

# Module Interface Specification for SpecSearch

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# 1 Revision History

Date	Version	Notes
2018-11-09	1.0	Creation of first draft for presentation.

## 2 Symbols, Abbreviations and Acronyms

See SRS Documentation at [\[give url —SS\]](#)

[\[Also add any additional symbols, abbreviations or acronyms —SS\]](#)

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### 3 Introduction

The following document details the Module Interface Specifications for SpecSearch. SpecSearch is scientific computing software that computes and plots the spectrum of a matrix operator that appears in a LAX pair that is compatible for solutions of the Non-Linear Schrödinger (NLS) equation. Consequently, this spectrum carries useful information regarding the stability of solutions to the NLS equation. Physicists are interested in this spectrum as the NLS equation models many physical phenomena, such as rogue waves or modulated wave packets. Mathematicians are interested in the analytical behaviour of this spectrum.

Complementary documents include the System Requirement Specifications and Module Guide. The full documentation and implementation can be found at [https://github.com/whitere123/CAS741\\_REW](https://github.com/whitere123/CAS741_REW).

The purpose of this document is to describe the intended behaviour of the access routines for SpecSearch's modules. In particular, mathematical notation will be used to describe the input/output relationships and external behaviour of the modules. The MIS is still abstract since it does not cover implementation of the modules and does not outline any code.

### 4 Notation

The structure of the MIS for modules comes from Hoffman and Strooper (1995), with the addition that template modules have been adapted from Ghezzi et al. (2003). The mathematical notation comes from Chapter 3 of Hoffman and Strooper (1995). For instance, the symbol  $:=$  is used for a multiple assignment statement and conditional rules follow the form  $(c_1 \Rightarrow r_1 | c_2 \Rightarrow r_2 | \dots | c_n \Rightarrow r_n)$ .

The following table summarizes the primitive data types used by Program Name.

Data Type	Notation	Description
character	char	a single symbol or digit
integer	$\mathbb{Z}$	a number without a fractional component in $(-\infty, \infty)$
natural number	$\mathbb{N}$	a number without a fractional component in $[1, \infty)$
real	$\mathbb{R}$	any number in $(-\infty, \infty)$
complex	$\mathbb{C}$	any number $x + iy$ with $x \in \mathbb{R}$ , $y \in \mathbb{R}$ and $i^2 = -1$ .

The specification of Program Name uses some derived data types: sequences, strings, and tuples. Sequences are lists filled with elements of the same data type. Strings are sequences of characters. Tuples contain a list of values, potentially of different types. In addition, Program



Name uses functions, which are defined by the data types of their inputs and outputs. Local functions are described by giving their type signature followed by their specification.

## 5 Module Decomposition

The following table is taken directly from the Module Guide document for this project.

Level 1	Level 2
Hardware-Hiding	
Behaviour-Hiding	Input Parameters Output Format Spectrum Matrix Exact Eigenvalue Equations Spectrum Error Equation Numerical Parameters Control
Software Decision	Sequence Data Structure Eigenvalue and Eigenvector Solver Diagonal Matrix Generator Elliptic Integral Elliptic Functions Plotting Linspace

Table 1: Module Hierarchy

## 6 MIS of Input Parameters

The secrets of this module are the data structure for input parameters and methods for verifying input.

### 6.1 Module

InParams

### 6.2 Uses

-

### 6.3 Syntax

Name	In	Out	Exceptions
Call_params	$k : \mathbb{R}$ $N : \mathbb{N}$	-	NonNumericalError
Verify_params	-	-	BadkRange, BadNRange
k	-	$\mathbb{R}$	-
N	-	$\mathbb{N}$	-

### 6.4 Semantics

#### 6.4.1 State Variables

$k : \mathbb{R}$

$N : \mathbb{N}$

#### 6.4.2 Environment Variables

InputParameters: The two values entered by the user.

