

Exercises from the final edition of a popular engineering math text. A collection of 1337 mostly odd-numbered exercises. Worked at a mediocre skill level in Mathematica 10. Browse PDFs at the website link provided in the Code tab, or download notebooks from branches.

Note: In a deep GitHub paradox, branch transfer cannot take place while this readme is displayed.

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