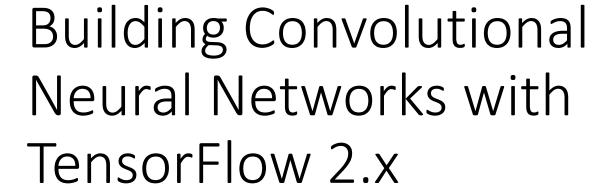




Billy Herzberg william.herzberg@marquette.edu









About Me

- BS Mechanical Engineering 2018 Marquette University
- MS Applied Statistics 2020 Marquette University
- PhD Computational Sciences 20?? Marquette University

- First started with deep learning in Summer 2019
- Convolutional Neural Networks for Electrical Impedance Tomography (EIT) image reconstruction
 - Post processing images with a U-Net CNN
 - Model-based, learned, iterative reconstruction



What Makes a Neural Network?



- Inputs *X*
- Truths *Y*
- Split into training and validation

•
$$X = [X_{tr} \quad X_{va}]^T$$

Model

- Has layers
- Has parameters θ
- Makes predictions

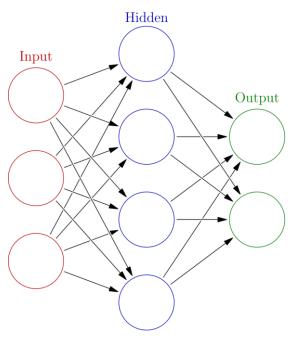
•
$$\hat{Y}^{(k)} = Net_{\theta}(X^{(k)})$$



- Evaluates model
- $loss = f(Y, \hat{Y})$



- Adjusts θ during training
- Ex. gradient descent
- Training the model
 - Split training data into batches
 - Update θ after each batch



Outline

- 1D Convolution
 - Stride, Padding
- 2D Convolution
 - Single channel input
 - Multiple channel input (i.e. RGB)
 - Multiple channel output
- Choosing Weights
 - Finding changes, edges, peaks, features, etc.
- Pooling Layers

- Transposed Convolutions
 - 1D
 - 2D
 - Stride, padding
 - Multiple channel input
 - Multiple channel output
- U-Net Architecture
 - Post-processing images



Outline

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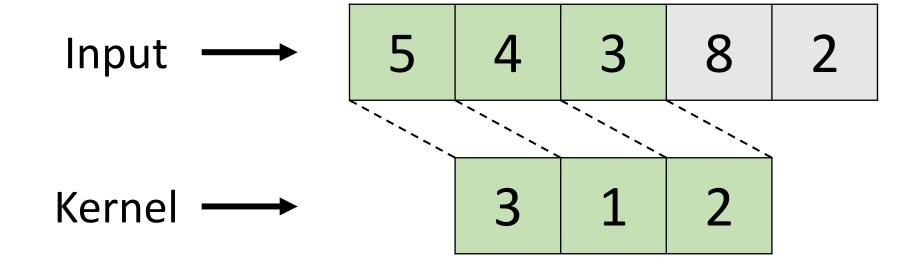


