Automated Multi-Objective Design Optimization of PM AC Machines Using Computationally Efficient FEA and Differential Evolution

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Abstract—The design optimization methods described in this paper are employing an ultrafast computationally efficient finite element analysis technique. A minimum number of magnetostatic solutions are used for the analysis, which makes possible the study of thousands of candidate motor designs with typical PC-workstation computational resources. A multi-objective differential evolution algorithm that considers a large number of independent stator and rotor geometric variables and performance criteria, such as average and ripple torque, losses, and efficiency, is used. The optimization method is demonstrated on different permanent magnet (PM) ac synchronous motors in the kilowatt and megawatt power ranges. For the low-power PM ac machine study, a nine-slot six-pole topology is considered. For the high-power PM ac machines, four case studies were carried out with the following: fractional-slot embedded surface PM (SPM), fractionalslot interior PM (IPM), integer-slot SPM, and integer-slot IPM, respectively. Four motor topologies are systematically compared based on optimal Pareto sets. The design optimization of IPM motors includes an additional search for an optimum operating torque angle corresponding to the maximum-torque-per-ampere condition.

Index Terms—Design optimization, electromagnetic analysis, electromagnetic modeling, finite-element methods, permanent-magnet (PM) machines, PM motors, synchronous machines.

I. INTRODUCTION

THE DESIGN of electric machinery is complicated by the usually large number of design variables related to complex geometries and material properties. In addition, the designer is often confronted by a large number of conflicting design objectives that further complicate the design process.

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In a typical design flow, initial device sizing is performed using analytical and magnetic equivalent circuit models, and finite element analysis (FEA) is used in the final steps of the design process for verification and parameter fine-tuning. In this approach, several iterations may be performed to satisfy a limited number of objectives. Furthermore, a majority of the design variables are predetermined based on the analytically derived models, and then, a small number of variables are finetuned using FEA. In this approach, only a small number of variables are varied using FEA, and the optimality of the final design is not guaranteed. On the other hand, a design process that relies solely on conventional FEA models to investigate a large number of candidate designs may be inadequate due to the prohibitively long computer execution times. This limitation of FEA-based models has prevented their application in largescale design optimization studies, where a significant number of design parameters are varied in the search for optimum designs.

Recent developments in the area of FEA-based evolutionary design synthesis and optimization were reviewed by Duan and Ionel [1] and can be classified into two distinct classes, the methods that consider complete transient solutions and rely on advanced computing facilities proposed by Jiang *et al.* [2] and the methods that rely on reduced-effort models in order to estimate machine performance during the iterative search. Examples of the latter include the work of Parasiliti *et al.* [3], Pellegrino and Cupertino [4], Arkadan *et al.* [5], Giurgea *et al.* [6], Sarikhani and Mohammed [7], and Ouyang *et al.* [8].

Several reduced-effort FEA modeling approaches have been proposed in the literature, e.g., [9]–[15]. These techniques aim to minimize the computational effort associated with FEA while maximizing the amount of available machine performance information. Previous methods were able to estimate the average torque and the torque ripple [9]–[11] or the stator core losses [12]. Computationally efficient FEA (CE-FEA) was introduced by the authors in [13] and [14]. In this new approach, both magnetic and electric circuit symmetries of permanent-magnet (PM) ac machines were exploited to reduce the number of required static finite element (FE) solutions. In CE-FEA, a comprehensive set of performance indices, including the induced voltage waveforms, average torque, profiles of cogging torque and torque ripple, flux density waveforms, winding inductances, and core losses, is extracted from a minimum number of magnetostatic FE solutions with a machine representation in the abc reference frame. The accuracy of

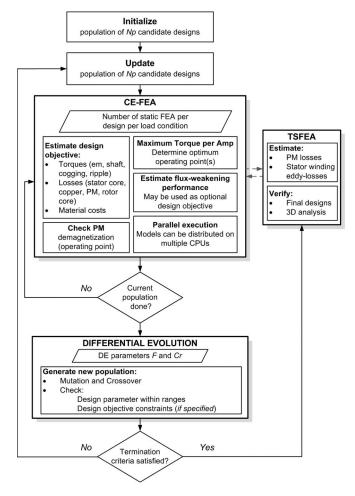


Fig. 1. Block diagram for model-based design optimization procedure employing CE-FEA and DE optimizer.

such an approach was validated by results from time-stepping (transient) FEA (TSFEA) [14], [16].

In this paper, an automated design tool that couples the CE-FEA computational method and the differential evolution (DE) optimizer [17] was developed. The method is demonstrated on two comprehensive large-scale design optimization studies that involve the evaluation of thousands of candidate designs. The first design study shows the application of the automated tool to the optimization of the existing design. This study demonstrates the possibility of torque-dense and torqueripple-free design of the interior PM (IPM) motor with three slots per pole pair. The second design study shows the application of the method to the systematic motor technology comparison where four high-power motor topologies are compared based on the optimal Pareto sets. The following four case-study machines are optimized and compared based on optimal Pareto sets: fractional-slot embedded surface PM (SPM), fractionalslot IPM (F-IPM), integer-slot embedded SPM, and integer-slot IPM (I-IPM). In both examples, a large number of stator and rotor variables are used to automatically optimize the average torque, the efficiency, and the cogging and the ripple torques.

