

engineering_math_worked_problems_with_Mathematica

Exercises from the final edition of a popular engineering math text. A collection of 1332 mostly odd-numbered exercises. Worked at a mediocre skill level in Mathematica 10. Browse PDFs at https://whiffie.github.io/engineering_math_worked_problems_with_Mathematica/, or get notebooks here.

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