# Project Title: System Verification and Validation Plan

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# 1 Revision History

| Date       | Version | Notes  |
|------------|---------|--|
| 2018-10-13 | 1.0     | Creation of first draft for VnV plan presentation.   |
| 2018-10-20 | 1.1     | Edit of 1.0. I considered all of the feed-back from my presentation and made necessary changes. I also prepared the document for submission. |
| 2018-10-22 | 1.2     | Edit of 1.1. Removed comments, updated test cases, added references, improved writing and added test-NFR2c.                                  |
| 2018-10-23 | 1.3     | Edit of 1.2. Minor corrections and revisions.  |

# 2 Symbols, Abbreviations and Acronyms

| symbol | description                |
|--------|----------------------------|
| Τ      | Test                       |
| R      | Requirement                |
| NFR    | Non-functional Requirement |

# Contents

| 1       | Rev            | vision History                                   | i  |  |  |  |  |  |  |  |
|---------|----------------|--|----|--|--|--|--|--|--|--|
| 2       | Syn            | nbols, Abbreviations and Acronyms                | ii |  |  |  |  |  |  |  |
| 3       | Ger            | General Information                              |    |  |  |  |  |  |  |  |
|         | 3.1            | Summary  | 1  |  |  |  |  |  |  |  |
|         | 3.2            | Objectives                                       | 1  |  |  |  |  |  |  |  |
|         | 3.3            | References                                       | 2  |  |  |  |  |  |  |  |
| 4       | Pla            | $\mathbf{n}$                                     | 2  |  |  |  |  |  |  |  |
|         | 4.1            | Verification and Validation Team                 | 2  |  |  |  |  |  |  |  |
|         | 4.2            | SRS Verification Plan                            | 3  |  |  |  |  |  |  |  |
|         | 4.3            | Design Verification Plan                         | 3  |  |  |  |  |  |  |  |
|         | 4.4            | Implementation Verification Plan                 | 3  |  |  |  |  |  |  |  |
|         | 4.5            | Software Validation Plan                         | 3  |  |  |  |  |  |  |  |
| 5       | Sys            | System Test Description                          |    |  |  |  |  |  |  |  |
|         | 5.1            | Tests for Functional Requirements                | 3  |  |  |  |  |  |  |  |
|         | 5.2            | Tests for Nonfunctional Requirements             | 5  |  |  |  |  |  |  |  |
|         | 5.3            | Traceability Between Test Cases and Requirements | 7  |  |  |  |  |  |  |  |
| 6       | Sta            | tic Verification Techniques                      | 7  |  |  |  |  |  |  |  |
| 7       | Apj            | Appendix   |    |  |  |  |  |  |  |  |
|         | 7.1            | Symbolic Parameters                              | 10 |  |  |  |  |  |  |  |
|         | 7.2            | Usability Survey Questions                       | 10 |  |  |  |  |  |  |  |
|         | 7.3            | Data Input Tables                                | 11 |  |  |  |  |  |  |  |
|         | 7.4            | Software Verification Checklist                  | 12 |  |  |  |  |  |  |  |
|         | 7.5            | Correct Matrix Form                              | 13 |  |  |  |  |  |  |  |
| ${f L}$ | $\mathbf{ist}$ | of Tables  |    |  |  |  |  |  |  |  |
|         | 1              | Traceability Between Test                        | 7  |  |  |  |  |  |  |  |
|         | 2              | Prescribed input for testing Rin                 | 11 |  |  |  |  |  |  |  |
|         | 3              | Prescribed input for Rin                         | 12 |  |  |  |  |  |  |  |

# List of Figures

This document discusses the verification and validation requirements for SpecSearch. The Project Management Body of Knowledge (PMBOK) guide provides unambigious definitions for verification and validation. PMBOK defines verification as "the evaluation of whether or not a product, service, or system complies with a regulation, requirement, specification, or imposed condition. It is often an internal process."

PMBOK defines validation as "the assurance that a product, service, or system meets the needs of the customer and other identified stakeholders. It often involves acceptance and suitability with external customers" [Project Management Institute, 2017]. After reading this document one should be able to create and run test cases to verify and validate SpecSearch.

## 3 General Information

## 3.1 Summary

The software that is going to be tested is called SpecSearch. SpeacSearch will search for the spectrum (set of eigenvalues) of a particular lax equation from a lax pair that is compatibilible with solutions to the Non-Linear Schrodinger (NLS) Equation. SpecSearch will also use the spectral information to determine the stability of the solutions. Refer to the instance models in the SRS for more details.