#### 6.4.3 Assumptions

- Call\_params is called before the values of any state variables will be accessed.
- The user inputs the state variables in the following order:  $(k, N)$

#### 6.4.4 Access Routine Semantics

InParams.k():

- output:  $out = k$

- exception: None

InParams.N():

- output:  $out = N$
- exception: None

Call\_Params():

- transition: The data is read sequentially from the command line. The data are separated by the return key. This data is used to populate the previously mentioned state variables.
- exception: If non-numerical data is entered.

Verify\_Params():

- exception: exc:=

$\neg(k \in (0, 1)) \Rightarrow \text{BadkRange}$

$\neg(N \in \mathbb{N}) \Rightarrow \text{BadNRange}$

#### 6.4.5 Local Functions

None

## 7 MIS of Output Format

The secret of this module is the format and structure of the output data.

### 7.1 Module

OutForm

### 7.2 Uses

Eigenvalue solver, Spectrum Error Equations and Numerical Parameters.

Name	In	Out	Exceptions
capture	$D_j : \mathbb{R}^{2n}$ $Er_j : \mathbb{R}^2$ $V_j : \mathbb{C}^{4n \times 4n}$ $Vl_j : \mathbb{R}^{4n}$	Spectrum	- - - -
Spectral	-	$\mathbb{C}^{4n(4n+2)}$	-
D	-	$\mathbb{R}^{2n}$	-
Er	-	$\mathbb{R}$	-

### 7.3 Semantics

The  $j$  refers to the  $j^{th}$  numerical method.  $j \in O(1), O(4), cheb$ .

#### 7.3.1 State Variables

$Spectral_j : \mathbb{C}^{4n(4n+2)}$   
 $D_j \in \mathbb{R}^{2n}$   
 $Er_j \in \mathbb{R}^2$

#### 7.3.2 Environment Variables

None.

#### 7.3.3 Assumptions

- Eigenvalue solver, Spectrum Error Equations and Numerical Parameters are called and their values are temporarily stored prior to OutForm.

### 7.3.4 Access Routine Semantics

OutForm.Dj():

- output:  $out = D_j$
- exception: None

OutForm.Erj():

- output:  $out = Er_j$
- exception: None

OutForm.Spectralj():

- output:  $out = Spectral_j$
- exception: None

capture():

- Transition: The data  $(D_j, Er_j, V_j, Vl_j)$  will be captured from the other modules and then stored into *Spectral* for convenience. Spectral is a data structure with four cell components. The first four cells are  $4n$  by  $4n + 1$  matrices created as follows: the  $4n$  by 1 vector of eigenvalues,  $Vl_j$ , will be transposed and turned into the  $(4n + 1)^{th}$  row of spectral. The previous  $4n$  rows of spectral will be the matrix,  $V_j$ , composed of the eigenvectors for the  $j$  numerical method. Each column of  $V_j$  is an eigenvector from the  $j$  numerical method. D will be stored in Spectral as the fourth cell component.
- Exception: None

### 7.3.5 Local Functions

None

## 8 MIS of Spectrum Matrix

The structure of the spectrum matrix, its data entries, how it is created, and the numerical method for approximating its eigenfunctions are the secrets of this module.

### 8.1 Module

SpecMat

### 8.2 Uses

This module uses Numerical Parameters.

### 8.3 Syntax

Name	In	Out	Exceptions
create	$n : \mathbb{N}$	SpecMat01	-
	$h : \mathbb{R}$	SpecMat04	-
	$elipdn : \mathbb{R}^{2n}$	SpecCheb	-
	$k : \mathbb{R}$		-
SpecMatO1	-	$\mathbb{R}^{4n \times 4n}$	-
SpecMatO4	-	$\mathbb{R}^{4n \times 4n}$	-
SpecCheb	-	$\mathbb{R}^{4n \times 4n}$	-

### 8.4 Semantics

#### 8.4.1 State Variables

$SpecCheb : \mathbb{R}^{4n \times 4n}$

$SpecMat04 : \mathbb{R}^{4n \times 4n}$

$SpecMat01 : \mathbb{R}^{4n \times 4n}$

#### 8.4.2 Assumptions

- All of the numerical parameters are calculated correctly and used as arguments in create.

