][4]={1, 3, 5, 7};

e)

```
i. #include <stdio.h>
int main ( )
{
    int i, y=0;
    char s[] = "Programming with C";
    for (i = 0; s[i] != '\0'; ++i) {
        if ((i % 2) == 0) y += x[i];
        printf("%c%c", s[i], s[i]);
    }
}
```

```
ii. #include <stdio.h>
int main( )
{
    int a, b, c=99;
    int x[][4] = {1,2,3,4,5,6,7,8,9,10,11,12};
    for (a = 0; a < 3; ++a) {
        for (b = 0; b < 4; ++b) {
            if (x[a][b] < c) c = x[a][b];
            printf("%d ", c);
        }
    }
}
```

5.a) Distinguish between a string and a character array.

b) What will be the output of the following programs?

```
i. #include <stdio.h>
int funct(int x) {
    int y;
    y = x * x;
    return y;
}
int main ( )
{
    int a, count, sum=0;
    for(count=1; count<=10; ++count) {
        a = funct(count);
        printf("%d ", a);
        sum += a;
    }
    printf("\nSum: %d", sum);
    return 0;
}
```

```
ii. include <stdio.h>
int funct(int *p)
{
    int i;
    for (i = 0; i < 5; i++) *(p+i) = *(p+i) / *(p+i);
}

int main( )
{
    int i, a[] = {10, 20, 30, 40, 50};
    funct(a);
    for (i = 0; i < 5; i++)
        printf("%d ", a[i]);
}
```

c) What are the problems with the following programs:

```
i. #include <stdio.h>
int main ( ) {
    float radius; area;
    printf("Radius = ?");
    scanf("%f", radius);
    area = 3.14159 * radius * radius;
    printf("Area: %f, &area);
    return 0;
}

/* CODE A */
```

```
ii. #include <stdio.h>
int main ( ) {
    int 2repeat = 10;
    for (int i=0; i<2repeat; i++) {
        printf("Hello Bangladesh \n");
    }
    return 0;
}

/* CODE B */
```

d) For two given strings S1 and S2, swap the value of S1 and S2, if S1 > S2.

e) Rewrite the program in (d) so that it allocates memory for S1 and S2 using dynamic memory allocation.

6.a) Define a structure **CourseResult** with members **Attendance**, **Perf**, and **Final**. Write a program to calculate the letter grade of a course using the structure **CourseResult** (as per SUST rules).

b) Declare an array of size 50 of type **CourseResult** and print how many students got A+.

c) Distinguish between the file opening modes "r" and "r+" and "w" and "a".

d) Write a program to write the **CourseResult** information in (b) into a text file.

e) Rewrite the program in (b) to display the information reading from the text file.

Course Code: EEE 101W
Course Title: Basic Electrical and Electronic Circuits

Time: 3 Hours
Total Marks: 100

Answer four questions taking two from each part. Figures at right margin show marks.

Part A

- 1 a) The current flowing through a point in a circuit is shown in fig. 1. Find the total charge flowing through that point in the circuit. (5)

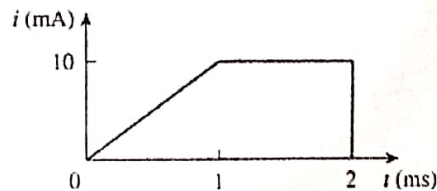


Figure 1: for question 1(a)

- b) Fig. 2 shows the current through and voltage across a given device. Find the total energy absorbed by the device for the period of $0 < t < 4$ s. (8)

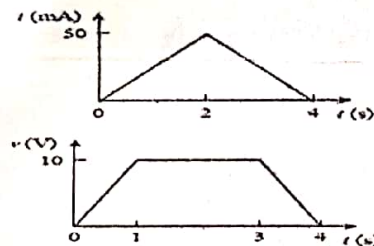


Figure 2: for question 1(b)

- c) Determine V in the circuit shown in fig. 3. (7)

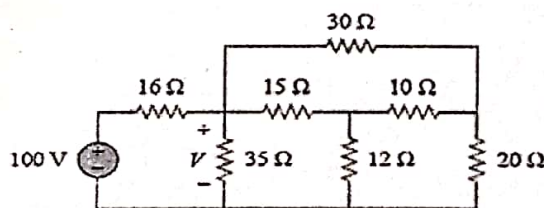


Figure 3: for question 1(c)

- d) Determine powers dissipated in the resistors in the circuit shown in fig. 4. (5)

