

## engineering\_math\_worked\_problems\_with\_Mathematica

Exercises from the final edition of a popular engineering math text. A collection of 1332 mostly odd-numbered exercises. Worked at a mediocre skill level in Mathematica 10. Browse PDFs on the locally hosted site, then come back and download anything interesting.

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