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1 - 5 Application of differential operators
Apply the given operator to the given functions. Show all steps in detail.
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1. 
$$D^2 + 2 D$$
; Cosh[2 x],  $e^{-x} + e^{2x}$ , Cos[x]

```
Clear["Global`*"]

r[x_] := Cosh[2 x]

r'''[x] + 2 r'[x]

4 Cosh[2 x] + 4 Sinh[2 x]

FullSimplify[%]

4 e<sup>2 x</sup>

s[x_] := e<sup>-x</sup> + e<sup>2 x</sup>

s'''[x] + 2 s'[x]

e<sup>-x</sup> + 4 e<sup>2 x</sup> + 2 (-e<sup>-x</sup> + 2 e<sup>2 x</sup>)

Simplify[%]

e<sup>-x</sup> (-1 + 8 e<sup>3 x</sup>) (* text answer is -e<sup>-x</sup> + 8 e<sup>2 x</sup> *)

u[x_] := Cos[x]

u'''[x] + 2 u'[x]

-Cos[x] - 2 Sin[x]
```

The above answers agree with the text (except yellow).

3. 
$$(D - 2 I)^2$$
;  $e^{2x}$ ,  $x e^{-2x}$ 

```
Clear["Global`*"]
v[x_] := e<sup>2 x</sup>
v''[x] - 4 v'[x] + 4 v[x]
```

$$w[x_{-}] := x e^{2 x}$$
 $w''[x] - 4 w'[x] + 4 w[x]$ 
 $4 e^{2 x} + 8 e^{2 x} x - 4 (e^{2 x} + 2 e^{2 x} x)$ 

## Simplify[%]

$$z[x_] := e^{-2x}$$

$$z''[x] - 4z'[x] + 4z[x]$$

The above answers agree with the text.

5. (D - 2 I)(D + 3 I); 
$$e^{2x}$$
, x  $e^{2x}$ ,  $e^{-3x}$ 

Clear["Global`\*"]

$$r[x_{-}] := e^{2x}$$

0

$$s[x_] := x e^{2x}$$

$$s''[x] + s'[x] - 6s[x]$$

$$u[x_] := e^{-3x}$$

$$u''[x] + u'[x] - 6u[x]$$

0

The above answers agree with the text.

## 6 - 12 General solution

Factor as in the text and solve.

7. 
$$(4 D^2 - I)y = 0$$

Clear["Global`\*"]

$$r = 4 y''[x] - y[x] == 0$$

$$-y[x] + 4y''[x] = 0$$

DSolve[r, y, x]

$$\left\{\left\{y \rightarrow Function\left[\left\{x\right\},\ e^{x/2}\ C\left[1\right]\ +\ e^{-x/2}\ C\left[2\right]\right]\right\}\right\}$$

The above answer matches the text's.

9. 
$$(D^2 - 4.20 D + 4.41 I)y = 0$$
  
Clear["Global`\*"]

Clear["Global`\*"]
$$s = y''[x] - 4.20 y'[x] + 4.41 y[x] == 0$$

$$DSolve[s, y, x]$$

$$4.41 y[x] - 4.2 y'[x] + y''[x] == 0$$

$$\left\{ \left\{ y \rightarrow Function[\{x\}, e^{2.1 x} C[1] + e^{2.1 x} x C[2] \right] \right\} \right\}$$

The above answer matches the text's.

```
11. (D^2 - 4.00 D + 3.84 I)y = 0
Clear["Global`*"]
u = y''[x] - 4.00 y'[x] + 3.84 y[x] == 0
DSolve[u, y, x]
3.84 y[x] - 4. y'[x] + y''[x] = 0
```

The above answer matches the text's.

 $\left\{ \left\{ y \to Function \left[ \, \left\{ \, x \, \right\} \, , \, \, e^{1 \, \cdot \, 6 \, \, x} \, \, C \, [\, 1 \, ] \, + \, e^{2 \, \cdot \, 4 \, \, x} \, \, C \, [\, 2 \, ] \, \, \right] \right\} \right\}$