The block diagram of the proposed model-based design optimization is shown in Fig. 1. In this figure, a DE algorithm is used to dynamically update and improve the candidate design

population, and the CE-FEA is used to extract the objectives (average and ripple torques, core losses, etc.). It should be noted that, for the case study, IPM machine parameters, such as the average electromagnetic and shaft torques, torque ripples, and efficiency, are extracted at a single load point from several magnetostatic solutions. These solutions take several seconds to execute using a typical PC-based workstation.

II. CE-FEA

The CE-FEA is applicable to the steady-state analysis of sine-wave energized current-regulated synchronous machines. In CE-FEA, a static nonlinear finite-element solver is utilized, and significant computational savings are obtained by utilizing additional symmetries of the magnetic circuit (beyond odd/even periodicity conditions) and electric circuits. The machine is analyzed/evaluated at several rotor positions with corresponding sequentially sampled phase current excitations based on the sinusoidal current waveform. Outputs such as the magnetic vector potentials, phase flux linkages, and stator core flux densities are reconstructed using the waveform symmetry conditions that stem from the magnetic and electric circuit symmetries. The corresponding Fourier series of the reconstructed quantities are obtained paying special attention to possible aliasing effects [14]. As a result, using the CE-FEA, performance parameters such as the back-EMF waveforms, average torque, profiles of cogging torque and torque ripples, and stator core losses can be extracted from a minimum number of magnetostatic FE solutions. This leads to a significant reduction of execution times when compared to the laborious TSFEA approaches while preserving the main benefits of FE solvers, i.e., accuracy of geometric shape and magnetic saturation representations. For example, to evaluate a candidate motor at a single operating condition, CE-FEA requires as few as three magnetostatic solutions (three rotor positions) for average torque and six solutions (six rotor positions) for *detailed* analysis that includes terminal voltage, torque ripple, and accurate core loss calculation [14].

In the present CE-FEA framework, additional loss components can be estimated using a combination of analytical and numerical methods. Eddy-current induced PM losses [18] and stator conductor induced eddy-current losses [19], [20] can be accounted for by means of analytical and/or numerical models. Meanwhile, the core losses and PM losses caused by the inverter/drive switching can be implemented into the CE-FEA utilizing the method presented in [21]. In the block diagram of the present model-based optimization procedure, the TSFEA can be used to estimate the eddy-current induced losses in both PMs and stator coils. After optimal designs are selected, a detailed TSFE analysis that accounts for additional loss components due to the inverter switching, not accounted for in the CE-FEA, should be performed. Further TSFE analysis may include the simulation of the effects of induced eddy currents in the lamination steel on the overall field distribution in the machine, as discussed in [22]. In addition, TSFEAbased numerical models can be used in selecting the appropriate circumferential and axial PM segmentations that will minimize induced eddy-current magnet losses.

While (convergence criteria are not satisfied)

For (every population member)
choose random members,
$$\mathbf{x_{r0}}$$
, $\mathbf{x_{r1}}$, and $\mathbf{x_{r2}}$

Generate a trial member
(crossover and mutation)
$$u_i = \begin{cases} x_{r0} + F(x_{r1} - x_{r2}), & \text{if } (\text{rand}(0, 1) \leq C_r) \\ x_i \end{cases}$$
End
For (every population member)

Select the new generation member
(if it outperforms the existing)
$$\mathbf{x} = \begin{cases} \mathbf{u}, & \text{if } (f(\mathbf{u}) \leq f(\mathbf{x})) \\ \mathbf{x} \end{cases}$$
End
End

Fig. 2. Simplified pseudocode of DE implementation for a single-objective minimization problem.

III. DESIGN OPTIMIZATION

A. Optimum Operating Point (MTPA)

The design optimization of IPM machines is complicated by the fact that the maximum torque production is a function of the advance angle of the current, which, in turn, is a function of the design parameters. This means that, for a systematic comparison of candidate designs, an additional search/optimization of the optimum operating point [maximum torque per ampere (MTPA)] has to be performed for every candidate design. The determination of the MTPA operating condition requires additional model iterations to obtain the optimum operating condition, hence increasing the execution time. This, however, is not of significant concern with CE-FEA, where several static FE solutions are sufficient for the estimation of the average torque [14].

B. DE Optimization Algorithm

The DE algorithm belongs to the wide class of metaheuristic optimizers that attempts to find a global minimum/maximum by iteratively improving a population of candidate designs until the convergence criteria are satisfied [17]. The differential part of the DE algorithm implies that, unlike other derivative-free population-based evolutionary algorithms (genetic algorithms, particle swarms, simulated annealing, etc.), DE utilizes a weighted difference between candidate designs to facilitate the improvement of future generations. The DE approach has been shown to outperform most population-based evolutionary algorithms on a number of benchmark test functions [1], [17].

In DE's most basic form (see Fig. 2), the parameters u_i of the new trial member \mathbf{u} are updated based on mutation and crossover ideas given in the following:

$$u_i = \begin{cases} [x_{r0} + F(x_{r1} - x_{r2})] & \text{if } (rand(0, 1)) \le C_r \\ x_i & \end{cases}$$
 (1)

where x_i is the parameter of the present population member and $[x_{r0} + F(x_{r1} - x_{r2})]$ is the mutation operation applied to the parameters of the three randomly selected present population members, x_{r0} , x_{r1} , and x_{r2} , with F being a positive real differ-

ence scale factor. The mutation operation is carried out only if the following crossover condition is satisfied: $\operatorname{rand}(0,1) \leq C_r$, where C_r is a predefined crossover probability. Once the trial member \mathbf{u} is created, its objective function $f(\mathbf{u})$ is evaluated and compared to the objective function of the present member $f(\mathbf{x})$. The trial vector \mathbf{u} is allowed to enter the population only if it outperforms the present member \mathbf{x} . The population size is heuristically chosen to be ten times the number of design variables [17].