Kernel →



Output —

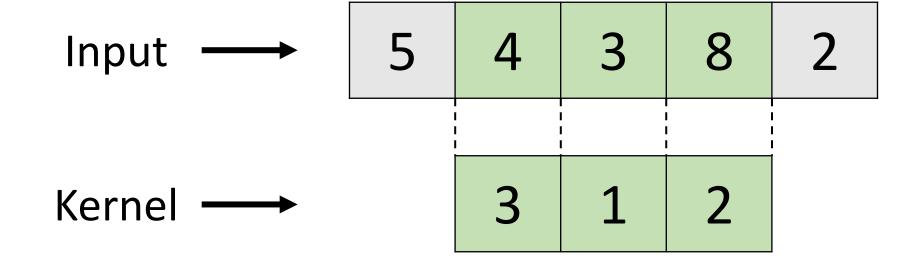




$$(5*3) + (4*1) + (3*2) = 25$$

Output ----

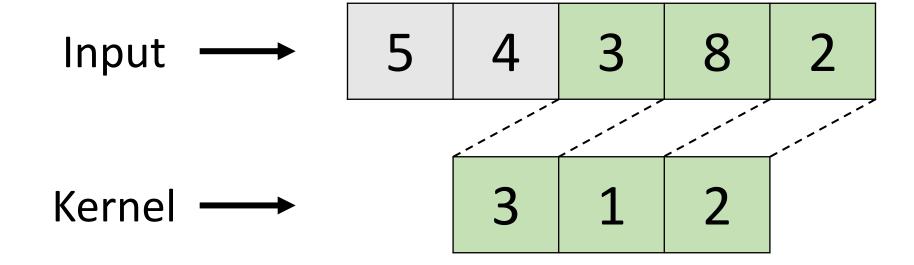




$$(4*3) + (3*1) + (8*2) = 31$$

Output → 25 31





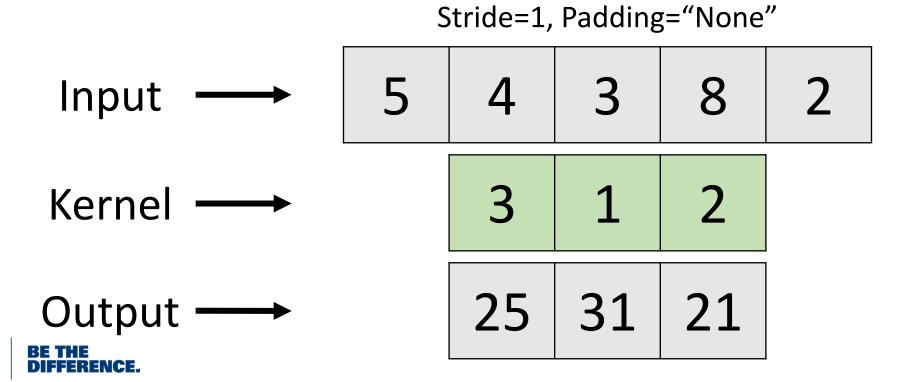
$$(3*3) + (8*1) + (2*2) = 21$$

Output ---

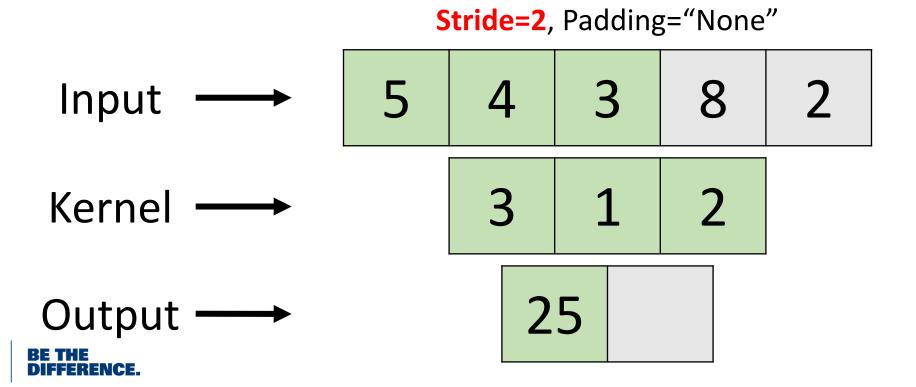
25 31 21



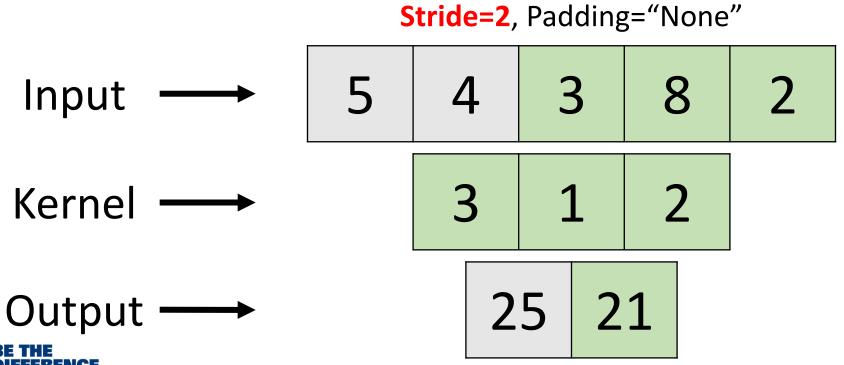
- Stride is the distance the kernel moves for each output calculation
- Padding can be used to get the desired size for the output



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- **Stride** is the distance the kernel moves for each output calculation
- Padding can be used to get the desired size for the output





- Stride is the distance the kernel moves for each output calculation
- Padding can be used to get the desired size for the output

Stride=1, Padding="Same"

Input → 0 5 4 3 8 2 0

Kernel → 3 1 2

Output → RETHE

- Stride is the distance the kernel moves for each output calculation
- Padding can be used to get the desired size for the output

Stride=1, Padding="Same"

Input → 0 5 4 3 8 2 0

Kernel → 3 1 2

Output → 13

- Stride is the distance the kernel moves for each output calculation
- Padding can be used to get the desired size for the output

Stride=1, Padding="Same"

Input → 0 5 4 3 8 2 0

Kernel → 3 1 2

Output → 13 25 31 21 26

Questions?

- 1D Convolutions
- Stride
- Padding

• Up next: 2D Convolutions



Outline

- 1D Convolution
 - Stride, Padding
- 2D Convolution
 - Single channel input
 - Multiple channel input (i.e. RGB)
 - Multiple channel output
- Choosing Weights
 - Finding changes, edges, peaks, features, etc.
- Pooling Layers

- Transposed Convolutions
 - 1D
 - 2D
 - Stride, padding
 - Multiple channel input
 - Multiple channel output
- U-Net Architecture
 - Post-processing images

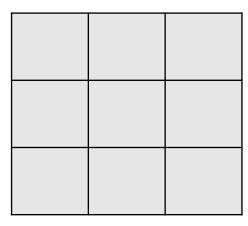


Input

Kernel

5	4	3	8	2
8	1	2	4	1
1	7	3	2	6
2	4	0	1	4
3	1	7	3	2

1	0	1
0	2	1
0	0	2





Input

5	4	3	8	2
8	1	2	4	1
1	7	3	2	6
2	4	0	1	4
3	1	7	3	2

Kernel

1	0	1
0	2	1
0	0	2

18	

$$(5*1) + (4*0) + (3*1) + \cdots$$

$$(8*0) + (1*2) + (2*1) + \cdots$$

$$(1*0) + (7*0) + (3*2) = 18$$

Input

5	4	3	8	2
8	1	2	4	1
1	7	3	2	6
2	4	0	1	4
3	1	7	3	2

Kernel

1	0	1
0	2	1
0	0	2

$$(4*1) + (3*0) + (8*1) + \cdots$$

 $(1*0) + (2*2) + (4*1) + \cdots$
 $(7*0) + (3*0) + (2*2) = 24$



Input

5	4	3	8	2
8	1	2	4	1
1	7	3	2	6
2	4	0	1	4
3	1	7	3	2

Kernel

1	0	1
0	2	1
0	0	2

$$(3*1) + (2*0) + (6*1) + \cdots$$

$$(0*0) + (1*2) + (4*1) + \cdots$$

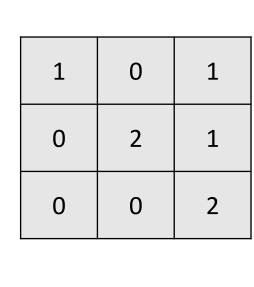
$$(7*0) + (3*0) + (2*2) = 19$$

• Again, stride and padding can be used to manipulate output size

Input

5	4	3	8	2
8	1	2	4	1
1	7	3	2	6
2	4	0	1	4
3	1	7	3	2

Kernel



Output

Stride=(1,1)
Padding="None"

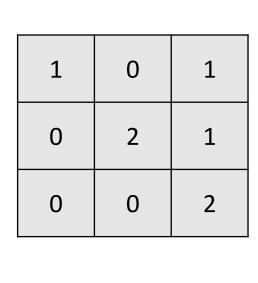
18	24	26
27	14	21
26	14	19

Again, stride and padding can be used to manipulate output size

Input

5	4	3	8	2
8	1	2	4	1
1	7	3	2	6
2	4	0	1	4
3	1	7	3	2

Kernel



Output

Padding="None"

18	26
26	19

Again, stride and padding can be used to manipulate output size

Input

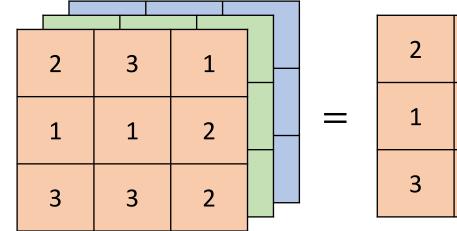
0	0	0	0	0	0	0
0	5	4	3	8	2	0
0	8	1	2	4	1	0
0	1	7	3	2	6	0
0	2	4	0	1	4	0
0	3	1	7	3	2	0
0	0	0	0	0	0	0

