In-Class activity 5 - Group Edith

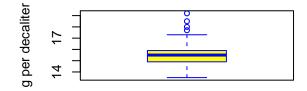
2023-04-04

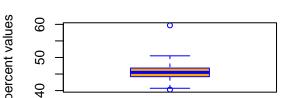
```
library(DAAG) # it cointains AIS dataset and CVlm (Cross-Validation for Linear Regression)
head(ais, n=10)
      rcc wcc
                hc
                     hg ferr
                               bmi
                                     ssf pcBfat
                                                  1bm
                                                         ht
                                                              wt sex sport
## 1 3.96 7.5 37.5 12.3
                          60 20.56 109.1 19.75 63.32 195.9 78.9
                                                                   f B_Ball
                                                                   f B_Ball
## 2 4.41 8.3 38.2 12.7
                          68 20.67 102.8 21.30 58.55 189.7 74.4
## 3 4.14 5.0 36.4 11.6
                         21 21.86 104.6 19.88 55.36 177.8 69.1
                                                                   f B_Ball
                                                                   f B_Ball
## 4 4.11 5.3 37.3 12.6
                          69 21.88 126.4 23.66 57.18 185.0 74.9
                                                                   f B_Ball
## 5 4.45 6.8 41.5 14.0
                          29 18.96 80.3 17.64 53.20 184.6 64.6
                                                                   f B_Ball
## 6 4.10 4.4 37.4 12.5
                          42 21.04 75.2 15.58 53.77 174.0 63.7
## 7 4.31 5.3 39.6 12.8
                          73 21.69 87.2 19.99 60.17 186.2 75.2
                                                                   f B_Ball
## 8 4.42 5.7 39.9 13.2
                          44 20.62 97.9 22.43 48.33 173.8 62.3
                                                                   f B_Ball
## 9 4.30 8.9 41.1 13.5
                          41 22.64 75.1 17.95 54.57 171.4 66.5
                                                                   f B_Ball
## 10 4.51 4.4 41.6 12.7
                          44 19.44 65.1 15.07 53.42 179.9 62.9
                                                                   f B Ball
library(e1071) # it includes function to compute skewness
library(plyr) # it allows to wrangle data
## Attaching package: 'plyr'
## The following object is masked from 'package:DAAG':
##
##
      ozone
library(ggplot2) # it allows to create a number of different types of plots
colSums(is.na(ais))
##
     rcc
            WCC
                    hc
                           hg
                                ferr
                                        bmi
                                               ssf pcBfat
                                                             1bm
                                                                     ht
                                                                            wt
##
       0
              0
##
     sex sport
ais2 <- subset(ais, sex=="m") # only male athletes
ais3 = ais2[,c(3,4,6,8)] # subset column number that correspond to "hg", "hc", "bmi" and "pcBfat"
newdata <- rename(ais3, c("hg"="HEMAGLOBIN", "hc"="HEMATOCRIT", "bmi"="BMI", "pcBfat"="BODY_FAT_PERC"))
str(newdata)
## 'data.frame':
                  102 obs. of 4 variables:
## $ HEMATOCRIT
                  : num 46.8 45.2 46.6 44.9 46.1 45.1 47.5 45.5 48.6 44.9 ...
## $ HEMAGLOBIN
                 : num 15.9 15.2 15.9 15 15.6 15.2 16.3 15.2 16.5 15.4 ...
                  : num 22.5 23.9 23.7 23.1 22.3 ...
## $ BODY_FAT_PERC: num 8.47 7.68 6.16 8.56 6.86 ...
summary(newdata)
     HEMATOCRIT
                     HEMAGLOBIN
                                        BMI
                                                   BODY_FAT_PERC
```

```
:40.30
                   Min.
                                   Min. :19.63
## Min.
                          :13.50
                                                   Min. : 5.630
  1st Qu.:44.23
                  1st Qu.:14.93
                                   1st Qu.:22.29
                                                   1st Qu.: 6.968
## Median :45.50
                  Median :15.50
                                   Median :23.56
                                                   Median : 8.625
          :45.65
                   Mean
                         :15.55
                                   Mean
                                         :23.90
                                                         : 9.251
## Mean
                                                   Mean
   3rd Qu.:46.80
                   3rd Qu.:15.90
                                   3rd Qu.:25.16
                                                   3rd Qu.:10.010
  Max.
          :59.70
                   Max.
                          :19.20
                                   Max.
                                          :34.42
                                                          :19.940
                                                   Max.
par(mfrow=c(2, 2)) # it divides graph area in two parts
boxplot(newdata$HEMAGLOBIN, col = "yellow", border="blue",
       main = "HEMAGLOBIN boxplot",
       ylab = "g per decaliter")
boxplot(newdata$HEMATOCRIT, col = "orange", border="blue",
       main = "HEMATROCRIT boxplot",
       ylab = "percent values")
boxplot(newdata$BMI, col = "green", border="blue",
       main = "BMI boxplot",
       ylab = "value")
boxplot(newdata$BODY_FAT_PERC, col = "red", border="blue",
       main = "BODY_FAT_PERC boxplot",
       ylab = "percent values")
```