There are two approaches to multi-objective optimization. The most straightforward approach is based on a weighted sum of objectives that transforms a multi-objective problem into a simple single-objective case, as given in

$$f_1 = \sum_{n=1}^{N} w_n f_n(\mathbf{x}). \tag{2}$$

However, in this approach, a choice of weights w_n may have a significant impact on the optimality of the final design. Moreover, the dual nature of some objectives (conflicting/nonconflicting) may lead to problems with proper weight assignment. For a given set of weights, this approach leads to a single optimal design that either maximizes or minimizes the objective function given in (2). The second approach to multi-objective optimization problems, used in this work, is based on the Pareto-dominance selection criteria. This approach typically results in the family of the best compromise designs that provide the designer with a clear view of various tradeoffs between a number of Pareto-optimal designs. Pareto-dominance selection criteria can be incorporated into the DE using several approaches outlined in [17] and [23].

C. Problem Statement

The multi-objective definition of the PM ac machine design used in this paper can be summarized as follows:

- minimize torque ripple and total losses (core and copper), while
- maximizing the torque production per unit volume at rated load.

One way to achieve this is by considering two objectives given by the following:

$$minimize: f_1 = T_{em(pk-pk)},$$

$$maximize: f_2 = \frac{T_{em}}{\sqrt{P_{Cu} + P_{Fe}}}$$
(3)

where f_1 corresponds to the peak-to-peak torque ripple and f_2 corresponds to "goodness," which is a measure of average torque production with respect to total losses. The outside diameter and axial length are fixed during the optimization. The axial length is then scaled to achieve the desired output ratings of different optimized machine designs. The current density and slot fill are fixed, respectively. Every candidate design for these IPM machines is evaluated at MTPA condition. The PM material and steel used in the core construction are fixed. A purely sinusoidal current-regulated sine-wave drive is assumed to be energizing such machines.

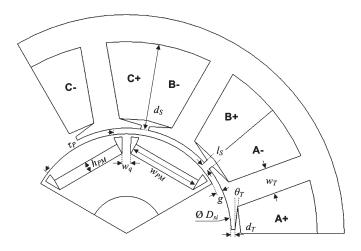


Fig. 3. Cross section of the 9-slot 6-pole IPM machine with 11 independent geometric variables used in multi-objective optimization.

TABLE I
EXPERIMENTAL RESULTS USED FOR VALIDATION AND CALIBRATION OF
THE COMPUTATIONAL MODEL

Speed		Torque	Current	Copper	Core
		[Nm]	$[A_{rms}]$	Loss [W]	Loss [W]
	Exp.	7.4	8.1	49.9	49.6
1800	Calc.	7.5	8.1	50.9	45.9
r/min	Exp.	14.7	15.7	187.4	55.4
	Calc.	15.0	15.7	191.2	52.2
	Exp.	7.4	8.6	56.3	147.6
3600	Calc.	7.5	8.6	57.4	140.8
r/min	Exp.	14.6	16.3	201.9	178.1
	Calc.	15.0	16.3	206.1	167.2

IV. CASE STUDY 1: LOW-POWER IPM MACHINE (9-SLOT, 6-POLE)

A. Problem Statement

In this section, an optimization study of the IPM machine with fractional-slot ($q=0.5~{\rm slots/pole/phase}$) shown in Fig. 3 is discussed. As a preliminary step, the numerical analysis model was validated against experimental data for a prototype motor, which is referenced in the following as a "typical design." Satisfactory agreement was noted for various load conditions, as exemplified in Table I.

The machine has been optimized following the procedure outlined in Sections II and III, with design parameter limits set to the values provided in Table II. The population size of a single generation was set to 100, and the DE algorithm was executed for 100 generations. These settings resulted in the total of 10000 candidate design evaluations. In the CE-FEA, six magnetostatic FE solutions are used to perform a detailed evaluation of every candidate motor operating at MTPA load condition. Additional search for MTPA operating condition is performed on every candidate design requiring four additional reduced CE-FEA evaluations with three static solutions each. Reduced CE-FEA with three static solutions per torque (advance) angle allows to rapidly estimate average torque [14] while ignoring torque ripple and bypassing costly postprocessing associated with flux density computations that require additional computational effort. The total simulation time required for the evaluation of 10000 candidate designs on a

TABLE II
OPTIMIZATION PARAMETERS: LIMITS AND VALUES CORRESPONDING TO
MACHINE OF FIG. 5. VALUES ARE PER UNIT OF POLE-PITCH ARC
LENGTH, AND THE UNIT FOR ANGLE IS MECHANICAL DEGREE