Kernel

1	0	1
0	2	1
0	0	2
•		

Output Stride=(1,1) Padding="Same"

- The dimension of the convolution is determined by the stride dimension, NOT the input or output dimension
- RGB images have three channels (one each for Red, Green, and Blue) and are therefor 3D arrays. Still, 2D convolutions are used



2	3	1
1	1	2
3	3	2

1	0	1
0	2	1
0	0	2

2	1	3
1	2	1
1	0	0

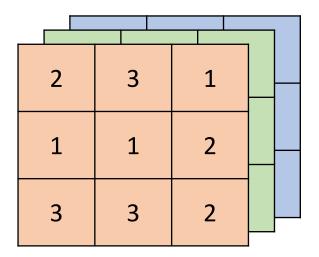


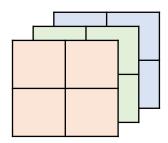
Input

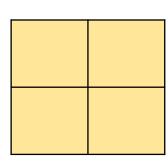
Kernel

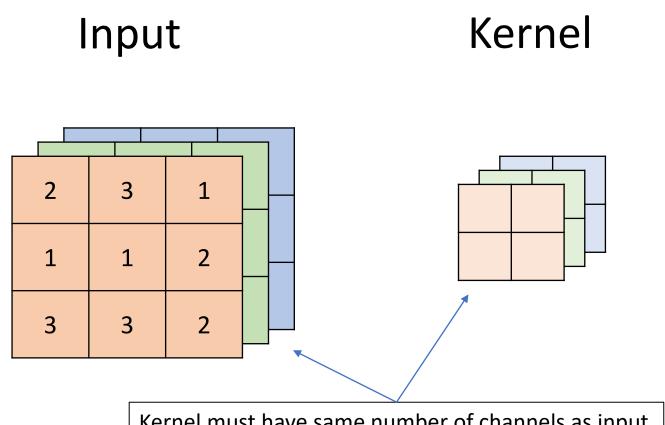
Output

Stride=(1,1)
Padding="None"



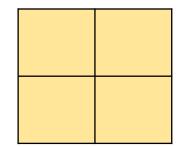






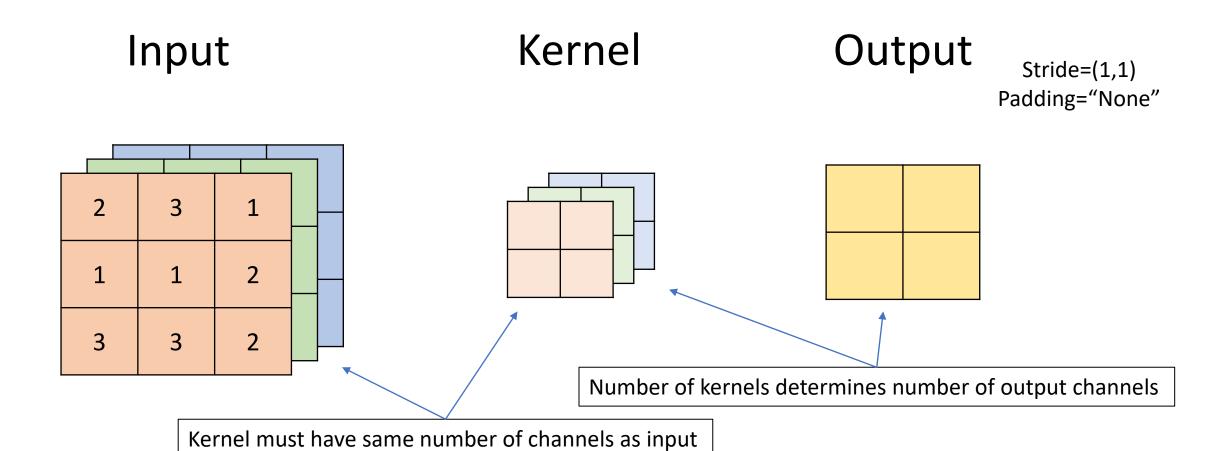
Output

Stride=(1,1) Padding="None"



Kernel must have same number of channels as input







BE THE DIFFERENCE.