HEMAGLOBIN boxplot

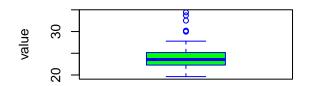
HEMATROCRIT boxplot

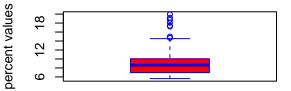




BMI boxplot

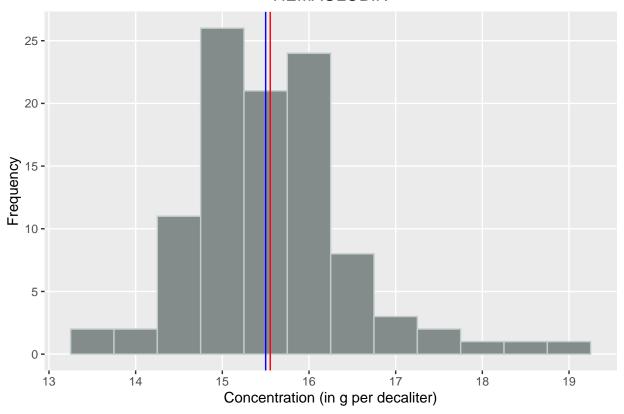
BODY_FAT_PERC boxplot





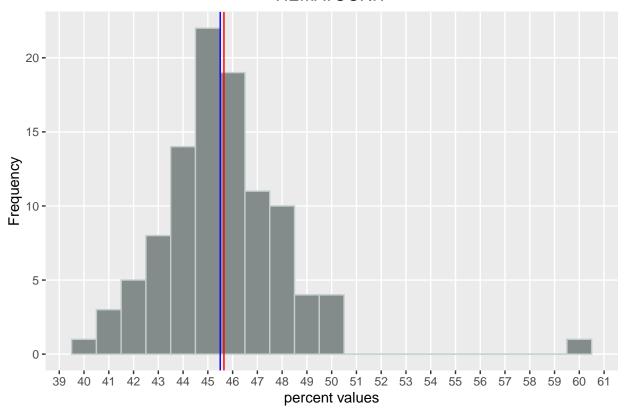
```
boxplot.stats(newdata$HEMAGLOBIN)$out # HEMAGLOBIN outliers
## [1] 18.0 19.2 18.5 17.7
boxplot.stats(newdata$HEMATOCRIT)$out #HEMATOCRIT outliers
## [1] 40.3 59.7
boxplot.stats(newdata$BMI)$out #BMI outliers
## [1] 29.97 32.52 30.18 34.42 33.73 30.18
boxplot.stats(newdata$BODY_FAT_PERC)$out #BODY_FAT_PERC outliers
## [1] 19.94 17.41 18.08 18.72 19.17 17.24 14.69 14.98
# Histogram of HEMAGLOBIN
qplot(HEMAGLOBIN, data = newdata, geom="histogram", binwidth=0.5,
      fill=I("azure4"), col=I("azure3")) +
  labs(title = "HEMAGLOBIN") +
  theme(plot.title = element_text(hjust = 0.5)) +
  labs(x = "Concentration (in g per decaliter)") +
  labs(y = "Frequency") +
  scale y continuous(breaks = c(0.5, 10.15, 20.25, 30.35, 40.45, 50), minor breaks = NULL) +
  scale_x_continuous(breaks = c(10:25), minor_breaks = NULL) +
  geom_vline(xintercept = mean(newdata$HEMAGLOBIN), show_guide=TRUE, color
             ="red", labels="Average") +
  geom_vline(xintercept = median(newdata$HEMAGLOBIN), show_guide=TRUE, color
             ="blue", labels="Median")
## Warning: `qplot()` was deprecated in ggplot2 3.4.0.
## This warning is displayed once every 8 hours.
## Call `lifecycle::last_lifecycle_warnings()` to see where this warning was
## generated.
## Warning: The `show_guide` argument of `layer()` is deprecated as of ggplot2 2.0.0.
## i Please use the `show.legend` argument instead.
## This warning is displayed once every 8 hours.
## Call `lifecycle::last_lifecycle_warnings()` to see where this warning was
## generated.
## Warning in geom_vline(xintercept = mean(newdata$HEMAGLOBIN), show_guide = TRUE,
## : Ignoring unknown parameters: `labels`
## Warning in geom_vline(xintercept = median(newdata$HEMAGLOBIN), show_guide =
## TRUE, : Ignoring unknown parameters: `labels`
```