Optii	nized	Fractional-slot (9-slot, 6-pole)							
Parar	neters	Lin	nits		Machine				
7-stator	, 4-rotor	Lower	Upper	M-1	M-2	M-3	Тур.		
	D_{si}	1.940	2.156	1.941	1.941	1.965	1.979		
	\overline{g}	0.027	0.069	0.028	0.040	0.062	0.034		
	$\overline{w_T}$	0.213	0.355	0.266	0.266	0.253	0.284		
Stator	l_s	0.062	0.275	0.072	0.070	0.084	0.156		
	d_s	0.550	0.824	0.801	0.820	0.815	0.742		
	$\overline{d_T}$	0.029	0.048	0.028	0.036	0.036	0.038		
	θ_T	7.50	30.00	9.02	8.83	12.42	18.75		
	w_{PM}	0.550	0.687	0.661	0.683	0.686	0.687		
Rotor	h_{PM}	0.055	0.103	0.099	0.102	0.103	0.079		
	$\overline{\tau_P}$	0.548	0.940	0.641	0.627	0.600	0.778		
	$\overline{w_q}$	0.027	0.096	0.092	0.091	0.072	0.062		

TABLE III

NUMBER OF MAGNETOSTATIC SOLUTIONS AND COMPUTATIONAL

TIME REQUIRED FOR EVALUATION OF A

SINGLE CANDIDATE DESIGN AT MTPA

CE-FEA	Solutions	Mesh density/Order	Computational Time [s]
Reduced	3	2384 el. / 1st	2.2
Detailed	6	2384 el. / 2nd	10.1
TOTAL	$4 \times Redu$	$ced + 1 \times Detailed$	18.9

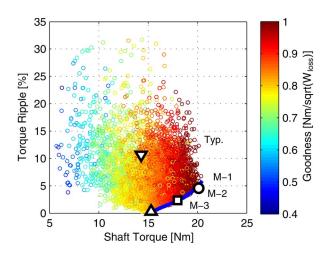


Fig. 4. Pareto-optimal set for design objectives. The three optimal machines M-1, M-2, and M-3 and the conventional machine are labeled. Shaft torque corresponds to the output torque after the core losses.

single core of the PC-based workstation is approximately 52 h. The detailed breakdown of model simulation times is provided in Table III.

Shown in Fig. 4 are the values of the design objectives specified above for 10 000 candidate designs as well as the objective function values corresponding to the final Pareto-optimal set of designs. The average shaft torque that accounts for core losses is plotted in Fig. 4 to provide a familiar basis of comparison of average and ripple torque production. From Fig. 4, it should be observed that a large variation between the torque ripple and the average torque production occurs from values as low as 0.4% to 32%, with the shaft torque varying from 6 to 21 N·m. Three Pareto-optimal machines are selected from the Pareto-optimal set, where the candidate design M-1 has the highest shaft torque (specific torque), the candidate design M-2 is a compromise between high torque and low ripple, and M-3 poses the low

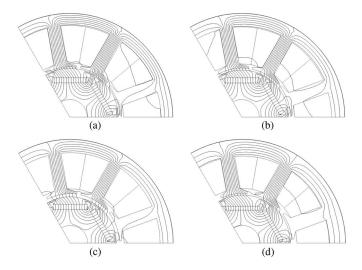


Fig. 5. Cross sections of optimized machines corresponding to Fig. 4 and Table II. Also shown are the flux plots for the rated-load conditions.

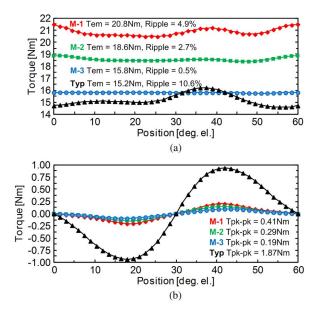


Fig. 6. Electromagnetic torque for machines of Fig. 5 (red: M-1; green: M-2; blue: M-3; black: typical design) supplied by a current-regulated sine-wave drive (purely sinusoidal currents are assumed). Torque profiles are verified/obtained using detailed FEA with Maxwell stress tensor and second-order elements.

torque ripple. Cross sections corresponding to machines M-1, M-2, and M-3 are shown in Fig. 5. Also shown in Fig. 5 is a typical design used for reference. The values of design variables corresponding to all machines are provided in Table II. Shown in Fig. 6(a) and (b) are the torque profiles corresponding to the four machines operating at rated-load (MTPA) and opencircuit (cogging torque) conditions, respectively. A significant reduction of both on-load and open-circuit ripple (cogging) is observed for the optimized designs. For machines M-1 and M-2, a significant increase in the average torque production is observed. More specifically, a 37% increase of the average torque is observed for machine M-1. From the results shown in Fig. 6(b), one observes a significant reduction of the cogging torque in the case of the optimized machines. The cogging torque is reduced by as much 90% in the case of the opti-

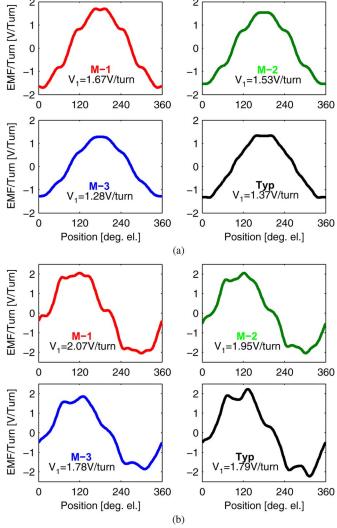


Fig. 7. Induced voltages at open-circuit and rated-load for machines in Fig. 5 (red: M-1; green: M-2; blue: M-3; black: typical design). Also shown are the peak values of the fundamental components.

mized machine M-3. It should be noted that results provided in Fig. 6 were verified with a detailed FEA that employs the Maxwell stress tensor and second-order finite elements for the calculation of the electromagnetic torque [16]. Open-circuit and rated-load induced voltages for the four machines are provided in Fig. 7, with their corresponding harmonic breakdowns given in Table IV.

