```
Example 2, p 83.
```

```
ClearAll["Global`*"]

hig = \{y''[x] + 3y'[x] + 2.25y[x] = -10e^{-1.5x}, y[0] = 1, y'[0] = 0\}

velm = DSolve[hig, y, x]

\{2.25y[x] + 3y'[x] + y''[x] = -10e^{-1.5x}, y[0] = 1, y'[0] = 0\}

\{\{y \rightarrow Function[\{x\}, -5.e^{-1.5x}(-0.2 - 0.3x + 1.x^2)]\}\}

Expand[-5.^ce^{-1.5c}(-0.2 - 0.3x + 1.x^2)]

1. e^{-1.5x} + 1.5e^{-1.5x}x - 5.e^{-1.5x}x^2

Simplify[%]

e^{-1.5x}(1. + 1.5x - 5.x^2)
```

The answer to example 2 in the text is duplicated.

1 - 10 Nonhomogeneous linear ODEs: General solution Find a (real) general solution. State which rule you are using.

```
xen = y''[x] + 5 y'[x] + 4 y[x] == 10 e^{-3 x}
jud = DSolve[xen, y, x]
4 y[x] + 5 y'[x] + y''[x] == 10 e^{-3 x}
\left\{ \left\{ y \rightarrow Function[\{x\}, -5 e^{-3 x} + e^{-4 x} C[1] + e^{-x} C[2] \right] \right\} \right\}
```

1. The text answer is found.

3. 
$$y'' + 3 y' + 2 y = 12 x^2$$

```
ClearAll["Global`*"]

oen = y''[x] + 3 y'[x] + 2 y[x] == 12 x<sup>2</sup>

qas = DSolve[oen, y, x]

2 y[x] + 3 y'[x] + y''[x] == 12 x<sup>2</sup>

\left\{ \left\{ y \rightarrow Function[\{x\}, 3 \left(7 - 6 x + 2 x^{2}\right) + e^{-2 x} C[1] + e^{-x} C[2] \right] \right\} \right\}

Expand[3 \left(7 - 6 x + 2 x^{2}\right)]

21 - 18 x + 6 x<sup>2</sup>
```

qas /. 
$$(3(7-6x+2x^2))$$
 -> 21 - 18 x + 6 x<sup>2</sup>   
  $\{\{y \rightarrow Function[\{x\}, (21-18x+6x^2) + e^{-2x}C[1] + e^{-x}C[2]]\}\}$ 

1. The text answer is found.

5. 
$$y'' + 4 y' + 4 y = e^{-x} Cos[x]$$

ClearAll["Global`\*"]

up = y''[x] + 4 y'[x] + 4 y[x] == 
$$e^{-x} \cos[x]$$
  
nap = DSolve[up, y, x]  
4 y[x] + 4 y'[x] + y''[x] ==  $e^{-x} \cos[x]$ 

$$\left\{ \left\{ y \to Function \left[ \, \left\{ x \right\} \, , \, \, e^{-2 \, x} \, C \left[ \, 1 \right] \, + \, e^{-2 \, x} \, x \, C \left[ \, 2 \, \right] \, + \, \frac{1}{2} \, e^{-x} \, Sin \left[ \, x \, \right] \, \right] \right\} \right\}$$

1. The text answer is found.

7. 
$$\left(D^2 + 2D + \frac{3}{4}I\right)y = 3e^x + \frac{9}{2}x$$

ClearAll["Global`\*"]

mop = 
$$y''[x] + 2 y'[x] + \frac{3}{4}y[x] == 3 e^x + \frac{9}{2}x$$

lam = DSolve[mop, y, x]

$$\frac{3 y[x]}{4} + 2 y'[x] + y''[x] = 3 e^{x} + \frac{9 x}{2}$$

$$\left\{ \left\{ y \to Function \left[ \left\{ x \right\}, \ \frac{2}{5} \left( -40 + 2 e^{x} + 15 \ x \right) + e^{-3 \ x/2} \ C[1] + e^{-x/2} \ C[2] \right] \right\} \right\}$$

Expand 
$$\left[\frac{2}{5} \left(-40 + 2 e^{x} + 15 x\right)\right]$$
  
-16 +  $\frac{4 e^{x}}{5}$  + 6 x

lam /. 
$$\left(\frac{2}{5} \left(-40 + 2 e^{x} + 15 x\right)\right) -> -16 + \frac{4 e^{x}}{5} + 6 x$$

$$\left\{ \left\{ y \to Function \left[ \left\{ x \right\}, \left( -16 + \frac{4 e^x}{5} + 6 x \right) + e^{-3 x/2} C[1] + e^{-x/2} C[2] \right] \right\} \right\}$$

1. The text answer is found.

9. 
$$(D^2 - 16 I) y = 9.6 e^{4 x} + 30 e^{x}$$

ClearAll["Global`\*"]

```
track = y''[x] - 16y[x] = 9.6e^{4x} + 30e^{x}
nard = DSolve[track, y, x]
 -16 y[x] + y''[x] = 30 e^{x} + 9.6 e^{4 x}
 \{y \rightarrow Function[\{x\}, 1.2 e^{-7.x} (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} x) + (-1.66667 e^{8.x} - 0.125 e^{11.x} + 1.e^{11.x} + 1.e^{11.x
                                            e^{4 \cdot x} C[1] + e^{-4 \cdot x} C[2]
-2.e^{1.x} - 0.15e^{4.x} + 1.2e^{4.x}
```