Input

2	3	1
1	1	2
3	3	2

1	0	1
0	2	1
0	0	2

2	1	3
1	2	1
1	0	0

2	3	1	
1	1	2	
3	3	2	

 2
 3
 1

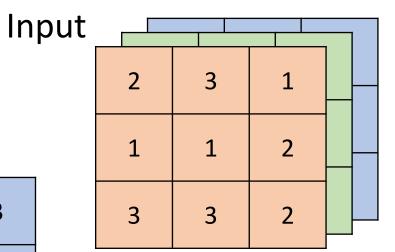
 1
 1
 2

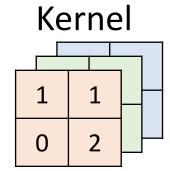
 3
 3
 2

1	0	1
0	2	1
0	0	2

1	0
1	1

1	0		(
	1	1		





 2
 3
 1

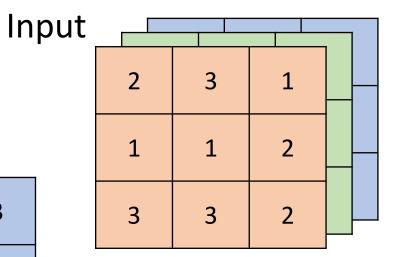
 1
 1
 2

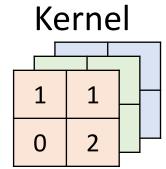
 3
 3
 2

1	0	1
0	2	1
0	0	2

1	0
1	1

1	1
2	2





7	

 2
 3
 1

 1
 1
 2

 3
 3
 2

1	0	1
0	2	1
0	0	2

1	0
1	1

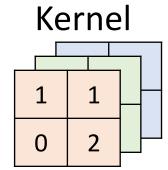
1	1	
2	2	

2	3	1		
1	1	2		
3	3	2		

Input

3

1



7	8
8	7

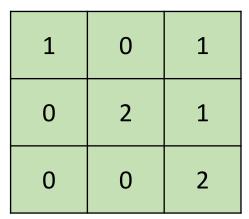
 2
 3
 1

 1
 1
 2

 3
 3
 2

1	1
0	2

7	8
8	7



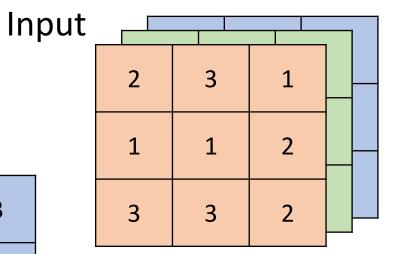
1	0
1	1

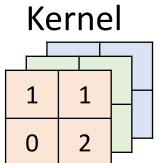
3	3
0	4

2	1	3
1	2	1
1	0	0

1	1
2	2

9	10
5	3

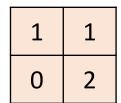




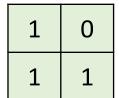
2 3 1

1	0	1
0	2	1
0	0	2

2	1	3
1	2	1
1	0	0

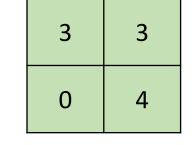


3



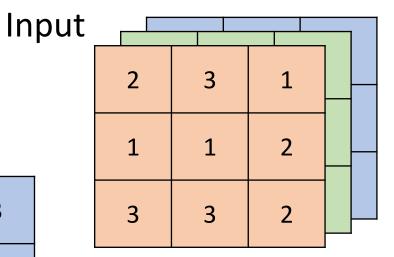
1	1
2	2

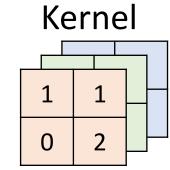
7	8
8	7



9	10
5	3

+





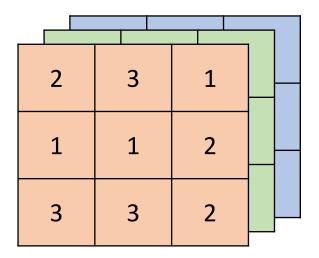
19	21
13	14

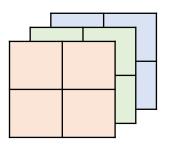
Input

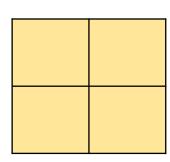
Kernel

Output

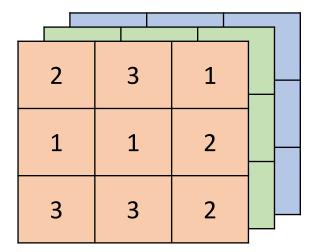
Stride=(1,1)
Padding="None"



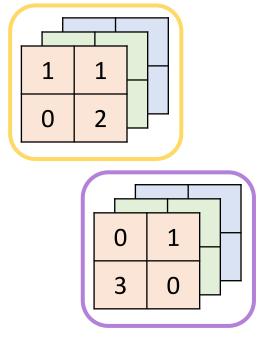




Input

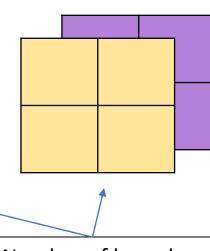


Kernel



Output

Stride=(1,1)
Padding="None"



Number of kernels determines number of output channels



Questions?

- 1D Convolutions
- 2D Convolutions
- Multiple input channels
- Multiple output channels

• Up next: Choosing weights



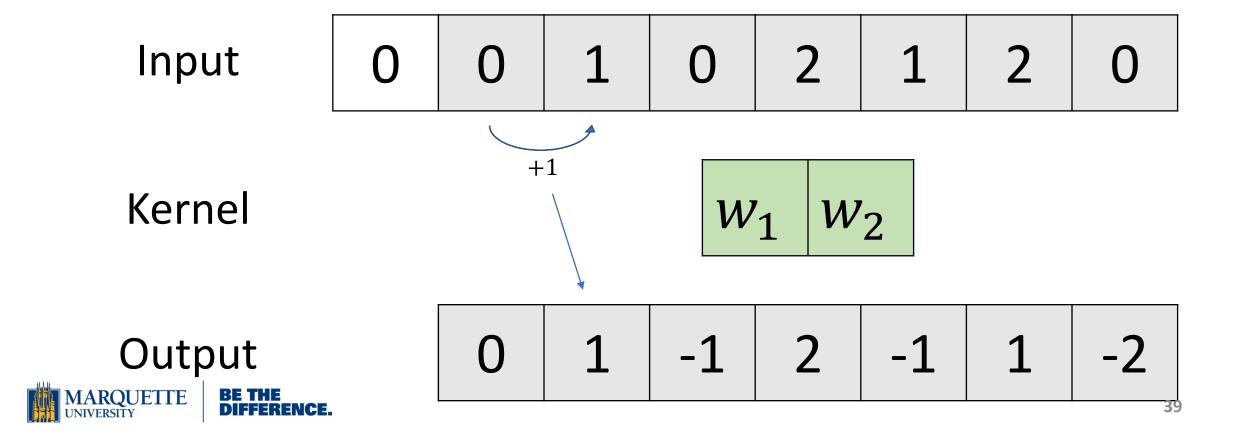
Outline

- 1D Convolution
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Can we choose a kernel so that the output is the change of the input?



• We can! Selecting $(w_1, w_2) = (-1,1)$ will output the change

Input



Kernel

J.	
MARQUETTE UNIVERSITY	BE THE DIFFERENCE.

0	1	-1	2	-1	1	-2
---	---	----	---	----	---	----

- Other kernels can be used to detect **peaks**, valleys, features, etc.
- Same idea works with multidimensional kernels
- Note that padding and stride=1 were used here

Input	0	0	1	0	2	1	2	0	0
Kernel				-1	2	-1			
Output MARQUETTE BE THE	ENCE	-1	2	-3	3	-2	3	-2	41

- So what kernels do we pick for our CNN?
- Luckily, we don't need to pick, the kernels are learned during training!

 For each convolutional layer, how many parameters need to be learned by the algorithm?

(num elements in kernel) * (num kernels) + (num kernels)

weights

biases



Questions?

