# At the beginning of mathematical objects

Jean-Frédéric Durand, M1, université Lille 1

### Introduction

- O Do you have a problem with 27 ? (three times three)
- O No? Well you are able to conceptualize (abstraction).

## Plan

- O The Birth of equations
- Formalization
- O Groups

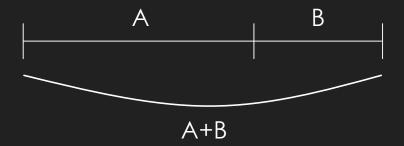
# The birth of Equations

- O This object called: unknown in mathematics has appeared for the time in the Antiquity.
- The problem was : « Division in Extrem and Mean Ratio »

## The birth of Equations

The Goal is to divide a segment in two.

The little section divide by the tall section equals the tall section divide by the entiere segment.



$$\frac{B}{A} = \frac{A}{A+B}$$

## The birth of Equations

- Others problems talking about area.
- O Egyptian: A number and its sevenths equals nineteen. What is this number?
- O Greek: Thales, Euclide, Pythagore

Solving methods are geometrical or numerical and always about lenght, area or volume.

#### Formalization

- In the ninth century, Al Khwarizmy invent two object :
  - O Unknown
  - O Equation
- O He still uses sentences but gave up the thing behind the number (length, area, volumes... etc)
- Now we can study equations for themselves.

#### Formalization

- O The nineteenth century: Galois created the concept of « group »
  - O For solving equations of higher degree
  - Open the way to a lot of derived object: circle, division ring

# Groups

- O A group is a couple (G,S)
  - O G a set : [a,b]
    - (number,variable,..etc)
  - O S an operation:
    - O (+,-,\*,/,..etc)



## Groups

- O A group has to respect four rules:
  - O Closure
    - O a,b in G; in G
  - O Associativity
    - O a,b,c in G:  $(a \cdot b) \cdot c = a \cdot (b \cdot c)$
  - O Identity Element (e)
    - O e,a in G;  $e \cdot a = a \cdot e = a$
  - O Inverse Element
    - O e,a,b in G;  $a \cdot b = b \cdot a = e$



#### Conclusion

- O Mathematics are universal?
- « Mathematics should be an obviousness for everyone, because it's only a logical concatenation, which is in theroy a formality of the 'common sense' shared by everybody » Poincaré

# Bibliography

- O Podcast Science
- R. Herz-Fischler, A Mathematical History of Division in Extreme and Mean Ratio, Wilfrid Laurier.
- O <a href="https://fr.wikipedia.org/wiki/Al-Khw%C3%A2rizm%C3%AE">https://fr.wikipedia.org/wiki/Al-Khw%C3%A2rizm%C3%AE</a>
- O <a href="https://fr.wikipedia.org/wiki/Groupe">https://fr.wikipedia.org/wiki/Groupe</a> (math%C3%A9matiques)

# Complex Number

- Tartaglia find a way to solve 3 degrees of equations
- O Sometimes in the middle of the calculation he falls of a monster.
- A monster is a square root of a negative number.
- O These numbers are called imaginary numbers.

# Complexe Number

- O Later D'Alembert found that these monster is a multiple of a number that mulitply -1.
- O Written a+ib
- O Complexe is not the meaning of difficulty here, but the fact of their composition in two member.