HEMAGLOBIN



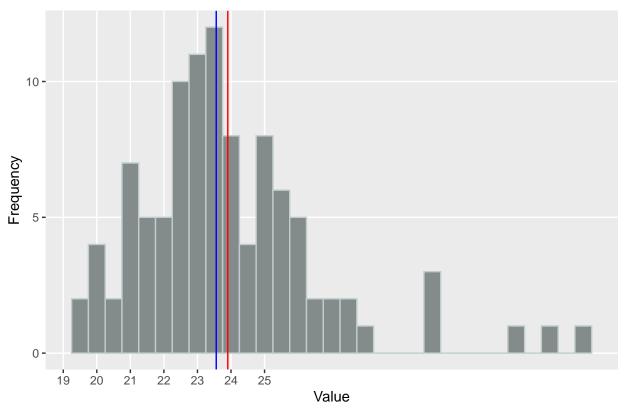
```
## Warning in geom_vline(xintercept = mean(newdata$HEMATOCRIT), show_guide = TRUE,
## : Ignoring unknown parameters: `labels`
## Warning in geom_vline(xintercept = median(newdata$HEMATOCRIT), show_guide =
## TRUE, : Ignoring unknown parameters: `labels`
```

HEMATOCRIT



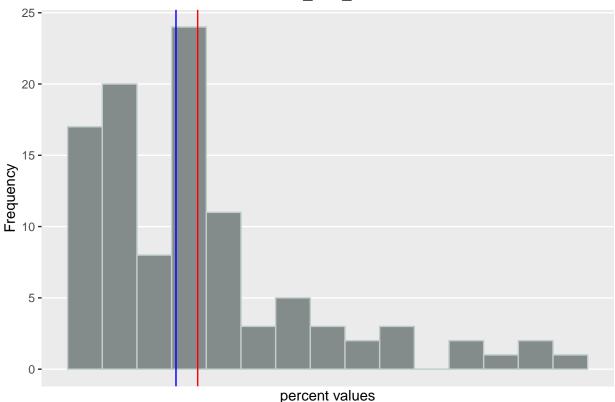
```
## Warning in geom_vline(xintercept = mean(newdata$BMI), show_guide = TRUE, :
## Ignoring unknown parameters: `labels`
## Warning in geom_vline(xintercept = median(newdata$BMI), show_guide = TRUE, :
## Ignoring unknown parameters: `labels`
```



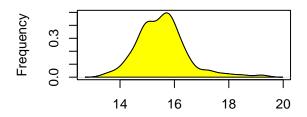


```
## Warning in geom_vline(xintercept = mean(newdata$BODY_FAT_PERC), show_guide =
## TRUE, : Ignoring unknown parameters: `labels`
## Warning in geom_vline(xintercept = median(newdata$BODY_FAT_PERC), show_guide =
## TRUE, : Ignoring unknown parameters: `labels`
```

BODY_FAT_PERC

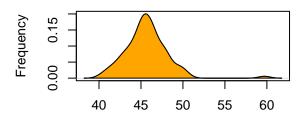


Density: HEMAGLOBIN



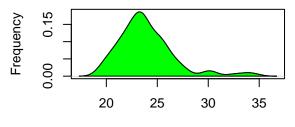
N = 102 Bandwidth = 0.2597 Skewness: 0.96

Density: HEMATOCRIT



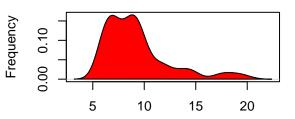
N = 102 Bandwidth = 0.6858 Skewness: 1.47