B. Design to Achieve Desired Ratings of 7.5 hp (15 N·m and 3600 r/min)

Here, three optimized machines (M-1, M-2, and M-3) and the typical (conventional) machine were scaled to achieve the desired 7.5-hp output rating. The axial length l_{Fe} is used to achieve this. Given in Table V are the corresponding axial lengths in per unit (p.u.) of the pole-pitch arc length for the four machines. Also reported in Table V are the PM and total machine masses per unitized to the machine of typical proportions. As expected, machine M-1, having the highest specific torque [see Fig. 6(a)], results in the shortest and lightest machine that

TABLE IV HARMONIC ANALYSIS OF INDUCED VOLTAGES SHOWN IN FIG. 7

	Motors		Harmonic order				
		1st	5th	7th	11th	13th	
	M-1	1.67	0.098	0.10	0.002	0.020	
Open	M-2	1.53	0.091	0.87	0.005	0.002	
circuit	M-3	1.28	0.048	0.047	0.003	0.002	
[V/turn]	Тур.	1.37	0.014	0.046	0.012	0.022	
	M-1	2.07	0.245	0.131	0.020	0.032	
Rated-load	M-2	1.95	0.185	0.124	0.034	0.024	
(MTPA)	M-3	1.78	0.194	0.059	0.021	0.004	
[V/turn]	Тур.	1.79	0.316	0.038	0.042	0.013	

TABLE V

AXIAL LENGTH AND MASSES FOR 7.5-HP RATING. PER-UNIT LENGTH IS DEFINED WITH RESPECT TO THE POLE-PITCH ARC LENGTH, AND MASS VALUES ARE PER UNITIZED TO TYPICAL DESIGN [SEE FIG. 5(d)]

	M-1	M-2	M-3	Тур.
Axial length [pu]	2.08	2.33	2.73	2.85
PM mass [pu]	0.93	1.05	1.25	1.00
Total mass [pu]	0.75	0.81	0.92	1.00

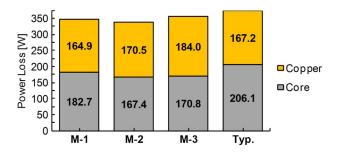


Fig. 8. Separation of loss components: Core loss (hysteresis and eddy) and copper winding loss for machines in Fig. 5.

utilizes the least PM material for the given rating. More specifically, for machine M-1, the mass of the PM material is reduced by 7% while the total machine mass and length are reduced by 25% and 23%, respectively. This is while the rated-load torque ripple and open-circuit cogging torque are reduced by 54% and 79%, respectively. This practically eliminates the need for stator and/or rotor skewing, hence reducing manufacturing costs. In the case of applications demanding higher torque production quality, further reductions of the torque ripple can be achieved with machines M-2 and M-3. Shown in Fig. 8 are the separations of loss components for the four machines. Here, it should be observed that machine M-2 results in the lowest overall loss and, hence, the highest efficiency of 94%. An almost equal split between copper and core losses for machine M-2 should also be noted, which is another indication of the "optimality" of the design from a loss point of view. Overall, machine M-2 offers the best balance between the output torque quality, efficiency, and material and manufacturing costs.

C. Discussion

The optimization results presented in this paper show several design trends that may seem unconventional. First, the optimized machines have a significant reduction, of up to an order of magnitude, of both rated-load and open-circuit (cogging) torque ripples (see Fig. 6). This is while the induced voltage

waveforms at both open-circuit and rated-load conditions are rich in their harmonic content, as can be observed from Fig. 7 and Table IV. In the optimized machines, the reduction in the torque ripple is achieved through a combination of design variables, namely, air-gap height, slot opening and tooth-tip shape (tip depth and tip angle), and the pole-arc length. In the optimized machines, these parameters result in a balance between the torque ripple produced by the back-EMF harmonics and the torque ripple resulting from the position-dependent variation of the stored magnetic energy as discussed in [14]. It should be noted that significant reduction of torque ripple levels in the optimized machines eliminates the need for stator and/or rotor skewing. The ripple-free operation of nonskewed optimized machines can be achieved with a well-tuned sinewave current-regulated drive, capable of regulating/eliminating higher order current harmonics (5th and 7th) that may result from the back-EMF harmonics.

Second, the three optimized machines tend to have lower pole-arc coverage (0.62 average), resulting in higher PM flux concentration/focusing. As can be seen from Fig. 7, this results in an increase of the fundamental component of the induced voltage of the optimized machines. For example, for machine M-1, operating under open-circuit conditions, the induced voltage is increased by 22% in comparison to that for the machine that has a conventional pole-arc coverage of 0.78.