# 3.2 Objectives

The qualities that are most important for SpecSearch are highlighted in this section. Many of these qualities are also presented in the SRS.

My supervisor and I intend to use this program as a tool to search for the continuous spectrum of the previously mentioned spectral problem. Spec-Search will only provide the approximate location of the spectrum and a finite number of elements in the spectrum. We will use this output as a guide in analytically solving for the entire continuous spectrum. Therefore, the code should be reliable and accurate within my supervisor's standards.

There are various numerical methods that can be used to approximate the

derivatives of the eigenfunctions [Graselli and Pelinovksy, 2007]. My supervisor and I intend to experiment with these different methods in an attempt to create a more accurate picture of the spectrum. Therefore, it is important that SpecSeach is maintainable and manageable.

SpecSearch will also be used by a team of researchers studying modulated wave packets and rogue waves. These users may not have a strong software developing background. Therefore, it is important that the code is easy to use and has a simple user interface.

The objectives are summarized in the following points for easy reference. The objectives are to:

- Build confidence in software correctness.
- Ensure maintainability and manageability
- Satisfy the requirements of my thesis supervisor and those outlined in the SRS.
- Verify usability.

#### 3.3 References

- Bernard Deconinck and Benjamin L.Segal. The stability spectrum for elliptic solutions to the focusing NLS equation. PhysicaD, 2017.
- Robert White. System Requirements Specification for SpecSearch. Github, 2018.
- Matheus Grasselli and Dmitry Pelinovsky. Numerical Mathematics. Jones and Bartlett Learning, 2007.

## 4 Plan

#### 4.1 Verification and Validation Team

The verification and validation team consists of my thesis supervisor, Dr. Dmitry Pelinovsky, and I.

#### 4.2 SRS Verification Plan

The SRS verification plan consists of feedback from Dr. Dmitry Pelinovsky (supervisor), Dr. Spencer Smith and CAS 741 classmates. My supervisor will provide feedback regarding mathematical theory, model assumptions, constraints and research goals. Feedback from classmates and Dr. Smith will criticize the document outline, readability and requirements.

## 4.3 Design Verification Plan

The design verification plan will simply involve inspection of the software by my thesis supervisor.

# 4.4 Implementation Verification Plan

The implementation verification plan consists of two parts. The first part is a software verification checklist. The checklist will be completed by researchers, Dr. Pelinovksy and I. The checklist verifies that basic software features have been implemented successfully. For example, it checks if the user was able to fufill their responsibilities outlined in the SRS. This checklist can be found in the appendix (7.4).

The second part involves running the software tests outlined in sections 5 and 6. Unit testing will also be performed.

#### 4.5 Software Validation Plan

This section does not apply to SpecSearch.

# 5 System Test Description

# 5.1 Tests for Functional Requirements

1. test-Rin1

Initial State: -

Input: Table 2 in Appendix 7.3.

Output: Error or pass message.

How test will be performed: Combinations of inputing non-numerical values as input (such as letters), or numerical values outside of their respective constraints, will be considered. A successful test in these instances will be an error message.

I will also test cases with each variable in the input having an acceptable numerical value. A successful test in these cases will be a pass message.

#### 2. test-Rfind1

Initial State: -

Input: Table 2 in Appendix 7.3 (Similar to test-Rin1).

Output: Size of spectrum array

How the test will be performed: Passing inputs from test-Rin1 should produce 4n eigenvalues. Unsuccessful cases from test-Rin1 should produce no eigenvalue array or an empty eigenvalue array. We are not testing for accuracy in this test.

#### 3. test-Rcon1

Initial State: -

Input: Table 2 in Appendix 7.3 (Similar to test-Rin1).

Output: Approximated Spectrum (Connected or disconnected)

How test will be performed: This test will check to see if there is a sufficient amount of points between the tagged portions of the spectrum. Tagged portions are the explicitly calculated eigenvalues from the previous test. The spectrum array should have 2\*m-1 approximated values between these "tagged portions", where m is the scaling parameter. Failed test cases from test-Rin1 should have no data for this section. We are not testing for accuracy in this test.

The scaling parameter has not been studied yet. It will be incorporated in the final draft of the documents.