Density: BMI



N = 102 Bandwidth = 0.763 Skewness: 1.39

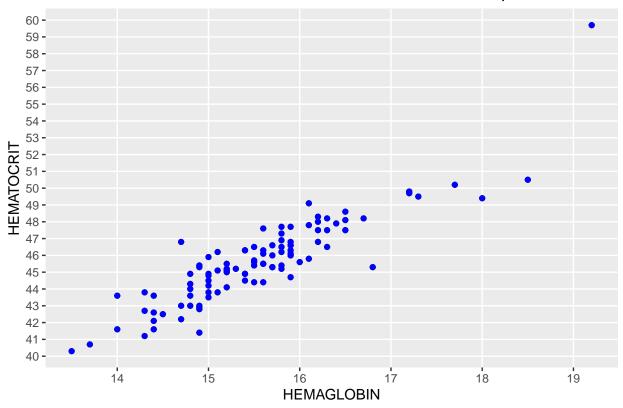
Density: BODY_FAT_PERC



N = 102 Bandwidth = 0.8103 Skewness: 1.51

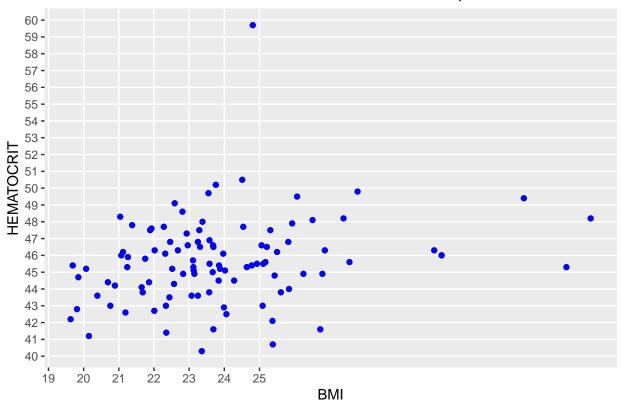
```
qplot(HEMAGLOBIN, HEMATOCRIT, data = newdata,
    main = "HEMAGLOBIN and HEMATOCRIT relationship") +
    theme(plot.title = element_text(hjust = 0.5)) +
    geom_point(colour = "blue", size = 1.5) +
    scale_y_continuous(breaks = c(30:65), minor_breaks = NULL) +
    scale_x_continuous(breaks = c(10:25), minor_breaks = NULL)
```

HEMAGLOBIN and HEMATOCRIT relationship



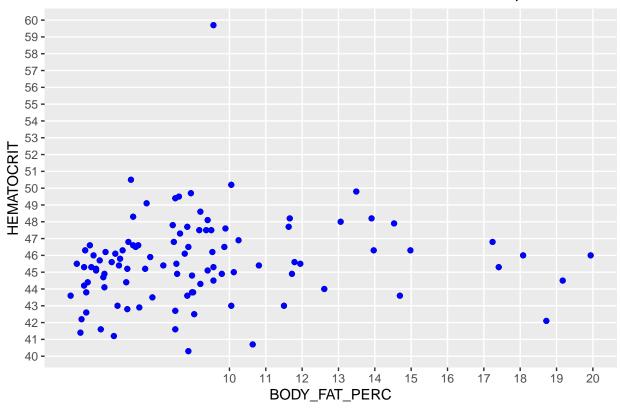
```
qplot(BMI, HEMATOCRIT, data = newdata,
    main = "BMI and HEMATOCRIT relationship") +
    theme(plot.title = element_text(hjust = 0.5)) +
    geom_point(colour = "blue", size = 1.5) +
    scale_y_continuous(breaks = c(30:65), minor_breaks = NULL) +
    scale_x_continuous(breaks = c(10:25), minor_breaks = NULL)
```

BMI and HEMATOCRIT relationship

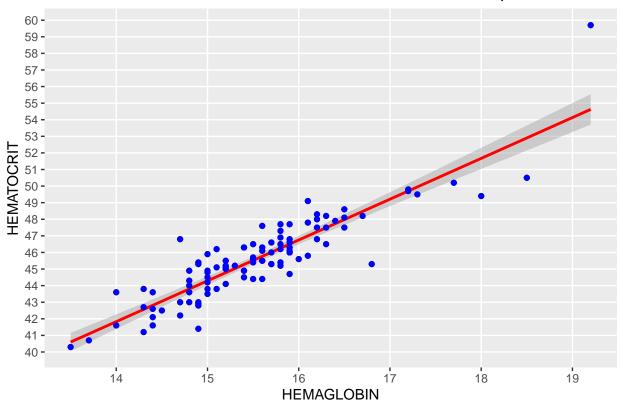


```
qplot(BODY_FAT_PERC, HEMATOCRIT, data = newdata,
    main = "BODY_FAT_PERC and HEMATOCRIT relationship") +
    theme(plot.title = element_text(hjust = 0.5)) +
    geom_point(colour = "blue", size = 1.5) +
    scale_y_continuous(breaks = c(30:65), minor_breaks = NULL) +
    scale_x_continuous(breaks = c(10:25), minor_breaks = NULL)
```

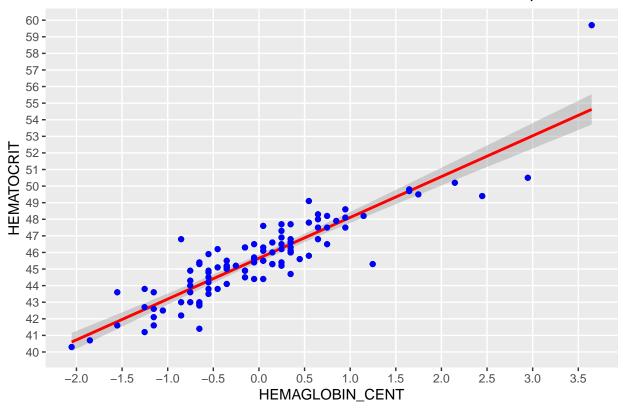
BODY_FAT_PERC and HEMATOCRIT relationship



