```
1 - 10 Inner product
 Let a = \{1, -3, 5\}, b = \{4, 0, 8\}, c = \{-2, 9, 1\}
 1. a.b, b.a, b.c
Clear["Global`*"]
aa = \{1, -3, 5\}; bb = \{4, 0, 8\}; cc = \{-2, 9, 1\}
{-2, 9, 1}
e1 = aa.bb
 44
e2 = bb.aa
 44
e3 = bb.cc
 3. |a|, |2b|, |-c|
Norm[aa]
 \sqrt{35}
Norm[2 bb]
 8 <del>√</del>5
Norm[-cc]
 \sqrt{86}
 5. |b + c|, |b| + |c|
e7 = Norm[bb + cc]
 \sqrt{166}
```

e8 = Norm[bb] + Norm[cc]

$$4\sqrt{5}+\sqrt{86}$$

e9 = FullSimplify[e7 == e8]

False

e10 = Norm[aa.cc]

24

e11 = Norm[aa] Norm[cc]

 $\sqrt{3010}$

9.
$$15a.b + 15a.c, 15a.(b+c)$$

e12 = 15 aa.bb + 15 aa.cc

300

e13 = 15 aa.(bb + cc)

300

17 - 20 Work

Find the work done by a force \mathbf{p} acting on a body if the body is displaced along the straight segment \overline{AB} from A to B. Sketch \overline{AB} and **p**.

17.
$$p = \{2, 5, 0\}, A: \{1, 3, 3\}, B: \{3, 5, 5\}$$

Clear["Global`*"]

$$aA = \{1, 3, 3\}; bB = \{3, 5, 5\}$$

{3, 5, 5}

$$pP = \{2, 5, 0\}$$

{2, 5, 0}

dis = bB - aA

{2, 2, 2}

wW = dis.pP

14

19.
$$p = \{0, 4, 3\}, A: \{4, 5, -1\}, B: (1, 3, 0\}$$

Clear["Global`*"]

$$pP = \{0, 4, 3\}; aA = \{4, 5, -1\}; bB = \{1, 3, 0\}$$

 $\{1, 3, 0\}$

dis = bB - aA

 $\{-3, -2, 1\}$

wW = dis.pP

- 5

22 - 30 Angle between vectors

Let
$$aA = \{1, 1, 0\}$$
; $bB = \{3, 2, 1\}$; $cC = \{1, 0, 2\}$

23. b, c

dotbc = bB.cC

5

e1 =
$$\frac{\text{dotbc}}{\text{Norm[bB] Norm[cC]}}$$

$$\sqrt{\frac{5}{14}}$$
 // N

0.597614

e2 = ArcCos[e1]

$$\operatorname{ArcCos}\Big[\sqrt{\frac{5}{14}}\,\Big] \; // \; \mathrm{N}$$

0.930274

$$e3 = \frac{e2}{Degree} // N$$

53.3008

31 - 35 Orthogonality is particularly important, mainly because of orthogonal coordinates, such as Cartesian coordinates, whose natural basis consists of three orthogonal

unit vectors.

31. For what values of a_1 are $\{a_1, 4, 3\}$ and $\{3, -2, 12\}$ orthogonal?

Clear["Global`*"]
e1 = {a₁, 4, 3}
{a₁, 4, 3}
e2 = {3, -2, 12}
{3, -2, 12}
e3 = e1.e2
28 + 3 a₁

Solve[e3 == 0]

$$\left\{\left\{a_1 \to -\frac{28}{3}\right\}\right\}$$

33. Unit vectors. Find all unit vectors $a = \{a_1, a_2\}$ in the plane orthogonal to $\{4, 3\}$

Clear["Global`*"]

 $e1 = {4, 3}$

{4,3}

e2 = Norm[e1]

5

 $e3 = \{a_1, a_2\}$

 $\{a_1, a_2\}$

e4 = Norm[e3]

$$\sqrt{\text{Abs}\left[\mathsf{a}_1\right]^2 + \text{Abs}\left[\mathsf{a}_2\right]^2}$$

e5 = Solve[e1.e3 == 0 && Norm[e3] == 1]

$$\left\{ \left\{ a_{1} \rightarrow \frac{3}{5}, \ a_{2} \rightarrow -\frac{4}{5} \right\}, \ \left\{ a_{1} \rightarrow -\frac{3}{5}, \ a_{2} \rightarrow \frac{4}{5} \right\} \right\}$$

36 - 40 Component in the direction of a vector

Find the component of a in the direction of b. Make a sketch.

37.
$$a = \{3, 4, 0\}, b = \{4, -3, 2\}$$

Clear["Global`*"]

To find the component of **a** in the direction of **b**, I first need to find the angle separating them.

```
e1 = \{3, 4, 0\}
{3, 4, 0}
e2 = \{4, -3, 2\}
{4, -3, 2}
e3 = _____e1.e2
     Norm[e1] Norm[e2]
e4 = ArcCos[e3]
\frac{\pi}{2}
```

These two vectors are perpendicular; therefore there is not projection (=0).

```
e5 = Norm[e1] Cos[e4]
 0
```

Green cells in this problem set denote agreement with the text answers.