#### 8.4.3 Access Routine Semantics

SpecMat.SpecMatO1:

- output:  $out = SpecMatO1$
- exception: None

SpecMat.SpecMatO4:

- output: out = SpecMatO4
- exception: None

SpecMat.SpecFour:

- output: out = SpecCheb
- exception: None

SpecMat.create():

- transition: The data (n,h,elipdn,k) will be captured from the other modules and used to create the spectral matrices. There will be three instances of the spectral matrix. Each corresponds to a different numerical algorithm for approximating the eigenfunction derivatives. Top top left and bottom right sections of the matrices are diagonal matrices with elements equal to the elipdn function evaluated at points in the discretized domain. The remain parts of the matrix are coefficients such that when multiplied by the eigenfunctions will create the appropriate approximation of the derivatives.
- exception: None

## 9 MIS of Exact Eigenvalue Equations

The secrets of this module are the analytical expressions for the two real eigenvalues.

### 9.1 Module

TheorEigenValues

### 9.2 Uses

This module uses input parameters.

### 9.3 Syntax

Name	In	Out	Exceptions
$\lambda_{O1}$	$k \in \mathbb{R}$	$\mathbb{R}$	-
$\lambda_{O2}$	$k \in \mathbb{R}$	$\mathbb{R}$	-

### 9.4 Semantics

#### 9.4.1 State Variables

None

#### 9.4.2 Environment Variables

None

#### 9.4.3 Assumptions

- These are the eigenvalues computed from segal et al. Refer to (segal) for more details regarding assumptions.

#### 9.4.4 Access Routine Semantics

*lambda<sub>O1</sub>*:

- output:  $\frac{1}{2}(1 + \sqrt{1 - k^2})$
- exception: None

*lambda<sub>O2</sub>*

- output:  $\frac{1}{2}(1 - \sqrt{1 - k^2})$
- exception: None



## 10 MIS of Spectrum Error Equation

The secret of this module is the equation for error between exact and approximated eigenvalues.

### 10.1 Module

ErrCalc

### 10.2 Uses

This module uses Exact Eigenvalue equations and Eigenvalue solver.

### 10.3 Syntax

Name	In	Out	Exceptions
$\lambda_O1$	-	$\mathbb{R}$	-
$\lambda_O2$	-	$\mathbb{R}$	-
$\lambda_C1$	-	$\mathbb{R}$	-
$\lambda_C2$	-	$\mathbb{R}$	-
$Err1$	$\lambda_O1 : \mathbb{R}$ $\lambda_C1 : \mathbb{R}$	$\mathbb{R}$	- -
$Err2$	$\lambda_C2 : \mathbb{R}$ $\lambda_C2 : \mathbb{R}$	$\mathbb{R}$	- -

### 10.4 Semantics

#### 10.4.1 State Variables

$\lambda_O1 : \mathbb{R}$   
 $\lambda_O2 : \mathbb{R}$   
 $\lambda_C1 : \mathbb{R}$   
 $\lambda_C2 : \mathbb{R}$

#### 10.4.2 Environment Variables

None

#### 10.4.3 Assumptions

- These are the eigenvalues computed from segal et al. Refer to (segal) for more details regarding assumptions.

#### 10.4.4 Access Routine Semantics

*Err1:*

- output:  $|\lambda_O1 - \lambda_C1|$
- exception: None

*Err2*

- output:  $|\lambda_O2 - \lambda_C2|$
- exception: None

*ErrCalc. $\lambda_O1$ :*

- output:  $\text{out} = \lambda_O1$
- exception: None

*ErrCalc. $\lambda_O2$ :*

- output:  $\text{out} = \lambda_O2$
- exception: None

*ErrCalc. $\lambda_C1$ :*

- output:  $\text{out} = \lambda_C1$
- exception: None

*ErrCalc. $\lambda_C2$ :*

- output:  $\text{out} = \lambda_C2$
- exception: None

## 11 MIS of Numerical Parameters

The secrets of this module are the range of the eigenfunction domain, points in the periodic domain and equation for the numerical scaling factor that computes the eigenfunction derivatives.