#### 4. test-Rplt

Initial State: -

Input: Table 2 in Appendix 7.3 (Similar to test-Rin1).

Output: A plot of the spectrum.

How test will be performed: This will involve visual inspection by my supervisor to see if the spectrum plot is adequate.

There should be no plot for the failed test cases in test-Rin1.

#### 5. test-Rstl

Initial State: -

Input: Table 2 in Appendix 7.3 (Similar to test-Rin1).

Output: Binary Variable (Verification of stability)

How test will be performed: The stability results will be compared with the stability analysis in [Deconinck and Segal, 2017]. My supervisor and I are still working on test cases for Rstl.Test-Rstl will be updated in the final draft of the documents.

# 5.2 Tests for Nonfunctional Requirements

#### 1. test-NFR1

Type: Static Initial State: -

Input/Condition: SpecSearch MATLAB code

How test will be performed: The software will be manually read by Dr. Pelinovksy and I to see if there is a more effective code structure to allow implementation of new numerical algorithms.

#### 2. test-NFR2a

Type: Manual Initial State: -

Input: Integer n (same as test-Rin1).

Output: Operator Matrix.

How test will be performed: Test-NFR2a will check if the operator matrix is of the correct form. See Appendix 7.5 for more detail. The values from table 2 will be used to inspect A1.

#### 3. test-NFR2b

Type: Manual Initial State: -

Input: Table 2 in Appendix 7.3 (Similar to test-Rin1).

Output: Spectrum.

How test will be performed: The output will be tested against the boundary value eigen-values derived analytically in Deconinck and Segal. See details below table 2 of appendix 7.3.

#### 4. test-NFR2c

Type: Usability Survey (see appendix 7.2)

How test will be performed: The survey will be administered to the future users of SpecSearch. Feedback from the survey will be considered when updating SpecSearch. The survey is in appendix 7.2.

## 5.3 Traceability Between Test Cases and Requirements

|            | Rin | Rfind | Rcon | Rplt | Rstl | NFR1 | NFR2 |
|------------|-----|-------|------|------|------|------|------|
| test-Rin   | X   |       |      |      |      |      |      |
| test-Rfind |     | X     |      |      |      |      |      |
| test-Rcon  |     |       | X    |      |      |      |      |
| test-Rplt  |     |       |      | X    |      |      |      |
| test-Rstl  |     |       |      |      | X    |      |      |
| test-NFR1  |     |       |      |      |      | X    |      |
| test-NFR2a |     |       |      |      |      |      | X    |
| test-NFR2b |     |       |      |      |      |      | X    |
| test-NFR2c |     |       |      |      |      |      | X    |

Table 1: Traceability Between Test

# 6 Static Verification Techniques

- Code inspection: I will go through the code to see if each part is correct with respect to the mathematical theory. In particular I will ensure that:
  - Variables are being used in the right context.
  - Functions from other packages are being used in the right context. Some packages have different standards for constants. For instance, one of the complete elliptic integral functions in matlab does not square the inputted variable. Theoretical convention dictates that this constant should be squared.
  - The dimensions of the vectors and matrices are appropriate. For example, multiplication of row with column versus column with row.
  - Equations are translated correctly into matlab syntax.
- Code walkthrough: My supervisor and I will go through the code together to ensure that:

- I correctly implemented the mathematical theory and numerical algorithms.
- $\,-\,$  I made the code manageable and maintainable for future use.

# References

- [1] Project Management Institute. A Guide to the Project Management Body of Knowledge (PMBOK Guide)—Sixth Edition. Project Management Institute, 2017.
- [2] Caswell and Johnston. Design Verification. University of Calary. 2017.
- [3] Bernard Deconinck and Benjamin L.Segal. The stability spectrum for elliptic solutions to the focusing NLS equation. PhysicaD, 2017.
- [4] Robert White. System Requirements Specification for SpecSearch. Github, 2018.
- [5] Matheus Grasselli and Dmitry Pelinovsky. Numerical Methods. Jones and Bartlett Learning; 1 edition, Aug. 13 2007

# 7 Appendix

# 7.1 Symbolic Parameters

# 7.2 Usability Survey Questions

- How long did it take before you could run the software? How many attempts at running SpecSeach did it take before you understood how to properly use it and interpret the output?
- Was this program useful for your research and were you able to interpret the results?
- What aspects of this software do you feel need improvement?
- How does this program compare with other software that finds this particular spectrum?
- Was it clear how and where to input the variables?
- Were the plots and stability results clear?