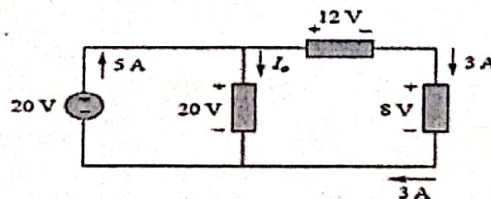
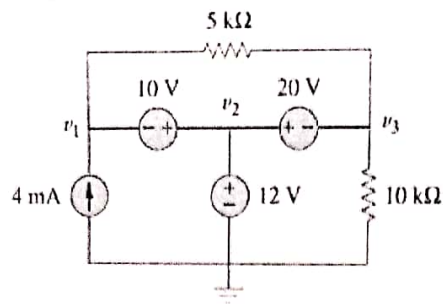
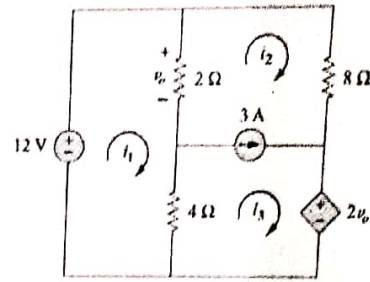


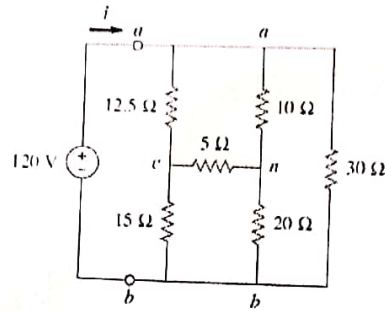
Figure 4: for question 1(d)



(a)



(b)



(c)

Figure 5: (a) for question 2(a) (b) for question 2(b) (c) for question 2(c)

2. a) Using nodal analysis, obtain node voltages v_1, v_2, v_3 in the circuit of figure 5(a) (7)
- b) Using mesh analysis, obtain i_1, i_2, i_3 in the circuit of figure 5(b) (9)
- c) Obtain the equivalent resistance R_{ab} for the circuit in fig 5(c) and use it to find current i . (9)
3. a) Find the Thevenin and Norton equivalents at terminals $a - b$ from figure (6) (12)

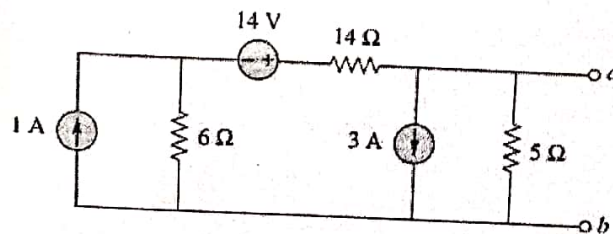


Figure 6: for question 3(a)

- b) Why superposition principle is not applicable in power calculation? Prove that, maximum power $P_{max} = \frac{V_{th}^2}{4R_{th}}$ (5)
- c) Compute the value of R that will result in maximum power transfer to the 10Ω resistor as shown in figure 7. Find the maximum power. (8)

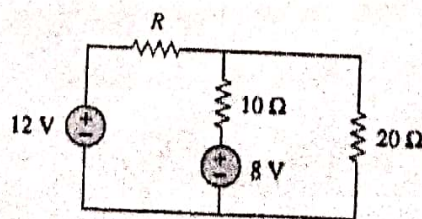


Figure 7: for question 3(c)

4. a) Determine v_o in the op-amp circuit of figure 8, show details calculation without using formula. (5)

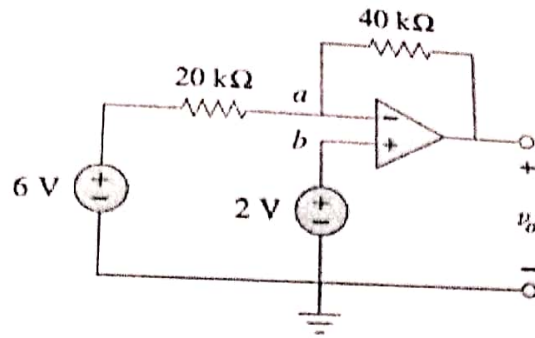


Figure 8: for question 4(a)

- b) Design an Op-amp circuit with inputs v_1 and v_2 such that $v_o = -5v_1 + 3v_2$. (10)
 c) If $v_1 = 1V$ and $v_2 = 2V$, find the v_o of the circuit of figure 9. (10)