### 11.1 Module

Numpars

### 11.2 Uses

This module uses Elliptic Functions, Diagonal Matrix, linspace, Elliptic Integral and input parameters.

### 11.3 Syntax

Name	In	Out	Exceptions
CreateVars	$k : \mathbb{R}$ $N : \mathbb{N}$	$xend : \mathbb{R}$ $Domain : \mathbb{R}^{2N}$ $ellipj : \mathbb{R}^{2N}$ $ellipMAT : \mathbb{R}^{2N \times 2N}$	-
xend	-	$\mathbb{R}$	-
Domain	-	$\mathbb{R}^{2N}$	-
ellipjdn	-	$\mathbb{R}^{2N}$	-
ellipjMAT	-	$\mathbb{R}^{2N \times 2N}$	-
h	-	$\mathbb{R}$	-

### 11.4 Semantics

#### 11.4.1 State Variables

$k : \mathbb{R}$   
 $Domain : \mathbb{R}^{2N}$   
 $ellipj : \mathbb{R}^{2N}$   
 $ellipMAT : \mathbb{R}^{2N \times 2N}$

#### 11.4.2 Environment Variables

None

### 11.4.3 Assumptions

- Input parameters is called before Numerical parameters.
- Input parameters does not throw an exception.

### 11.4.4 Access Routine Semantics

*Numpars.xend:*

- output: *xend*
- exception: None

*Numpars.Domain*

- output: *Domain*
- exception: None

*Numpars.ellipjdn:*

- output: *out = ellipjdn*
- exception: None

*Numpars.ellipjMAT:*

- output: *out = ellipjMAT*
- exception: None

*Numpars.h:*

- output: *out = h*
- exception: None

*Numpars.CreateVars:*

- transition: The data  $(N, k)$  will be captured from the input parameters and used to create the state variables.  $k$  will be inputted as an argument into the elliptic integral module. The resulting integral is equal to *xend*.  
The domain is created using linspace. The endpoint arguments of linspace are  $-xend$  and *xend*, respectively. The distance between partition points in the resulting domain is  $h = \frac{xend}{N}$ . Ellipjdn is derived from computing the ellipjdn value of each point in Domain. EllipjMAT is a diagonal matrix whose diagonal is Ellipjdn.
- exception: None

## 12 MIS of Eigenvalue and Eigenvector Solver

The secret of this module is the numerical algorithm for calculating the eigenvalues and eigenvectors of an  $n$  by  $n$  matrix.

### 12.1 Module

eig (<https://www.mathworks.com/help/matlab/ref/eig.html>)

### 12.2 Uses

This module uses Spectrum Matrix.

### 12.3 Syntax

Name	In	Out	Exceptions
solver	$A : \mathbb{C}^{n \times n}$	$\mathbb{C}^n \times \mathbb{R}^{n \times n}$	NotsquareMat

### 12.4 Semantics

#### 12.4.1 State Variables

None.

#### 12.4.2 Environment Variables

None.

#### 12.4.3 Assumptions

- The input is a square matrix.

#### 12.4.4 Access Routine Semantics

eig():

- output: out:=  $\lambda$  and  $\bar{v}$  such that:  
 $A\bar{v} = \lambda\bar{v}$   
 $\bar{v} : \mathbb{C}^n$  and  $\lambda : \mathbb{C}$
- exception: exce:=  $A \notin \mathbb{R}^{n \times n} \Rightarrow \text{NotSquareMatrix}$

## 13 MIS of Diagonal Matrix

The secrets of this module are the numerical algorithm for creating an  $n$  by  $n$  diagonal matrix from an  $n$  by 1 vector and the numerical algorithm for creating an  $n$  by 1 vector from an  $n$  by  $n$  diagonal matrix.