- 1D Convolutions
- 2D Convolutions
- Multiple Channels
- Choosing weights to highlight features

• Up next: Pooling layers and a classification example



Outline

- 1D Convolution
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 - 2D
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 - Multiple channel output
- U-Net Architecture
 - Post-processing images



Pooling Layers

- Pooling layers reduce the resolution (height and/or width)
- Extract dominant features that are positionally invariant
- Reduce noise

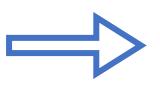
• Slide a window over the input and take the max (or mean, etc.) of the input values as the output

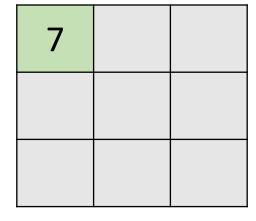
 Max pooling is typically used in CNN's because it disregards noise better than other options



Input

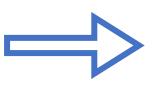
1	2	4	1
7	3	2	6
4	0	1	4
1	7	3	2





Input

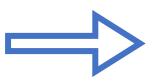
1	2	4	1
7	3	2	6
4	0	1	4
1	7	3	2



7	4	

Input

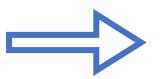
1	2	4	1
7	3	2	6
4	0	1	4
1	7	3	2



7	4	6

Input

1	2	4	1
7	3	2	6
4	0	1	4
1	7	3	2



7	4	6
7	3	6
7	7	4

- Pooling layers are defined by kernel size and stride
- There are no learned parameters in a pooling layer

Input

Output

Kernel Size=(2,2) Stride=(1,1)

1	2	4	1
7	3	2	6
4	0	1	4
1	7	3	2

7	4	6
7	3	6
7	7	4

Questions?

- 1D Convolutions
- 2D Convolutions
- Multiple Channels
- Choosing weights to highlight features
- Max Pooling

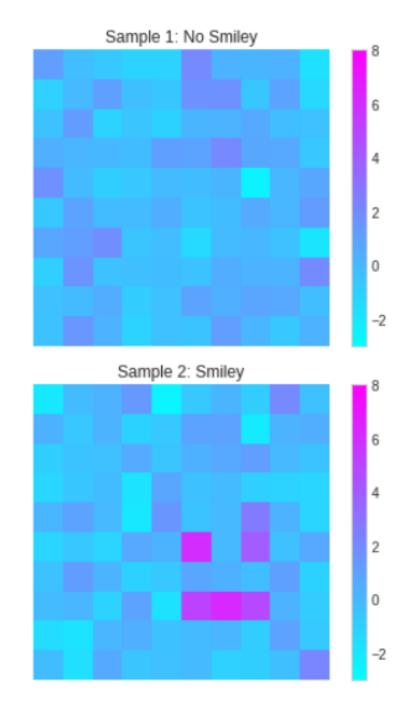
• Up next: Classification Example in Google Colab



Classification Example

- Network Architecture
 - Input Layer
 - Convolutional Layer
 - 1 kernel
 - Pooling Layer
 - Output Layer

- Sigmoid Activation
- Binary Cross Entropy



Outline

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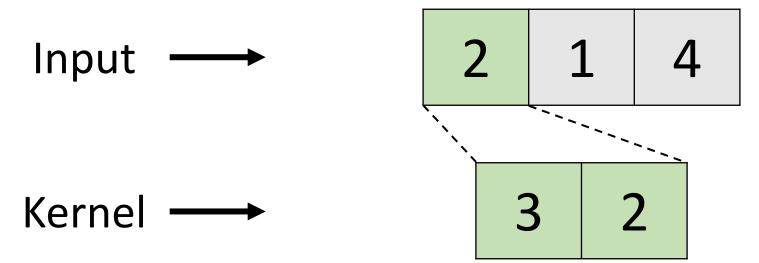
Transposed Convolutions

- 1D
- 2D
- Stride, padding
- Multiple channel input
- Multiple channel output
- U-Net Architecture
 - Post-processing images



- Also called backwards convolution or deconvolution among other things (transposed makes the most sense in my opinion)
- A form of up sampling
- Increases the resolution (height and width) of the input
 - Kernel size, stride, and padding help manage output sizes
- Usually used while decreasing the number of channels



