Clear["Global`*"]

- 1. Linear ODE. If p and r in y' + p(x) y = r(x) are continuous for all x in an interal $|x x_0| \le a$, show that f(x, y) in this ODE satisfies the conditions of our present theorems, so that a corresponding initial value problem has a unique solution. Do you actually need these theorems of this ODE?
- 3. Vertical strip. If the assumptions of theorems 1 and 2 are satisfied not merely in a rectangle but in a vertical infinite strip $|x x_0| < a$, in what interval will the solution of (1) exist?
- 5. Length of x-interval. In most cases the solution of an initial value problem (1) exists in an x-interval larger than that guaranteed by the present theorems. Show this fact for $y' = 2y^2$, y(1) = 1 by finding the best possible a (choosing b optimally) and comparing the result with the actual solution.
- 7. Maximum α . What is the largest possible α in example 1 in the text?
- 9. Common points. Can two solution curves of the same ODE have a common point in a rectangle in which the assumptions of the present theorems are satisfied?