### 13.1 Module

diag (<https://www.mathworks.com/help/matlab/ref/diag.html>)

### 13.2 Uses

This module uses Numerical Parameters.

### 13.3 Syntax

Name	In	Out	Exceptions
solver	$A$ : Diagonal $n$ by $n$ matrix	$\mathbb{C}^n$	NotDiagMat
solver	$v : \mathbb{C}^n$	Diagonal $n$ by $n$ matrix	NotVector

### 13.4 Semantics

#### 13.4.1 State Variables

None.

#### 13.4.2 Environment Variables

None.

#### 13.4.3 Assumptions

- The input is a square matrix or column vector.

#### 13.4.4 Access Routine Semantics

diag.solver():

- output (if In=A): out:= v such that:  
 $A(j, j) = v(j)$  for  $j=1,2,\dots,n$
- exception (if In=A): exce:=  $A \notin (DiagonalMatrix) \Rightarrow$  NotSquareMatrix

- output (if  $\text{In}=\mathbf{v}$ ):  $\text{out}:=\mathbf{A}$  such that:  
 $A(j,j) = v(j)$  for  $j=1,2,\dots,n$  and zero else.
- exception (if  $\text{In}=\mathbf{v}$ ):  $\text{exce}:= v \notin \mathbb{C}^n \Rightarrow \text{Not vector}$

## 14 MIS of Elliptic Integral

The secret of this module is the the numerical algorithm for calculating the complete elliptic integral for some real constant  $k$ .

### 14.1 Module

ellipK (<https://www.mathworks.com/help/symbolic/elliptick.html>)

### 14.2 Uses

This module uses Numerical Parameters.

### 14.3 Syntax

Name	In	Out	Exceptions
solver	$k : \mathbb{R}$	$\mathbb{R}$	NonNumeric

### 14.4 Semantics

#### 14.4.1 State Variables

None.

#### 14.4.2 Environment Variables

None.

#### 14.4.3 Assumptions

- The argument is a real number.
- The user understands the physical context of the number  $k$ .

#### 14.4.4 Access Routine Semantics

ellipK.solver():

- output :

$$\int_0^{\frac{\pi}{2}} \frac{dx}{\sqrt{1 - k \sin^2(x)}}$$

- exception :  $\text{exce} := \neg(k \in \mathbb{R}) \Rightarrow \text{NonNumeric}$



## 15 MIS of Elliptic Functions

The secret of this module is the the numerical algorithm for calculating the values of the elliptic functions.

### 15.1 Module

ellipj (<https://www.mathworks.com/help/matlab/ref/ellipj.html>)

### 15.2 Uses

This module uses Numerical Parameters.

### 15.3 Syntax

Name	In	Out	Exceptions
solver	$X : \mathbb{R}^n$ $k : \mathbb{R}$	$\mathbb{R}^{3xn}$	BadVal

### 15.4 Semantics

#### 15.4.1 State Variables

None.

#### 15.4.2 Environment Variables

None.

#### 15.4.3 Assumptions

None.

#### 15.4.4 Access Routine Semantics

ellipj.solver():

- output :  $Y : \mathbb{R}^n$  such that  $Y(1, j) = sn(X(j), k)$ ,  $Y(2, j) = cn(X(j), k)$  and  $Y(3, j) = dn(X(j), k)$ . See Module link for more detail regarding jacobi elliptic functions sn,dn and cn.
- exception :  $exce := \neg(X \in \mathbb{R}^n) \Rightarrow \text{BadVal}$

## 16 MIS of Plotting

The secret of this module is the plotting methods/algorithms.

### 16.1 Module

plot (<https://www.mathworks.com/help/matlab/ref/plot.html>)

### 16.2 Uses

This module uses Output.