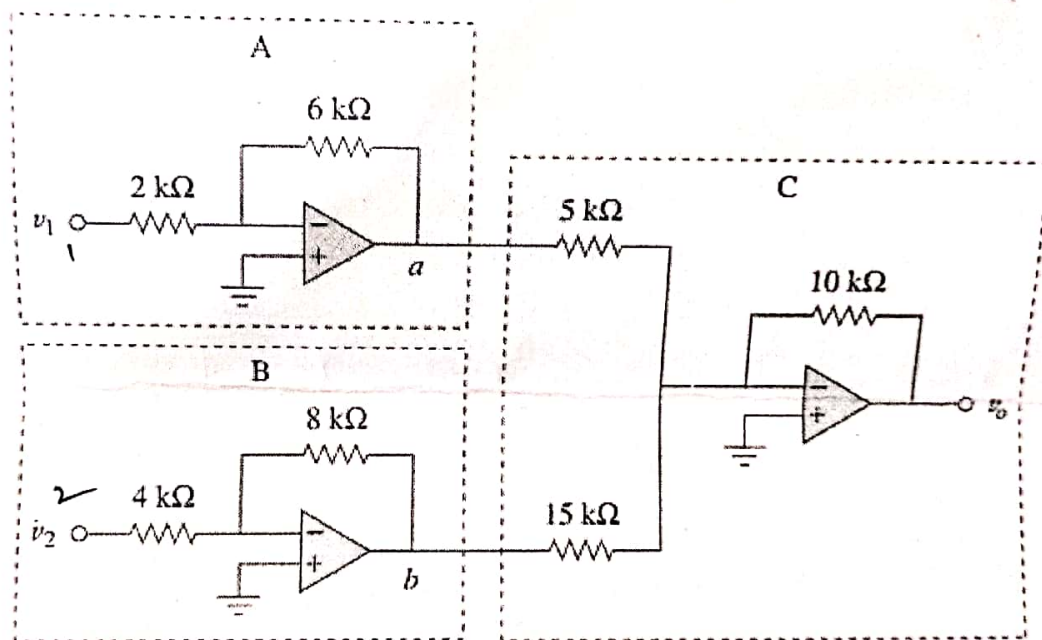


Figure 9: for question 4(c)

5. a) Determine the current through a $200 \mu F$ capacitor whose voltage is shown in figure 10. (9)

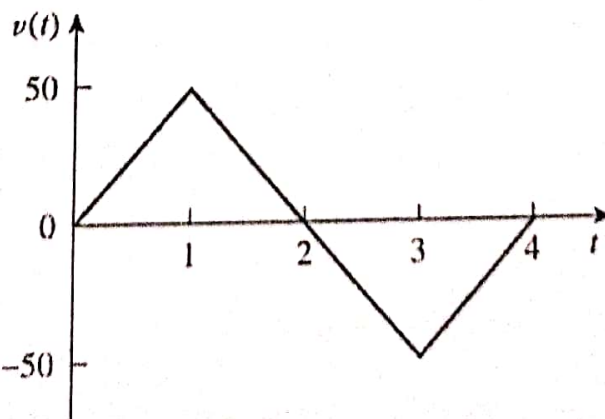


Figure 10: for question 5(a)

$$v_2 = \frac{R_2}{R_1 + R_2} v_1$$

b) Obtain the energy stored in the capacitors under dc condition from figure 11.

(8)

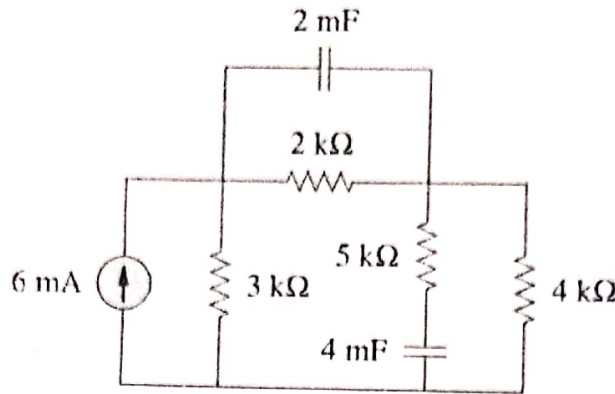


Figure 11: for question 5(b)

c) If $v_1 = 10 \cos 2t$ mV, and $v_2 = 0.5t$ mV, find v_o in the op-amp circuit of figure 12.

(8)

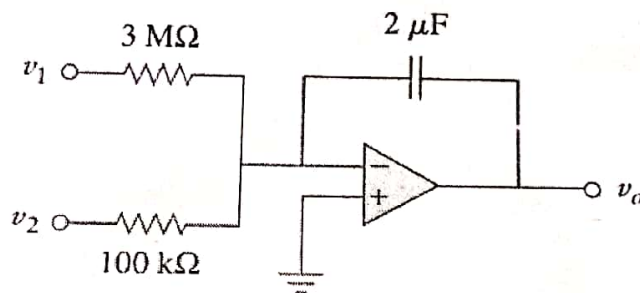


Figure 12: for question 5(c)

6. a) Reduce the following Boolean expressions to the indicated number of literals-

(9)

(i) $A'C' + ABC + AC'$

to three literals

(ii) $(x'y' + z)' + z + xy + wz$

to three literals

(iii) $A'B(D' + C'D) + B(A + A'CD)$

to one literal

b) A manufacturing plant needs to have a horn sound to signal quitting time. The horn should be activated when either of the following conditions is met:

(8)

i. Its after 5 oclock and all machines are shut down.

ii. Its Friday, the production run for the day is complete, and all machines are shut down.

Design a logic circuit that will control the horn. c) Design a 8×1 MUX by using 2×1 MUX.

(8)