

IMPROVING OPTIMALITY AND SPEED OF GREEDY GROUP RECURSION ALGORITHM

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ABSTRACT

Recently (Liu et al., 2025) has presented efficient algorithm - Greedy Group Recursion (GGR) - for reordering the rows and the fields within each row of an input table to maximize key-value (KV) cache reuse when performing LLM serving. In this paper, we propose several adjustments to GGR algorithm that can improve optimality of the solution and reduce its execution time.

1 INTRODUCTION

There has been growing research on LLM inference optimization. In particular, recent work (Liu et al., 2025; Cheng et al., 2025) presents solutions to optimize relational data analytics workloads for offline LLM inference. It proposes Greedy Group Recursion (GGR), an approximate algorithm that leverages functional dependencies (such as primary and foreign key relationships from the data schema) and table statistics, which are readily available in many databases and analytics systems, to reduce the search space.

The GGR algorithm is defined by a specification in Algorithm 1.

REFERENCES

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Algorithm 1 Greedy Group Recursion (GGR)

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1: Input: Table  $T$ , Functional Dependency  $FD$ 
2: Output: Prefix Hit Count  $S$ , Reordered List of Tuples  $L$ 

3: function HITCOUNT( $v, c, T, FD$ )
4:    $R_v \leftarrow \{i \mid T[i, c] = v\}$ 
5:    $\text{inferred\_cols} \leftarrow \{c' \mid (c, c') \in FD\}$ 
6:    $\text{inferred\_vals} \leftarrow \{T[R_v[0], c'] \mid c' \in \text{inferred\_cols}\}$ 
7:    $\text{tot\_len} = \text{len}(v)^2 + \sum_{c' \in \text{inferred\_cols}} \left( \frac{\sum_{r \in R_v} \text{len}(T[r, c'])}{|R_v|} \right)^2$ 
8:   return  $\text{tot\_len} \times (|R_v| - 1), [c] + \text{inferred\_cols}, \text{inferred\_vals}$ 
9: end function

10: function GGR( $T, FD$ )
11:   if  $|T|_{\text{rows}} = 1$  then
12:     return 0,  $[T[1]]$ 
13:   end if
14:   if  $|T|_{\text{cols}} = 1$  then
15:      $S \leftarrow \sum_{v \in \text{distinct}(T[:, 1])} \text{HITCOUNT}(v, 1, T)$ 
16:     Return  $S, \text{sort}([T[i] \mid i \in 1 \dots |T|_{\text{rows}}])$ 
17:   end if
18:    $\text{max\_HC}, b\_v, b\_c, b\_cols, b\_vals \leftarrow -1, \text{None}, \text{None}, [], []$ 
19:   for  $c \in \text{columns}(T), v \in \text{distinct}(T[:, c])$  do
20:      $HC, cols, vals \leftarrow \text{HITCOUNT}(v, c, T, FD)$ 
21:     if  $HC > \text{max\_HC}$  then
22:        $\text{max\_HC}, b\_v, b\_c, b\_cols, b\_vals = HC, v, c, cols, vals$ 
23:     end if
24:   end for
25:    $R\_v \leftarrow \{i \mid T[i, b\_c] = b\_v\}$ 
26:    $A\_HC, L\_A \leftarrow \text{GGR}(T[\text{rows} \setminus R\_v, \text{cols}], FD)$ 
27:    $B\_HC, L\_B \leftarrow \text{GGR}(T[R\_v, \text{cols} \setminus b\_cols], FD)$ 
28:    $C\_HC, \_ \leftarrow \text{HITCOUNT}(b\_v, b\_c, T, FD)$ 
29:    $S \leftarrow A\_HC + B\_HC + C\_HC$ 
30:    $L \leftarrow [[b\_v] + b\_vals + L\_B[i] \mid i \in 1 \dots |R\_v|] + L\_A$ 
31:   return  $S, L$ 
32: end function

33: return GGR( $T, FD$ )

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