V. CASE STUDY 2: HIGH-POWER PM MACHINES

A. Problem Statement

In the four machines shown in Fig. 9, two stator cores, the fractional-slot with q = 0.5 and the integer-slot with q = 2, and two rotor topologies, the SPM with radial magnetization and the generic IPM with single layer and uniform/parallel magnetization, are considered. In the fractional-slot topologies, the semiclosed slot opening was preferred to enable the generalization of results to a wide range of designs and ratings. For the larger machines, the magnetic equivalent of the tooth tip shown in Fig. 9(a) and (b) can be realized, for example, by using a magnetic wedge. In the design of the machines, the outside diameter, conductor current density, frequency, and number of poles are assumed to be constant and are summarized in Table VI. The outer diameter of the machine has been fixed to a value of 3 m, while the slot fills corresponding to the integer-slot and fractional-slot topologies are equal to 35% and 40%, respectively. The rare-earth magnet remanence and relative permeability are equal to 1.14 T and 1.1, respectively. The steel assumed for the construction of both stator and rotor cores is M19-26Ga. The stator and rotor geometric design parameters and corresponding ranges used in the design process are summarized in Table VII. It should be noted that, in the case of the fractional-slot SPM and IPM machines [see Fig. 9(a) and (b)], seven and eight parameters are used for optimization, respectively, whereas in the case of the integerslot SPM and IPM machines [see Fig. 9(c) and (d)], six and seven parameters are used, respectively.

An additional search of an optimum operating point (MTPA) was performed for every IPM candidate machine design. The

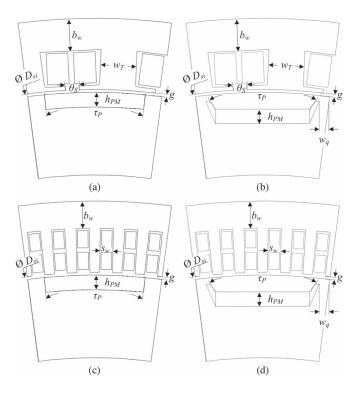


Fig. 9. Cross sections of four case-study machines, showing machine geometries. Due to the even periodicity, two poles of fractional-slot machines are modeled (a) and (b), and due to the odd periodicity, only a single pole of integer-slot machines is modeled (c) and (d).

	Fractional-slot	Integer-slot
Number of slots	36	144
Number of poles	24	24
Rated frequency [Hz]	30	30
Stator outer diameter, D_{so} [mm]	3000	3000
Current density $[A_{rms}/mm^2]$	4.05	4.65

TABLE VII
INDEPENDENT DESIGN VARIABLES AND LIMITS FOR THE
CASE STUDY 2 OF FIG. 9

	Fractional-slot		Intege	er-slot
	min	max	min	max
Stator inner diameter, D_{si} [mm]	2500	2650	2500	2650
Air-gap height, g [mm]	4	10	4	10
Tooth width, w_T [mm]	50	125	N/A	N/A
Slot width, w_S [mm]	N/A	N/A	15	45
Back iron width, w_B [mm]	110	150	25	100
Slot opening, θ_S [deg. mech.]	0.5	4	N/A	N/A
	SI	PM	IP	M
Pole arc angle, τ_P [deg. el.]	110	170	110	150
PM height, h_{PM} [mm]	15	60	15	50
q-axis bridge, w_q [mm]	60	70	N/A	N/A

four topologies shown in Fig. 9 were evaluated with 5000 candidate designs each, resulting in a total of 20 000 candidate machine design evaluations. The total simulation time on a typical PC workstation utilizing a single core was equal to a very reasonable 124 h. The detailed breakdown of model simulation times is provided in Table VIII. It should be noted that further reduction of the simulation time is achievable by evaluating CE-FEA candidate design models in parallel on multiple cores.

TABLE VIII

Number of Magnetostatic Solutions and Computational Time
Required for Evaluation of a Single Candidate Design
(Including MTPA Search for IPMs)

Fractiona	l-slot SPM		
CE-FEA	Solutions	Mesh density/Order	Computational Time [s]
Detailed	7	2991 el. / 2nd	15.7
TOTAL	$1 \times Detai$	led	15.7
Fractiona	l-slot IPM		
Reduced	3	2588 el. / 1st	2.5
Detailed	7	2588 el. / 2nd	16.1
TOTAL	$4 \times Redu$	$ced + 1 \times Detailed$	26.1
Integer-sle	ot SPM		
Detailed	9	1963 el. / 2nd	19.5
TOTAL	$1 \times Detai$	led	19.5
Integer-sle	ot IPM		
Reduced	3	1852 el. / 1st	2.1
Detailed	9	1852 el. / 2nd	20.2
TOTAL	$4 \times Redu$	$ced + 1 \times Detailed$	28.6

B. Optimization Results

The optimization results of the four machine topologies (see Fig. 9) are shown in Fig. 10. Shown in Fig. 10 are the objective function values, i.e., the electromagnetic torque per unit axial length and the torque ripple at rated load, subject to parameter constraints provided in Table VII. As mentioned before, the outside stator diameter is fixed to 3 m; hence, here, the specific torque is defined as the torque per unit axial length of the machine. The objective functions corresponding to all candidate designs (20 000) are shown in Fig. 10. Also shown in Fig. 10 are the Pareto-optimal sets corresponding to every machine topology of Fig. 9.

Depicted in Fig. 11 are the evolutions of the design parameters for the fractional-slot embedded SPM machine during the course of optimization. From Fig. 11, it should be noted that, in the multi-objective optimization that results in the distributed Pareto-optimal sets, such as the ones shown in Fig. 10, the design parameters are not guaranteed to converge to constant values. This is in contrast to single-objective optimization studies where all design parameters are guaranteed to converge to constant optimal values corresponding to a single optimal machine design. As can be seen from Fig. 11, design variables converge to a bounded region of parameter values which corresponds to designs in the Pareto-optimal set.