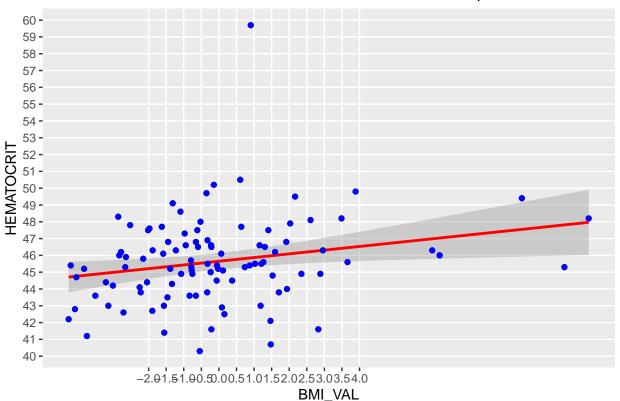
HEMAGLOBIN and HEMATOCRIT relationship



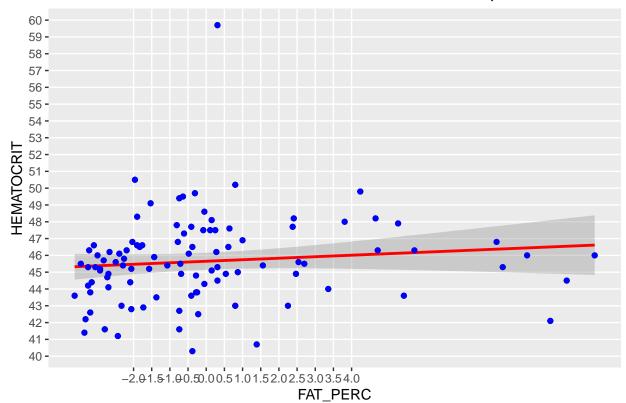
HEMAGLOBIN_CENT and HEMATOCRIT relationship



BMI_VAL and HEMATOCRIT relationship



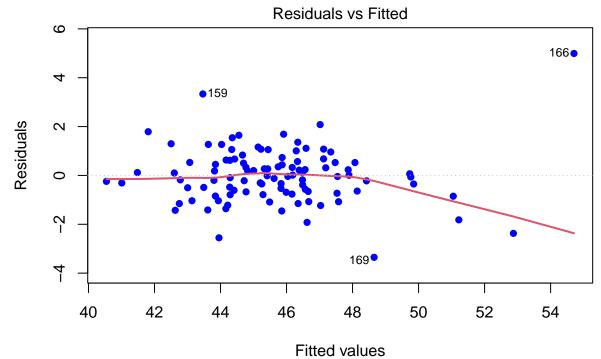
FAT_PERC and HEMATOCRIT relationship



mod1 = lm(HEMATOCRIT ~ HEMAGLOBIN_CENT+FAT_PERC+BMI_VAL, data = newdata)
summary(mod1)

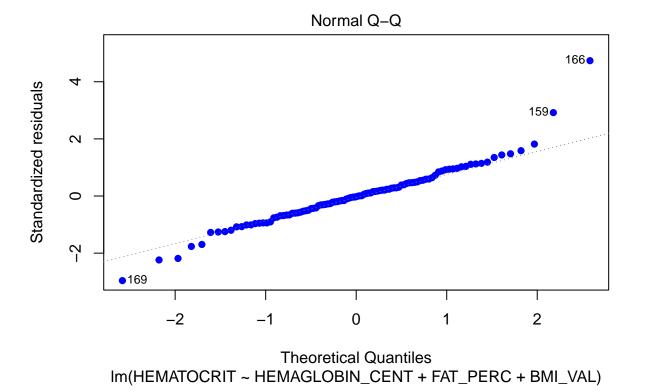
```
##
## Call:
## lm(formula = HEMATOCRIT ~ HEMAGLOBIN_CENT + FAT_PERC + BMI_VAL,
       data = newdata)
##
##
## Residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
  -3.3523 -0.6691 -0.0266 0.5588 4.9926
##
##
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                   45.65000
                               0.11443 398.925
                                                 <2e-16 ***
## HEMAGLOBIN_CENT 2.49389
                               0.12937 19.278
                                                 <2e-16 ***
## FAT PERC
                   0.04711
                               0.04662
                                        1.010
                                                  0.315
## BMI_VAL
                   -0.05794
                               0.05577 -1.039
                                                  0.301
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.156 on 98 degrees of freedom
## Multiple R-squared: 0.8035, Adjusted R-squared: 0.7975
## F-statistic: 133.6 on 3 and 98 DF, p-value: < 2.2e-16
modSummary <- summary(mod1) # capture model summary as an object</pre>
modCoeff <- modSummary$coefficients # model coefficients</pre>
```

```
std.error <- modCoeff["HEMAGLOBIN_CENT", "Std. Error"] # get standard error</pre>
hem_t_value <- beta.estimate/std.error # calculate t statistic</pre>
sprintf(fmt = "%10s is the t-value for HEMAGLOBIN", hem_t_value)
## [1] "19.2778709228326 is the t-value for HEMAGLOBIN"
beta.estimate <- modCoeff["FAT_PERC", "Estimate"] # qet beta coefficient estimate
std.error <- modCoeff["FAT_PERC", "Std. Error"] # get standard error</pre>
fat_t_value <- beta.estimate/std.error # calculate t statistic</pre>
sprintf(fmt = "%10s is the t-value for Body Fat Percentage", fat t value)
## [1] "1.01046086146836 is the t-value for Body Fat Percentage"
beta.estimate <- modCoeff["BMI_VAL", "Estimate"] # get beta coefficient estimate
std.error <- modCoeff["BMI_VAL", "Std. Error"] # get standard error</pre>
bmi t value <- beta.estimate/std.error # calculate t statistic</pre>
sprintf(fmt = "%10s is the t-value for BMI", bmi_t_value)
## [1] "-1.03883606994576 is the t-value for BMI"
f_statistic <- mod1$fstatistic[1] # calculate F statistic</pre>
f <- summary(mod1)$fstatistic # parameters for model p-value calculation
print(f) # print F value
##
     value
             numdf
                      dendf
## 133.6155 3.0000 98.0000
plot(mod1, pch=16, col="blue", lty=1, lwd=2, which=1)
```