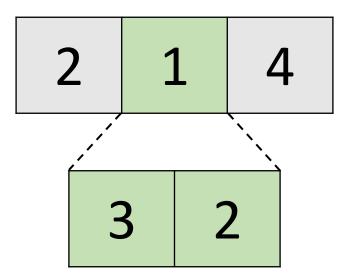


$$(2*3) = 6$$
 $(2*2) = 4$



Input ---

Kernel →



$$(1*3) = 3$$

$$(1*3) = 3$$
 $(1*2) = 2$

Output ----

6 4+3

Input — 2 1

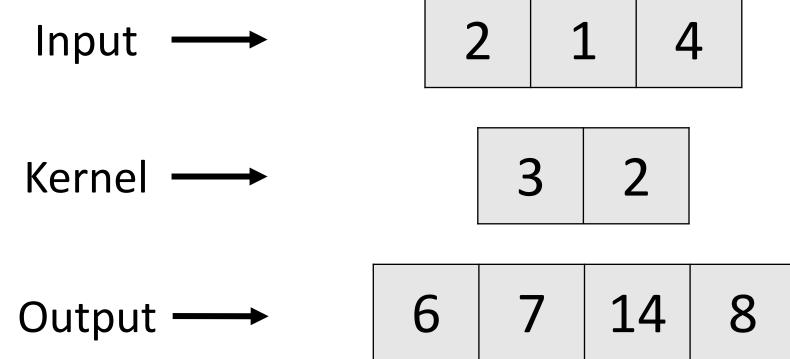
Kernel →

$$(4*3) = 12$$
 $(4*2) = 8$

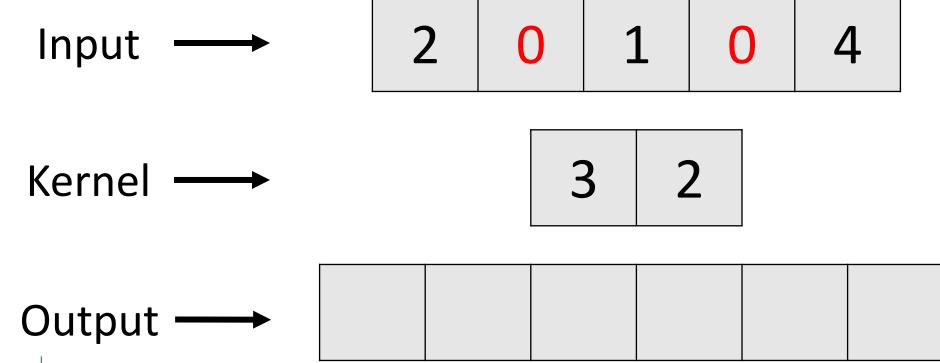
2+12

Output — 6 4+3

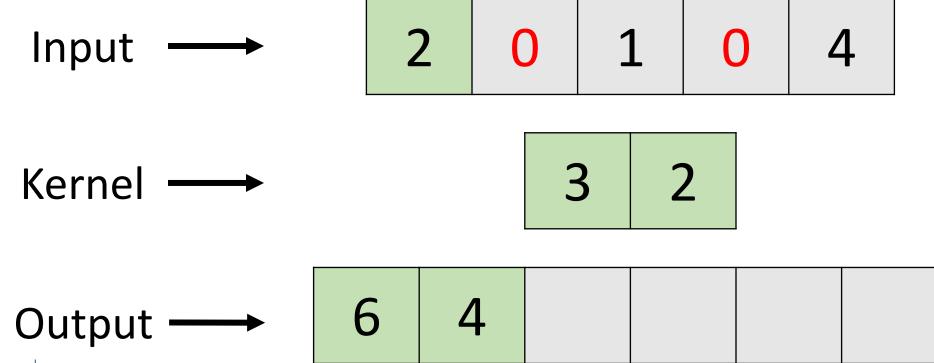
This example used a stride of 1 and no padding