### 16.3 Syntax

Name	In	Out	Exceptions
plot	$X : \mathbb{R}^n$ $Y : \mathbb{R}^n$	graph(Y)	BadVal, DimensionErr

### 16.4 Semantics

#### 16.4.1 State Variables

None.

#### 16.4.2 Environment Variables

None.

#### 16.4.3 Assumptions

None.

#### 16.4.4 Access Routine Semantics

plot.plot():

- Transition: Plot accepts two vectors as input. A figure is created with the following properties. The domain ranges from the minimum of X to the maximum of X. The range ranges from the minimum of Y to the maximum of Y. The pairs  $(X(j), Y(j))$  for  $j = 1, 2, \dots, n$  are plotted on a figure with respect to the aforementioned axes.
- exception : exce1:=  $\neg(X, Y \in \mathbb{C}^n) \Rightarrow \text{BadVal}$   
exce2:=  $\neg(\dim(Y) = \dim(X)) \Rightarrow \text{DimensionErr}$

## 17 MIS of Linspace

The secret of this module is the software algorithm for creating a vector with equally spaced entries.

### 17.1 Module

Linspace (<https://www.mathworks.com/help/matlab/ref/linspace.html>)

### 17.2 Uses

This module uses Numerical Parameters.

### 17.3 Syntax

Name	In	Out	Exceptions
create	$a : \mathbb{R}$ $b : \mathbb{R}$ $c : \mathbb{N}$	$\mathbb{R}^c$	BadVal,notInt

### 17.4 Semantics

#### 17.4.1 State Variables

None.

#### 17.4.2 Environment Variables

None.

#### 17.4.3 Assumptions

None.

#### 17.4.4 Access Routine Semantics

linspace.create():

- output :  $X \in \mathbb{R}^c$  such that  $X(1)=a$ ,  $X(n)=b$  and  $|x(k) - x(k-1)| = \frac{b-a}{n-1}$  for  $k \in 2, 3, 4, \dots, n$ .
- exception :  $\text{exce} := \neg(c \in \mathbb{N}) \Rightarrow \text{notInt}$
- exception :  $\text{exce} := \neg(a : \mathbb{R}) \Rightarrow \text{BadVal}$
- exception :  $\text{exce} := \neg(b : \mathbb{R}) \Rightarrow \text{BadVal}$

## 18 MIS of Control

The secret of this module is the algorithm that coordinates the overall program and interaction between modules.

### 18.1 Module

Main

### 18.2 Uses

This module uses Input Parameters, Numerical Parameters, Spectrum Matrix, Eigenvalue solver, Spectrum Error , Output and plotting.

### 18.3 Syntax

Name	In	Out	Exceptions
main	-	-	-

### 18.4 Semantics

#### 18.4.1 State Variables

None.

#### 18.4.2 Environment Variables

None.

#### 18.4.3 Assumptions

None.

#### 18.4.4 Access Routine Semantics

main():

- transition: This function controls the running of the scientific software. First, input is taken from the user. This input is used to create useful numerical parameters that will drive the rest of the calculations. The input is brought to the numerical parameters module where useful constants, matrices and elliptic function values are calculated. The state variables from Numerical parameters are used as arguments in Spectrum Matrix. The spectrum (eigenvalues) can be calculated once the spectrum matrix is created. These eigenvalues are plotted and their deviation from theoretical values are computed (err modules).

## References

- Carlo Ghezzi, Mehdi Jazayeri, and Dino Mandrioli. *Fundamentals of Software Engineering*. Prentice Hall, Upper Saddle River, NJ, USA, 2nd edition, 2003.
- Daniel M. Hoffman and Paul A. Strooper. *Software Design, Automated Testing, and Maintenance: A Practical Approach*. International Thomson Computer Press, New York, NY, USA, 1995. URL <http://citeseer.ist.psu.edu/428727.html>.

## 19 Appendix

[Extra information if required —SS]