As can be observed from the results of Fig. 10, the two objectives considered in the optimization study are conflicting. This means that the choice of an optimal machine design involves evaluating tradeoffs between the designs in the Paretooptimal set. From Fig. 10, a large variability of the specific torque, torque ripple, and "goodness" should be noted. Comparing integer-slot and fractional-slot machines, one should notice a significant increase of the specific torque for the machines with integer-slot stators. This can be explained by the fact that the fractional-slot topology used in this work has a low fundamental winding factor of 0.866. Also, as expected, fractional-slot machine designs have lower torque ripple values when compared to the integer-slot machines. On the other hand, comparison of the "goodness" of the fractional and integer-slot machines may be affected by several factors not fully accounted for in the current analysis. More specifically, fractional-slot winding machine designs may result in increased eddy-current

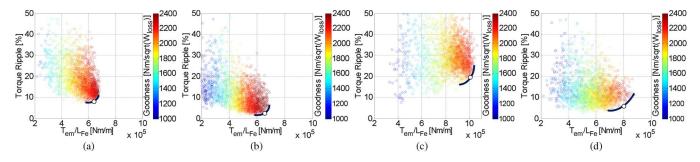


Fig. 10. Design objectives showing the following: Design objectives of all candidate designs, Pareto-optimal sets after 50 generations, and the selected optimal machines. (a) F-SPM. (b) F-IPM. (c) I-SPM. (d) I-IPM.

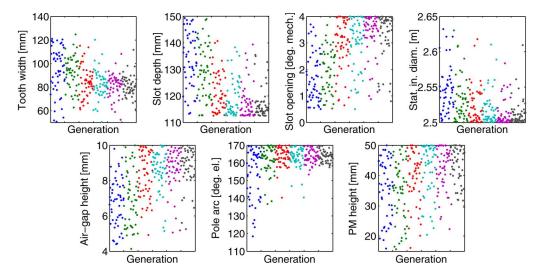


Fig. 11. Evolution of design parameters of fractional-slot embedded SPM motor during the 50 generations (only the (blue) 1^{st} , (green) 10^{th} , (eq) 20^{th} , (cyan) 30^{th} , (purple) 40^{th} , and (black) 50^{th} generations are plotted). Every point represents a candidate design parameter in the corresponding generation. Variables are not expected to converge to constant values in a multi-objective optimization.

losses in the PMs and in the stator windings due to the high harmonic content of the armature MMF. Another factor that may affect the comparison of the loss performance of the two winding topologies is the active axial length, which affects the ratio of end winding losses to the total machine losses.

Four optimal designs corresponding to every motor topology are selected from the four optimal sets shown in Fig. 10. Namely, these designs are the fractional-slot SPM (F-SPM), F-IPM, integer-slot SPM (I-SPM), and I-IPM.

The designs are selected based on the best compromise between the specific torque and the torque ripple corresponding to every Pareto-set in Fig. 10. The cross sections corresponding to the four optimal designs and the corresponding parameters are provided in Fig. 12 and Table IX. From Fig. 12(b) and (d), one should note that the nonmagnetic space at the end of the magnets was not geometrically correlated as a dependent variable of the magnet arc or length facing the air gap. It was expected that the optimization algorithm would push the magnet to the maximum allowable dimensions to a configuration that has no space at the end of the magnet as shown in Fig. 9(b) and (d).

Depicted in Fig. 13(a) and (b) are the torque profiles corresponding to the four machines operating at rated-load (MTPA) and open-circuit (cogging torque) conditions, respectively. As

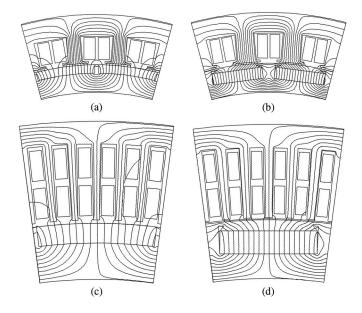


Fig. 12. Cross sections of four optimal machines, showing machine geometries and open-circuit flux distributions. Due to the even periodicity, two poles of fractional-slot machines are modeled (a) and (b), and due to the odd periodicity, only a single pole of integer-slot machines is modeled (c) and (d). The combination of (a) and (b) has a different scale with the combination of (c) and (d).

TABLE IX
OPTIMAL DESIGN PARAMETERS CORRESPONDING TO MACHINES
SHOWN IN FIG. 12

	F-SPM	F-IPM	I-SPM	I-IPM
Stator inner diameter, D_{si} [mm]	2500	2505	2501	2515
Air-gap height, g [mm]	9.0	7.1	8.8	5.6
Tooth width, w_T [mm]	76.6	96.7	N/A	N/A
Slot width, w_S [mm]	N/A	N/A	38.9	34.3
Back iron width, w_B [mm]	113.0	113.1	57.5	61.0
Slot opening, θ_S [deg. mech.]	4.0	3.85	N/A	N/A
Axial length, l_{Fe} [mm]	1953	2028	1276	1576
Pole arc angle, τ_P [deg. el.]	165.9	110.1	169.3	128.1
PM height, h_{PM} [mm]	49.7	56.4	50.5	59.7
PM height, h_w [mm]	N/A	251.2	N/A	252.5
q-axis bridge, w_q [mm]	N/A	68.9	N/A	65.2