## 7.3 Data Input Tables

The following data table is for test-Rin1. An "X" indicates no-input or incorrect input. Incorrect input is anything that is non-numerical (ie letters or symbols).

| Input ID | a  | b  | k     | n   | Result |
|----------|----|----|-------|-----|--------|
| I1       | 1  | 1  | 0.9   | 100 | Pass   |
| I2       | X  | 1  | 0.9   | 10  | Error  |
| I3       | 1  | X  | 0.9   | 100 | Error  |
| I4       | 1  | 1  | X     | 100 | Error  |
| I5       | 1  | 1  | 0.9   | X   | Error  |
| I6       | 1  | 1  | 1     | 1.2 | Error  |
| I7       | 1  | 1  | 1.2   | 100 | Error  |
| I8       | 1  | -1 | 0.9   | 100 | Error  |
| I9       | -1 | 2  | 0.9   | 100 | Pass   |
| I10      | 1  | 2  | 0.99  | 100 | Pass   |
| I11      | 1  | 3  | 0.99  | 500 | Pass   |
| I13      | 1  | 1  | 0     | 150 | Pass   |
| I14      | -1 | 2  | 0.9   | 330 | Pass   |
| I15      | 1  | 1  | 0.99  | 170 | Pass   |
| I16      | 1  | 5  | 0.999 | 590 | Pass   |
| I17      | 1  | 1  | 0     | 200 | Pass   |

Table 2: Prescribed input for testing Rin

The following table outlines the boundary value test cases that can be verified from previous literature. A 'V' means that the parameter is free to vary.

For these cases all of the eigenvalues, except for four of them, will be purely imaginary. The remaing four have the form:  $\lambda = \frac{\pm}{2}a(1+\sqrt{1-k^2})$  and  $\lambda = \frac{\pm}{2}a(1-\sqrt{1-k^2})$  for B1 (see table 3).

As for B2, the eigenvalues will have the form:  $\lambda = \frac{1}{2}a(\frac{\pm}{k} + i\sqrt{1-k^2})$  and  $\lambda = \frac{1}{2}a(\frac{\pm}{k} - i\sqrt{1-k^2})$ . [Deonick and segal 2017]

| Boundary ID | a                      | b        | k |
|-------------|------------------------|----------|---|
| B1          | $\sqrt{b}$             | $a^2$    | V |
| B2          | $\sqrt{\frac{b}{k^2}}$ | $a^2k^2$ | V |
| В3          | V                      | V        | 0 |

Table 3: Prescribed input for Rin

The plan is to run B1 with a=b=1 and k=0.999. B2 will be run with the same input. The expected eigenvalues were previously mentioned.

#### 7.4 Software Verification Checklist

- Does the software allow the user to fufill their responsibilities (as outlined in the SRS)?
- Does the software fufill its intended responsibilities (see SRS)?
- Was the intended user able to use the software and interpret the output for their research purposes?
- Are any of the system constraints violated (see SRS)?

#### 7.5 Correct Matrix Form

test-NFR2a will ensure that the matrix for which the eigen values are calculated, E, is of the correct form. For any given input n, the matrix is 4n by 4n. It is of the form [A1A2;A2(-A1)] where A1,A2 is the first row and A2-A1 is the second row. A1 and A2 are matrices. A2 is a diagonal 2n by 2n matrix and A1 is 2n by 2n and defined as follows: A1(i,j) = n/2 for (1,2),(2,3),... (2n-1,2n) and A1(i,j)=-n/2 for (2,1),(3,2) ... (2n,2n-1). A1(1,2n)=-n/2 and A1(2n,1)=n/2. //

For example for arbitrary n it should have the form:

$$A1 = \begin{bmatrix} 0 & \frac{n}{2} & 0 & 0 & 0 & -\frac{n}{2} \\ -\frac{n}{2} & 0 & \frac{n}{2} & 0 & 0 & 0 \\ 0 & -\frac{n}{2} & 0 & \frac{n}{2} & 0 & 0 \\ 0 & 0 & -\frac{n}{2} & 0 & \frac{n}{2} & 0 \\ 0 & 0 & 0 & -\frac{n}{2} & 0 & \frac{n}{2} \\ \frac{n}{2} & 0 & 0 & 0 & -\frac{n}{2} & 0 \end{bmatrix}$$