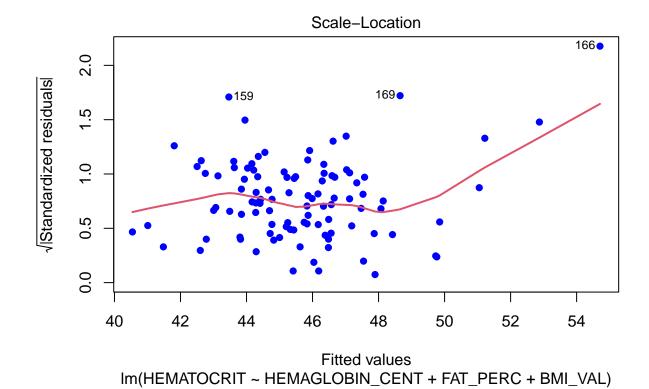


Im(HEMATOCRIT ~ HEMAGLOBIN_CENT + FAT_PERC + BMI_VAL)

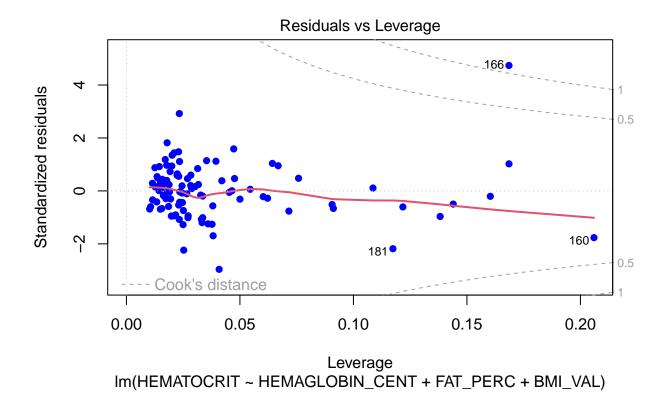
plot(mod1, pch=16, col="blue", lty=1, lwd=2, which=2)



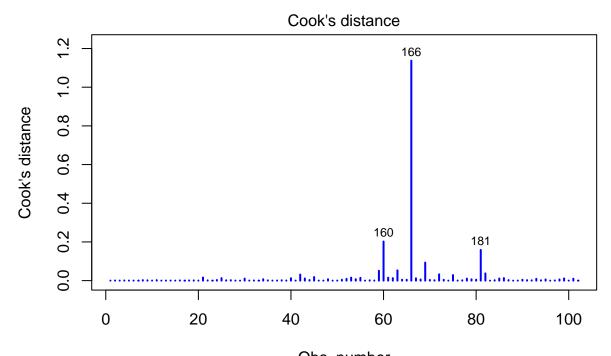
plot(mod1, pch=16, col="blue", lty=1, lwd=2, which=3)



plot(mod1, pch=16, col="blue", lty=1, lwd=2, which=5)

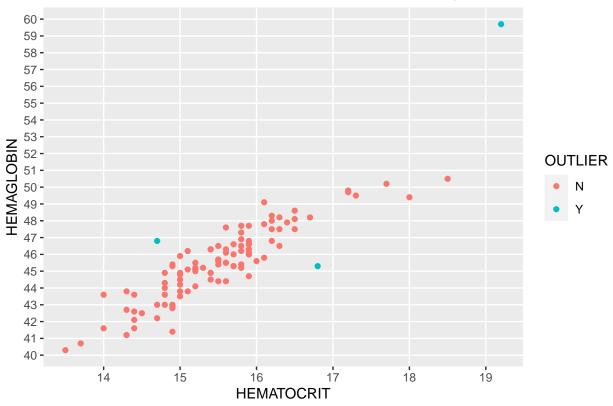


plot(mod1, pch=16, col="blue", lty=1, lwd=2, which=4)