1. Above: altered format of a section prior to hand replacement.

```
scis = nard /.
                             -2. e^{1.x} - 0.15 e^{4.x} + 1.2 e^{4.x}
            {{y →
                                                    Function \left[ \, \left\{ \, x \, \right\} \, , \, \, \left( \, - \, 2 \, . \, \, e^{1 \, \cdot \, \, x} \, - \, 0 \, . \, 15 \, \, e^{4 \, \cdot \, \, x} \, + \, 1 \, . \, 2 \, \, e^{4 \, \cdot \, \, x} \, \, x \, \right) \, + \, e^{4 \, \cdot \, \, x} \, \, C \, [\, 1 \, ] \, + \, e^{-4 \, \cdot \, \, x} \, \, C \, [\, 2 \, ] \, \, \right] \, \right\} \, d^{-1} \, d^{-1}
```

2. Above: hand replacement of a section.

yit = -2. 
$$e^{1 \cdot x} - 0.15 \cdot e^{4 \cdot x} + 1.2 \cdot e^{4 \cdot x} + e^{4 \cdot x} \cdot C[1] + e^{-4 \cdot x} \cdot C[2]$$
  
-2.  $e^{1 \cdot x} - 0.15 \cdot e^{4 \cdot x} + 1.2 \cdot e^{4 \cdot x} \cdot C[1] + e^{-4 \cdot x} \cdot C[2]$ 

3. Above: removed parentheses from a section by hand.

bag = yit /. -0.15 
$$e^{4 \cdot x} + e^{4 \cdot x} C[1] -> + e^{4 \cdot x} C[3]$$
  
-2.  $e^{1 \cdot x} + 1.2 e^{4 \cdot x} x + e^{-4 \cdot x} C[2] + e^{4 \cdot x} C[3]$ 

- 4. Above: consolidated constants in a factor's coefficient by hand, resulting in the text answer.
- 11 18 Nonhomogeneous linear ODEs: IVPs Solve the initial value problem. State which rule you are using. Show each step of your calculation in detail.

11. 
$$y'' + 3y = 18x^2, y[0] = -3, y'[0] = 0$$

ClearAll["Global`\*"]

$$nom = \{y''[x] + 3y[x] = 18x^2, y[0] = -3, y'[0] = 0\}$$

$$kla = DSolve[nom, y, x]$$

$$\{3y[x] + y''[x] = 18x^2, y[0] = -3, y'[0] = 0\}$$

$$\{\{y \rightarrow Function[\{x\}, -4 + 6x^2 + Cos[\sqrt{3}x]]\}\}$$

1. The answer matches the text.

13. 
$$8 y'' - 6 y' + y = 6 Cosh[x], y[0] = 0.2, y'[0] = 0.05$$

ClearAll["Global`\*"]

$$\begin{aligned} &\text{uil} = \{8 \ y''[x] - 6 \ y'[x] + y[x] = 6 \ \text{Cosh}[x], \ y[0] = 0.2, \ y'[0] = 0.05\} \\ &\text{qwx} = \text{DSolve}[\text{uil}, \ y[x], \ x] \\ &\{y[x] - 6 \ y'[x] + 8 \ y''[x] = 6 \ \text{Cosh}[x], \ y[0] = 0.2, \ y'[0] = 0.05\} \\ &\Big\{\Big\{y[x] \rightarrow e^{-x} \left(0.2 + 1. \ e^{5 \ x/4} - 2. \ e^{3 \ x/2} + e^{2 \ x}\right)\Big\}\Big\} \end{aligned}$$

Expand [qwx]

$$\{\{y[x] \rightarrow 0.2 e^{-x} + 1. e^{x/4} - 2. e^{x/2} + e^x\}\}$$

1. The answer matches the text.

```
15. (x^2 D^2 - 3 x D + 3 I) y = 3 Log[x] - 4, y[1] = 0, y'(1) = 1;
y_p = Log[x]
```

ClearAll["Global`\*"]

 $\{\{y[x] \rightarrow Log[x]\}\}$ 

1. The answer matches the text.

17. 
$$(D^2 + 0.2 D + 0.26 I) y = 1.22 e^{0.5 x}, y[0] = 3.5, y'[0] = 0.35$$

ClearAll["Global`\*"]

hal = 
$$\{y''[x] + 0.2 y'[x] + 0.26 y[x] = 1.22 e^{0.5 x}, y[0] = 3.5, y'[0] = 0.35\}$$
  
 $xxa = DSolve[hal, y[x], x]$   
 $\{0.26 y[x] + 0.2 y'[x] + y''[x] = 1.22 e^{0.5 x}, y[0] = 3.5, y'[0] = 0.35\}$   
 $\{\{y[x] \rightarrow 2. e^{-0.1 x} (0.75 Cos[0.5 x] + 1. e^{0.6 x} Sin[0.5 x]^2)\}\}$   
bur =  $xxa /. (1. e^{0.6 x} Cos[0.5 x]^2 + 1. e^{0.6 x} Sin[0.5 x]^2) \rightarrow 1. e^{0.6 x}$   
 $\{\{y[x] \rightarrow 2. e^{-0.1 x} (1. e^{0.6 x} + 0.75 Cos[0.5 x] - 0.5 Sin[0.5 x])\}\}$ 

1. Above: altered with hand-inserted trig ident  $\sin^2 x + \cos^2 x = 1$ .

## Expand[bur]

```
\left\{\left\{y\,[\,x\,]\,\to\,2\,.\,\,\mathrm{e}^{0\,.\,5\,\,x}\,+\,1\,.\,5\,\,\mathrm{e}^{-0\,.\,1\,\,x}\,\,\mathrm{Cos}\,[\,0\,.\,5\,\,x\,]\,\,-\,1\,.\,\,\mathrm{e}^{-0\,.\,1\,\,x}\,\,\mathrm{Sin}\,[\,0\,.\,5\,\,x\,]\,\,\right\}\right\}
```

2. The above answer matches the text.