```
11 - 14 Linear transformations
Find the inverse transformation.
```

```
11. y_1 = 0.5 x_1 - 0.5 x_2

y_2 = 1.5 x_1 - 2.5 x_2
```

ClearAll["Global`*"]

$$\{5. y1 - 1. y2 = x1, 3. y1 - 1. y2 = x2\}$$

Above: The expressions match the text.

```
13. y_1 = 5 x_1 + 3 x_2 - 3 x_3

y_2 = 3 x_1 + 2 x_2 - 2 x_3

y_3 = 2 x_1 - x_2 + 2 x_3
```

ClearAll["Global`*"]

$${2 y1 - 3 y2 = x1, -10 y1 + 16 y2 + y3 = x2, -7 y1 + 11 y2 + y3 = x3}$$

Above: The answer matches the text.

ClearAll["Global`*"]

$$e1 = \{3, 1, -4\}$$

$$\{3, 1, -4\}$$

 $\sqrt{26}$

Above: The answer matches the text. If I do the problem with literal interpretation of the given vector

Norm $[\{\{3, 1, -4\}\}^{\dagger}]$

$$\sqrt{26}$$

it still comes out right.

17.
$$\{\{1, 0, 0, 1, -1, 0, -1, 1\}\}^{\dagger}$$

ClearAll["Global`*"]

 $\sqrt{5}$

Above: The answer matches the text.

19.
$$\left\{ \left\{ \frac{2}{3}, \frac{2}{3}, \frac{1}{3}, 0 \right\} \right\}^{\dagger}$$

ClearAll["Global`*"]

$$e1 = \left\{ \frac{2}{3}, \frac{2}{3}, \frac{1}{3}, 0 \right\}$$

$$\left\{\frac{2}{3}, \frac{2}{3}, \frac{1}{3}, 0\right\}$$

1

Above: The answer matches the text.

21 - 25 Inner product. Orthogonality.

21. Orthogonality. For what value(s) of k are the vec-

$$\{\{2, \frac{1}{2}, -4, 0\}\}^{\dagger} \text{ and } \{\{5, k, 0, \frac{1}{4}\}\}^{\dagger} \text{ orthogonal?}$$

ClearAll["Global`*"]

$$e1 = \left\{2, \frac{1}{2}, -4, 0\right\}$$

$$\{2, \frac{1}{2}, -4, 0\}$$

$$e2 = \left\{5, k, 0, \frac{1}{4}\right\}$$

$$\{5, k, 0, \frac{1}{4}\}$$

$$10+\frac{k}{2}$$

$$e4 = Solve[e3 == 0, k]$$

$$\{ \{ k \rightarrow -20 \} \}$$

Above: The answer matches the text.