

Trefethen p15 to p27.

This notebook showcases the second thirteen problems in Trefethen's classic book *Spectral Methods in MATLAB*. These problems have been ported to Python by Praveen Chandrashekar. Later problems in the set will have been ported to Python by Orlando Camargo Rodríguez.

Program 15 : Solve eigenvalue BVP

```
In [38]: 1 %matplotlib inline
2 %config InlineBackend.figure_format='svg'
3 from numpy import dot,argsort,linspace,shape,zeros,polyval,polyfit,pi,real
4 #from chebPy import cheb
5 from scipy.linalg import solve,eig
6 from matplotlib.pyplot import figure,subplot,plot,title,axis
7
```

```
In [2]: 1 from numpy import pi,cos,arange,ones,tile,dot,eye,diag
2
3 def cheb(N):
4     '''Chebushev polynomial differentiation matrix.
5     Ref.: Trefethen's 'Spectral Methods in MATLAB' book.
6     '''
7     x = cos(pi*arange(0,N+1)/N)
8     if N%2 == 0:
9         x[N//2] = 0.0 # only when N is even!
10    c = ones(N+1); c[0] = 2.0; c[N] = 2.0
11    c = c * (-1.0)**arange(0,N+1)
12    c = c.reshape(N+1,1)
13    X = tile(x.reshape(N+1,1), (1,N+1))
14    dX = X - X.T
15    D = dot(c, 1.0/c.T) / (dX+eye(N+1))
16    D = D - diag( D.sum(axis=1) )
17    return D,x
18
```