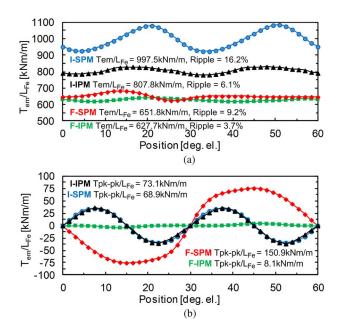


Fig. 13. Electromagnetic torque for machines of Fig. 12 (red: F-SPM; green: F-IPM; blue: I-SPM; black: I-IPM) supplied by a current-regulated sine-wave drive (purely sinusoidal currents are assumed). Torque profiles are verified/obtained using detailed FEA with Maxwell stress tensor and second-order elements.

mentioned previously, a significant increase of the specific torque is observed for the integer-slot machines (I-SPM and I-IPM). On the other hand, a significant improvement of the torque ripple is achieved with fractional-slot designs (F-SPM and F-IPM). Ripple-free operation of the optimized F-IPM machine, at both rated-load and open-circuit conditions, should be noted. The torque profiles shown in Fig. 13 were verified with a detailed FEA that employs the Maxwell stress tensor and second-order finite elements [16].

C. Design to Achieve Desired Rating of 20 MW and 150 r/min

In this section, four optimized machines (F-SPM, F-IPM, I-SPM, and I-IPM) were scaled axially to achieve the desired 20-MW output rating. The corresponding axial lengths for the four machines are provided in Table IX. Also depicted in Table X are the PM and total machine masses corresponding to the four optimal designs. As expected, I-SPM machine [see Fig. 12(c)], having the highest specific torque [see Fig. 13(a)], results in the shortest and lightest machine that utilizes the least

TABLE X
PM MASS AND TOTAL ACTIVE MACHINE MASS. PER-UNIT PM MASS OF I-SPM OPTIMAL DESIGN WITH PM MASS OF 3440 kg. PER-UNIT TOTAL MASS OF I-SPM OPTIMAL DESIGN WITH TOTAL ACTIVE MASS OF 63 467 kg

	F-SPM	F-IPM	I-SPM	I-IPM
PM mass [pu]	1.49	1.58	1.00	1.24
Total mass [pu]	1.57	1.64	1.00	1.25

PM material for the given rating. The PM mass and the total active material mass (magnet, copper, and iron) of the I-SPM design are 3440 and 63 467 kg, respectively.

D. Discussion

The optimized machines presented in this paper aim at improving torque production quality while minimizing active machine mass and losses. These objectives are oftentimes conflicting as can be observed from Fig. 10. In other words, selecting a design with high specific torque usually results in a machine with high torque ripple. In addition, selecting a design with high specific torque may result in a machine having a significantly shorter axial length, hence increasing the proportion of end winding losses in the overall total machine loss and potentially reducing the efficiency. In addition, machines with high specific torque result in smaller machines with less surface area to dissipate the losses, hence potentially requiring more sophisticated thermal management.

As shown in this paper, accurate comparison of different machine topologies should be performed on the basis of comparing their respective Pareto-optimal sets. In this approach, the variability of design objectives due to design parameters is eliminated. Hence, only optimal machines corresponding to every topology (number of slots/poles, magnet arrangement, etc.) are compared. For example, considering the fractional slot with SPM [see Fig. 10(a)] and IPM [see Fig. 10(b)] arrangements, there exists a large number of suboptimal designs that result in similar design objectives. However, comparing the Pareto-optimal sets, it is clear that the IPM design outperforms the SPM design in terms of both the specific torque and torque ripple performance.

VI. CONCLUSION

In this paper, a comprehensive FEA-based multi-objective design optimization method for PM ac machines has been presented. Two examples demonstrate that this approach, which is based on the recently developed CE-FEA technique, is well suited for large-scale design synthesis and optimization. The developed method relies solely on FEA for the calculation of relevant performance information using modest PC-based computational facilities and practically eliminates the need for using less accurate analytical and lumped parameter equivalent circuit models in automated electric machine design.

For the first case study of an F-IPM motor rated at 7.5 hp, a total of 11 stator and rotor independent design variables have been simultaneously optimized to satisfy multiple design criteria. The total simulation time for 10 000 designs, which included the search of the MTPA condition for every candidate

design, was 52 h on a typical PC-based workstation. In the second case study, four integral megawatt direct-drive machines, namely, fractional-slot embedded SPM, fractional-slot IPM, integer-slot embedded SPM, and integer-slot IPM, with a total of 20 000 candidate machine designs have been evaluated in 124 h with the same hardware and software setup.

Results presented in this paper highlight the conflicting nature of typical design objectives (torque density, torque ripple, and efficiency). In addition, results presented in this paper show that torque-dense and low-torque-ripple motors can be designed using automated design tools such as the one introduced by the authors.

The Pareto-optimal design sets derived through a DE algorithm can serve as a basis for quantitatively analyzing the tradeoffs specific to multi-objective optimization. The first case study has interestingly showed that an optimal design with high efficiency and virtually zero torque ripple can be achieved even for an F-IPM topology with three slots per pole pair. In the second case study, different machine topologies were systematically compared in terms of specific torque output, torque ripple, and cost, leading to an optimal selection.

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