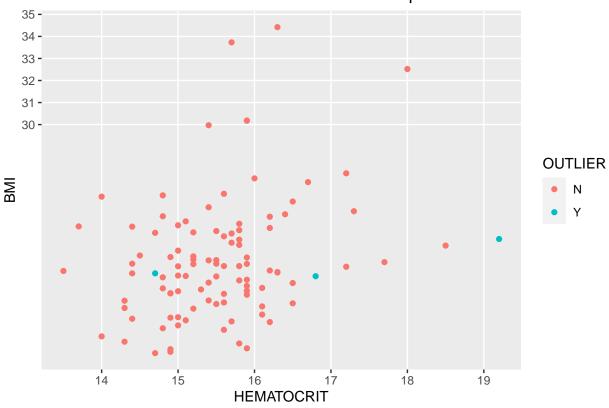
Obs. number Im(HEMATOCRIT ~ HEMAGLOBIN_CENT + FAT_PERC + BMI_VAL)





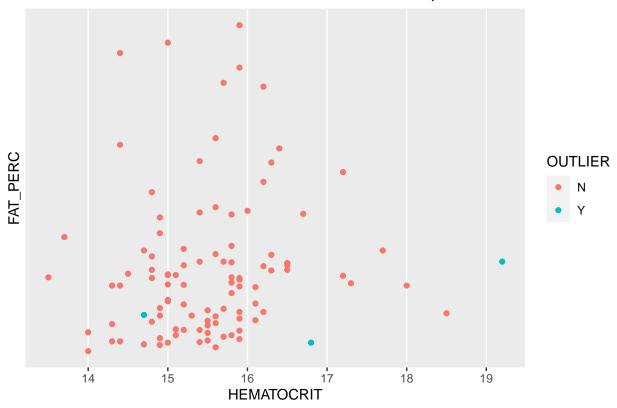
```
qplot(HEMATOCRIT, BMI, data = newdata1, colour = OUTLIER,
main = "BMI and HEMATOCRIT relationship") +
  theme(plot.title = element_text(hjust = 0.5)) +
  scale_y_continuous(breaks = c(30:65), minor_breaks = NULL) +
  scale_x_continuous(breaks = c(10:25), minor_breaks = NULL)
```





```
qplot(HEMATOCRIT, FAT_PERC, data = newdata1, colour = OUTLIER,
main = "FAT_PERC and HEMATOCRIT relationship") +
  theme(plot.title = element_text(hjust = 0.5)) +
  scale_y_continuous(breaks = c(30:65), minor_breaks = NULL) +
  scale_x_continuous(breaks = c(10:25), minor_breaks = NULL)
```

FAT_PERC and HEMATOCRIT relationship



```
newdata2 <- subset(newdata1, OBS != 159 & OBS != 166 & OBS != 169,
                 select=c(HEMAGLOBIN, HEMATOCRIT, BMI, FAT_PERC))
HEMAGLOBIN_CENT = scale(newdata2$HEMAGLOBIN, center=TRUE, scale=FALSE) # center the variable
FAT_CENT = scale(newdata2$FAT_PERC, center=TRUE, scale=FALSE)
BMI_VAL = scale(newdata2$BMI, center=TRUE, scale=FALSE)
mod2 = lm(HEMATOCRIT ~ HEMAGLOBIN_CENT+BMI_VAL+FAT_CENT, data = newdata2)
summary(mod2)
##
## Call:
## lm(formula = HEMATOCRIT ~ HEMAGLOBIN_CENT + BMI_VAL + FAT_CENT,
##
       data = newdata2)
##
## Residuals:
##
      Min
                1Q Median
                                3Q
                                       Max
## -0.7909 -0.2300 -0.0116 0.2202 1.1808
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   15.51212
                               0.03606 430.127
                                                <2e-16 ***
## HEMAGLOBIN_CENT 0.34905
                               0.01727 20.215
                                                 <2e-16 ***
## BMI_VAL
                   0.03701
                               0.01707
                                       2.168
                                                 0.0327 *
## FAT_CENT
                   -0.01968
                               0.01452 - 1.355
                                                 0.1786
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

##