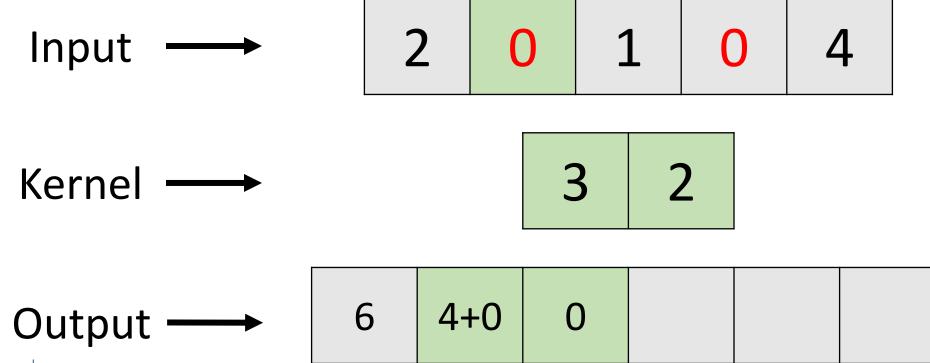




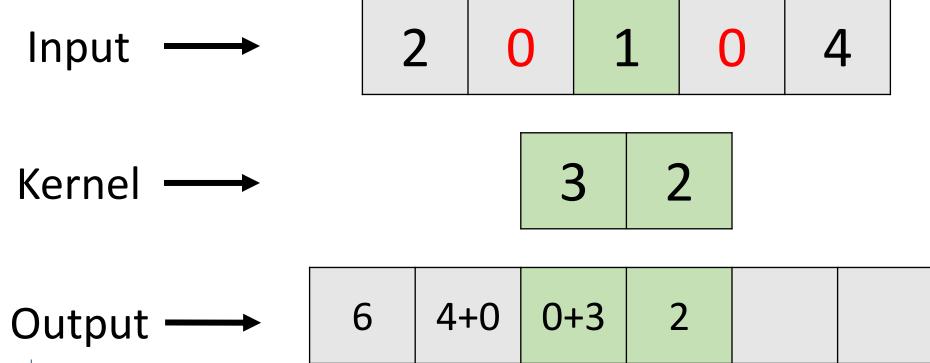




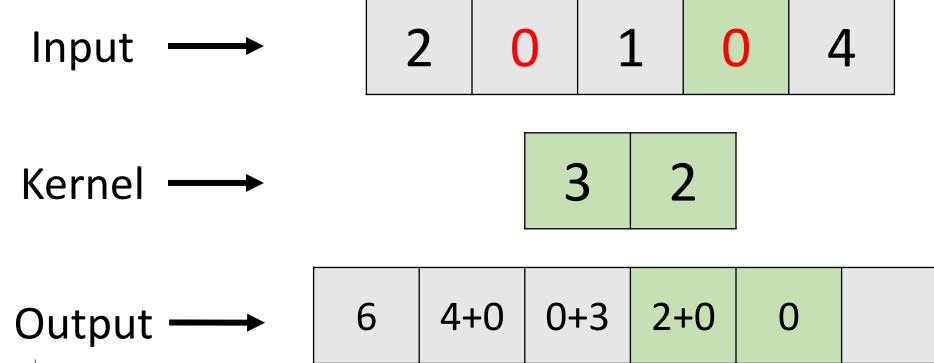




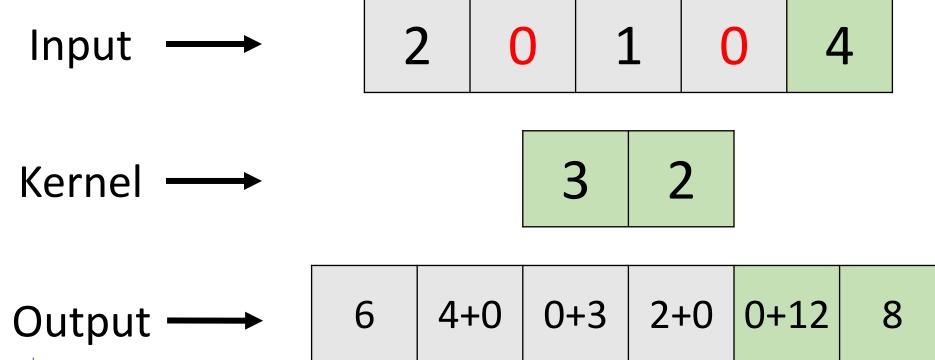




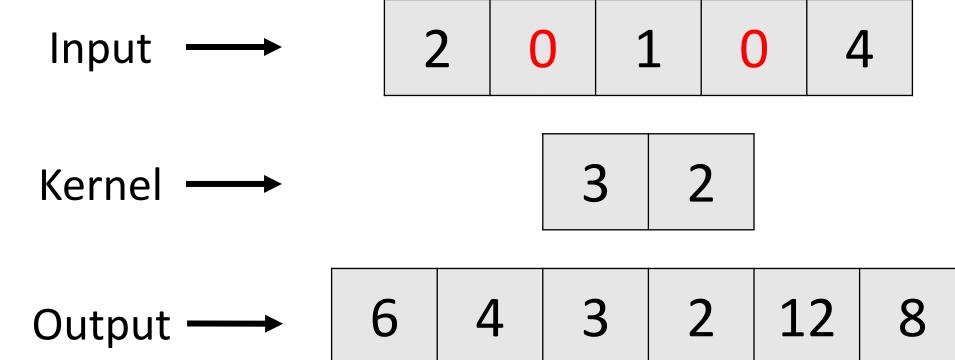






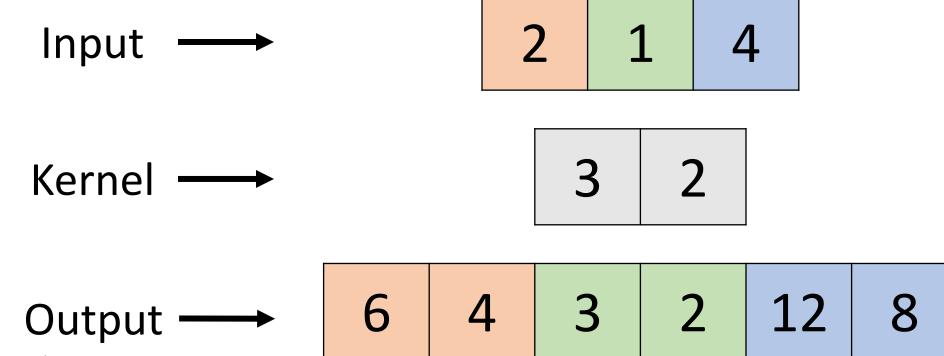


 Padding the input with 0's has the same effect as adding a stride to the output





 Padding the input with 0's has the same effect as adding a stride to the output (stride=2)





Questions?

- 1D Convolutions
- 2D Convolutions
- Multiple Channels
- Choosing weights to highlight features
- 1D Transposed Convolutions

Up next: 2D Transposed Convolutions



- Again, 2D refers to the dimension of the stride parameter
- Padding between input entries with zeros or adjusting the stride of the output work with 2D transposed convolutions too



• Example with no padding (output stride = (1,1))

Input

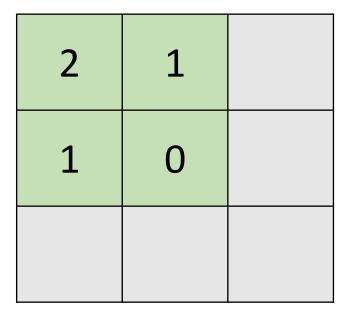
Kernel

Output

 1
 2

 3
 4

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• Example with no padding (output stride = (1,1))

Input

Kernel

Output

1 2

3 | 4

2 1

1 | 0

2	1+2	2
1	0+2	0

• Example with no padding (output stride = (1,1))

Input

Kernel

Output

1234

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2	1+2	2
1+6	0+2+3	0
3	0	

• Example with no padding (output stride = (1,1))

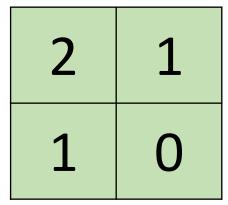
Input

Kernel

Output

 1
 2

 3
 4



2	1+2	2
1+6	0+2+ 3+8	0+4
3	0+4	0

• Example with no padding (output stride = (1,1))

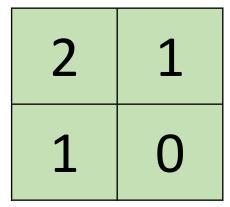
Input

Kernel

Output

 1
 2

 3
 4



2	3	2
7	13	4
3	4	0



• The stride of (1,1) resulted in overlap in the orange output entries

Input Kernel Output

1 2 1 7 13 4 1 0 3 4 0



These mean the same thing. It's not two separate things being done; it's two ways of thinking of the same thing

• Example with padding (output stride = (2,2))

Input

Kernel

Output

1	0	2
0	0	0
3	0	4

2	1
1	0

2	1	4	2
1	0	2	0
6	3	8	4
3	0	4	0



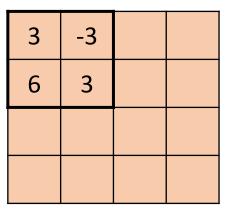
Input

3	1
-1	2

Kernel

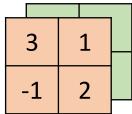
1	-1
2	1

Output

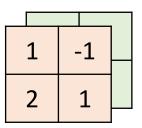


1	1
2	1

Input



Kernel



Input

3	1
-1	2

-1 | 2

Kernel

1	-1
2	1

Output

3	-3	1	-1
6	3	2	1
-1	1	2	-2
-2	-1	4	2

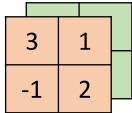
+

1	1
2	1

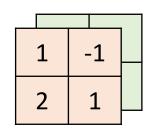
1 0 -1 -1

1	0	1	0
-1	-1	-1	-1
2	0	1	0
-2	-2	-1	-1

Input



Kernel

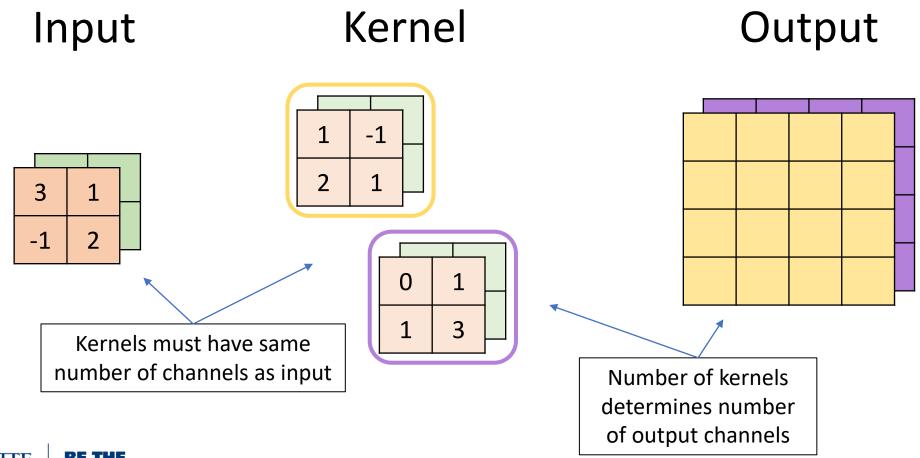


Output

4	-3	2	-1
5	2	1	0
1	1	3	-2
-4	-3	3	1









Transposed Convolution Layer

 For each transposed convolutional layer, how many parameters need to be learned by the algorithm?

(num elements in kernel) * (num kernels) + (num kernels)

weights

biases



Questions?