```
## Residual standard error: 0.3588 on 95 degrees of freedom
## Multiple R-squared: 0.8311, Adjusted R-squared: 0.8257
## F-statistic: 155.8 on 3 and 95 DF, p-value: < 2.2e-16
par(mfrow = c(2,2)) # display a unique layout for all graphs
plot(mod2)
                                                   Standardized residuals
                 Residuals vs Fitted
                                                                        Normal Q-Q
                                         810
                                                                                             81<sub>O</sub>
Residuals
                                                         က
                                         600
     0.5
             0
     -1.0
                                      8
                                                                 OCOM
                                                                                           2
             14
                      15
                               16
                                        17
                                                                 -2
                                                                              0
                                                                                     1
                      Fitted values
                                                                     Theoretical Quantiles
Standardized residuals
                                                   Standardized residuals
                   Scale-Location
                                                                  Residuals vs Leverage
                                                                          081
                                         600
                                                         က
                                                                                                 0.5
      1.0
                                                                                0
                                                                                        630
     0.0
                                                                           distance
                                                                                                 0.5
             14
                      15
                               16
                                        17
                                                             0.00
                                                                     0.05
                                                                             0.10
                                                                                      0.15
                                                                                              0.20
                      Fitted values
                                                                          Leverage
AIC(mod1)
## [1] 324.9052
AIC(mod2)
## [1] 83.93676
BIC(mod1)
## [1] 338.0301
BIC(mod2)
## [1] 96.91236
set.seed(123) # setting seed to reproduce results of random sampling
trainingRowIndex <- sample(1:nrow(newdata2), 0.7*nrow(newdata2)) # training and testing: 70/30 split
trainingData <- newdata2[trainingRowIndex, ] # training data</pre>
testData <- newdata2[-trainingRowIndex, ]</pre>
                                                   # test data
modTrain <- lm(HEMATOCRIT ~ HEMAGLOBIN+BMI+FAT_PERC, data=trainingData) # build the model
```

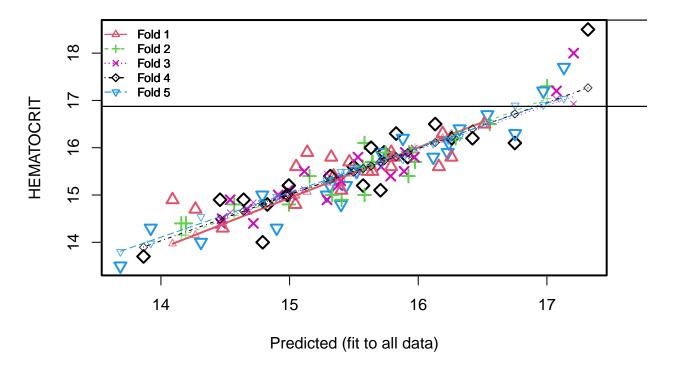
predict <- predict(modTrain, testData) # predicted values</pre>

```
summary(modTrain)
##
## Call:
## lm(formula = HEMATOCRIT ~ HEMAGLOBIN + BMI + FAT_PERC, data = trainingData)
##
## Residuals:
##
      Min
                1Q Median
                                3Q
                                       Max
## -0.7892 -0.2394 -0.0052 0.2120 1.1949
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) -0.95692
                        0.97380 -0.983
                                              0.329
## HEMAGLOBIN
               0.34466
                          0.02058 16.750
                                             <2e-16 ***
## BMI
               0.03922
                           0.02468
                                   1.589
                                              0.117
## FAT PERC
              -0.01435
                           0.01874 -0.766
                                              0.447
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.3691 on 65 degrees of freedom
## Multiple R-squared: 0.8251, Adjusted R-squared: 0.817
## F-statistic: 102.2 on 3 and 65 DF, p-value: < 2.2e-16
act_pred <- data.frame(cbind(actuals=testData$HEMATOCRIT, predicteds=predict)) # actuals_predicteds</pre>
cor(act_pred) # correlation_accuracy
##
                actuals predicteds
              1.0000000 0.9199378
## actuals
## predicteds 0.9199378 1.0000000
head(act_pred, n=10)
##
      actuals predicteds
## 1
        15.9
              15.93254
## 2
        15.2
              15.44810
## 3
        15.9 15.94459
## 10
        15.4 15.37968
              16.23528
## 11
        16.1
## 19
        15.4
              15.17829
## 20
        16.2
              16.27280
## 24
        15.5
              15.89244
## 28
        15.6
               15.53141
## 35
        13.7
               13.91348
min_max <- mean(apply(act_pred, 1, min) / apply(act_pred, 1, max))</pre>
print(min_max) # show the result
## [1] 0.982513
mape <- mean(abs((act_pred$predicteds - act_pred$actuals))/act_pred$actuals)</pre>
print(mape) # show the result
## [1] 0.01774838
kfold <- CVlm(data = newdata2, form.lm = formula(HEMATOCRIT ~ HEMAGLOBIN+BMI+FAT_PERC), m=5,
                   dots = FALSE, seed=123, legend.pos="topleft",
                   main="Cross Validation; k=5",
```

plotit=TRUE, printit=FALSE)

```
## Warning in CVlm(data = newdata2, form.lm = formula(HEMATOCRIT ~ HEMAGLOBIN + :
##
## As there is >1 explanatory variable, cross-validation
## predicted values for a fold are not a linear function
## of corresponding overall predicted values. Lines that
## are shown for the different folds are approximate
```

Cross Validation; k=5



attr(kfold, 'ms')

[1] 0.1469749