- 1D Convolutions
- 2D Convolutions
- Multiple Channels
- Choosing weights to highlight features
- 1D Transposed Convolutions
- 2D Transposed Convolutions
- Up next: U-Net Architecture for post processing images



Outline

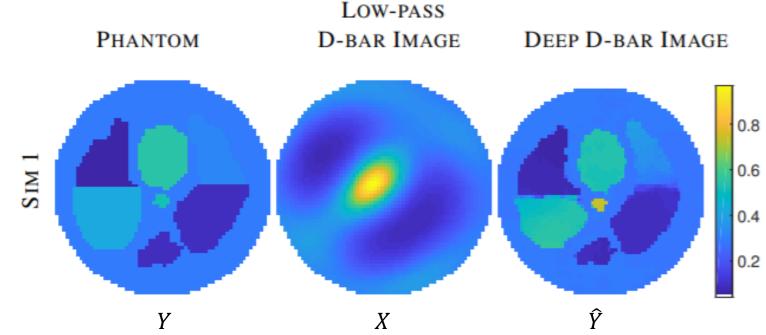
- 1D Convolution
 - Stride, Padding
- 2D Convolution
 - Single channel input
 - Multiple channel input (i.e. RGB)
 - Multiple channels on output
- Choosing Weights
 - Finding changes, edges, peaks, features, etc.
- Pooling Layers

- Transposed Convolutions
 - 1D
 - 2D
 - Stride, padding
 - Multiple channel input
 - Multiple channel output
- U-Net Architecture
 - Post-processing images



U-Net Architecture

- Presented by Ronneberger et al. in 2015 for image segmentation
- Shown to sharpen EIT D-bar reconstructions by Hamilton and Hauptmann in 2018





U-Net Architecture

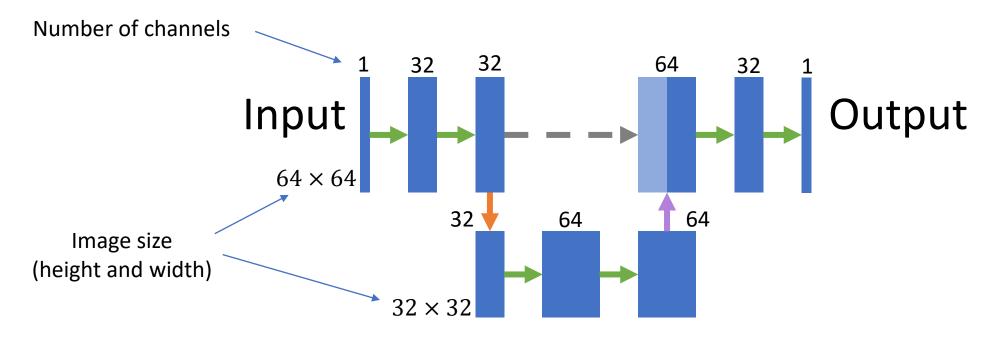
- Contracting path (left) identifies features
- Expanding path (right) offers localization

Convolution

→ Max Pool

Transpose Convolution

Concatenation





U-Net Architecture

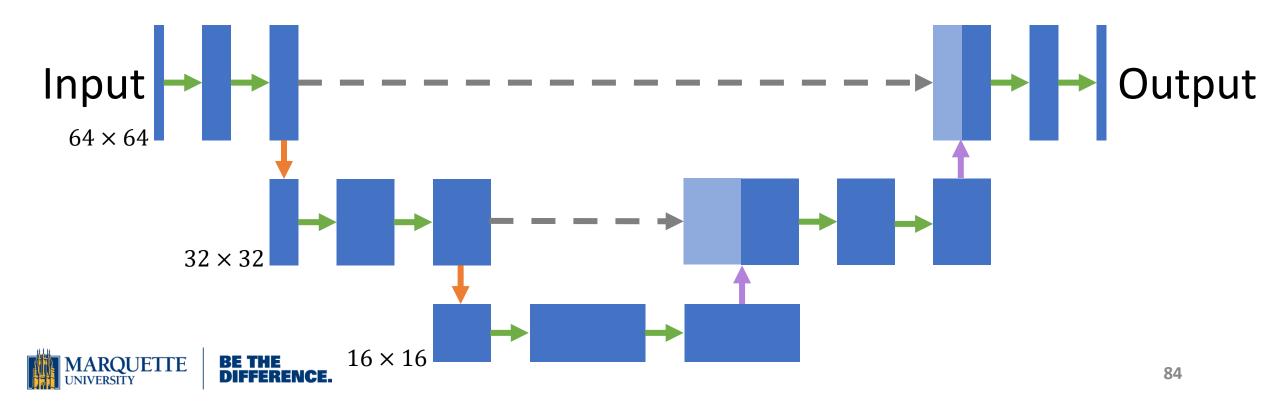
- Contracting path (left) identifies features
- Expanding path (right) offers localization

Convolution

→ Max Pool

Transpose Convolution

Concatenation



Questions?

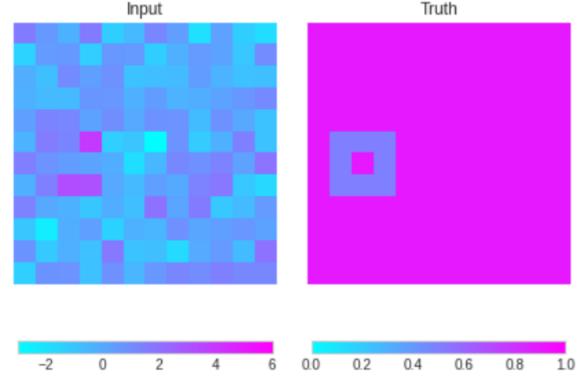
- 1D Convolutions
- 2D Convolutions
- Multiple Channels
- Choosing weights to highlight features
- 1D Transposed Convolutions
- 2D Transposed Convolutions
- U-Net Architecture
- Up next: U-Net Example in Google Colab



U-Net Example

- Input is a blurry image with (or without) a smiley face
- Truth is an image with a ring (or without) and no noise

- Network
 - U-Net
 - 1 Max Pool Layer
 - MSE loss function
 - ReLU activation





Why use CNNs? (as opposed to dense networks)

- Number of weights is not related to the image sizes
 - Could have used 500x500 smiley face images

- Feature learning
 - By the end of training, the classifier knew what features to look for
- Spatially invariant
 - Can detect a smiley face in any location

Thank You!

Questions?

