

# Scientific works in mathematics

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# Outline

- ▶ Types of mathematical works
- ▶ Publication standards in pure and applied mathematics
- ▶ Data handling
- ▶ Ethical issues
- ▶ Citation guidelines
- ▶ References

# Warning!

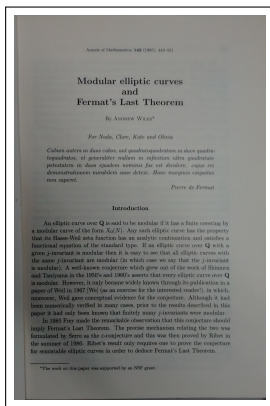
- ▶ This presentation is not exhaustive.
- ▶ It is not meant to be definitive, and only presents some guidelines.
- ▶ Always discuss with a mentor if in doubt.

# Types of mathematical works

Mathematics is made public as:

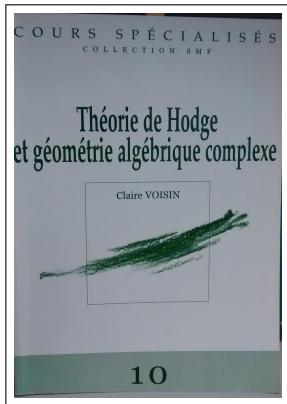
- ▶ Research papers (in journals or conference proceedings);
- ▶ Research monographs or textbooks;
- ▶ PhD theses;
- ▶ Survey-type papers, including (most) master or bachelor theses;
- ▶ Software.

A *research paper* is a self-contained article presenting one or more **new** results in mathematics; these results must be proved completely according to the standards of mathematical rigor.

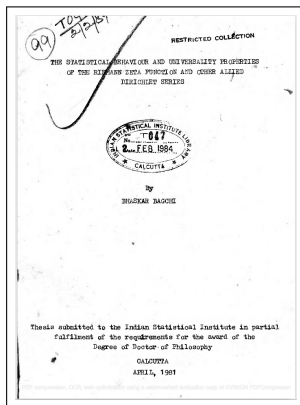


In statistics, a paper can also deal with new software or applications of statistics.

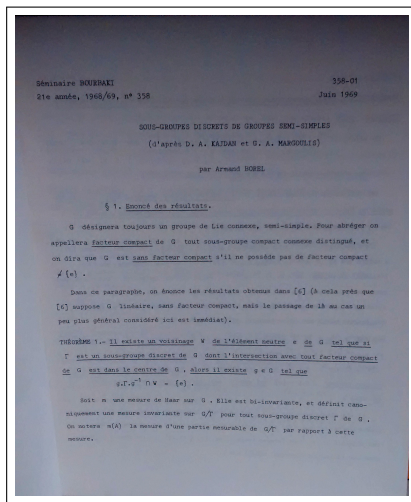
A *research monograph* is a book on a mathematical topic; it may contain new original research, but it can also be a presentation of known results and methods.



A *PhD thesis* in mathematics contains one or more **new** results with complete proofs, often presented with more details and background than in a research article, and sometimes combined with surveys of known material.



A *survey* is an article that presents mostly known results, either with proofs or in an informal way.





- ▶ Software may be a computer program used to prove a result contained in a research paper (“computer-assisted proofs”);
- ▶ It may be a computer program implementing a new algorithm or giving a new implementation of a known algorithm.

# Publication process

- Research papers are often first made available as *preprints* on web sites such as <http://arxiv.org>; the preprint should be complete and fully checked by the author(s).

The screenshot shows the arXiv preprint page for the paper "The entropy formula for the Ricci flow and its geometric applications" by Grisha Perelman. The page is from Cornell University Library and includes a search bar, navigation links, and a sidebar with download options and context information.

**Mathematics > Differential Geometry**

## The entropy formula for the Ricci flow and its geometric applications

Grisha Perelman  
(Submitted on 11 Nov 2002)

We present a monotonic expression for the Ricci flow, valid in all dimensions and without curvature assumptions. It is interpreted as an entropy for a certain canonical ensemble. Several geometric applications are given. In particular, (1) Ricci flow, considered on the space of Riemannian metrics modulo diffeomorphism and scaling, has no nontrivial periodic orbits (that is, other than fixed points); (2) In a region, where singularity is forming in finite time, the injectivity radius is controlled by the curvature; (3) Ricci flow can not quickly turn an almost euclidean region into a very curved one, no matter what happens far away. We also verify several assertions related to Richard Hamilton's program for the proof of Thurston geometrization conjecture for closed three-manifolds, and give a sketch of an edictic proof of this conjecture, making use of earlier results on collapsing with local lower curvature bound.

Comments: 39 pages  
Subject: Differential Geometry (math.DG)  
MSC-class: 53C  
Cite as: [arXiv:math/0211159](https://arxiv.org/abs/math/0211159) [math.DG]  
(or [arXiv:math/0211159v1](https://arxiv.org/abs/math/0211159v1) [math.DG] for this version)

**Submission history**  
From: Grisha Perelman [[view email](#)]  
[v1] Mon, 11 Nov 2002 16:11:49 GMT (39kb)

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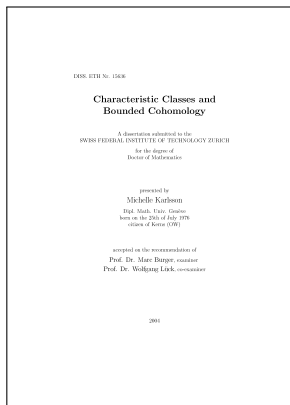
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[38 blog links](#) (what is this?)

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- ▶ Research papers are then usually submitted for publication, either to a specialist mathematical journal, or as a chapter of a proceedings volume for a conference.
- ▶ In principle, the results of a research paper are considered to have been checked and verified for correctness only after it is accepted for publication, after full refereeing by one or more experts.

**Important.** At ETH Zürich, one copy of every PhD thesis is kept by the main library, and one by the mathematics library.



# Publication standards: “pure” mathematics

- ▶ The most prestigious papers appear in generalist mathematical journals, or in journals specializing in some specific area of mathematics (e.g., analysis, combinatorics, number theory, etc); proceedings of conferences are, usually, not as important;
- ▶ If there is more than one author, they are listed *in alphabetical order*, with no implied ordering concerning the share of the work done by the various authors.
- ▶ The thesis advisor (for a PhD thesis) or mentor (for a postdoctoral researcher) or head of group or institute does not usually appear as an author, unless he or she has contributed scientifically at the same level as other authors.

## Special features: statistics

- ▶ Prestigious papers on theory appear in mathematical journals focusing on statistics; prestigious papers involving a new method **and** applications appear also in journals such as *Nature Methods*;
- ▶ If there is more than one author, the listing of the names usually has some meaning. In particular, the first author contributed most and the last author is most senior and usually gave most strategic input (he or she is not listed if he or she did not contribute to the paper). The authors mentioned between first and last contributed less.
- ▶ Simulation studies must be archived in a way that a third person can reproduce them.

## Special features: operations research

- ▶ Prestigious papers may also appear in a highly competitive proceedings volume;
- ▶ Scientific computations must be reproducible, best practice being to make the computer code publicly available.

# Numerical experiments in applied mathematics

- ▶ Numerical experiments **must** be fully reproducible: any reader of the paper should be able to reproduce all the results from the paper the code and data available online.
- ▶ The computer code is part of the scientific work, hence it should appear in an Appendix (if short enough) or in a repository that is publicly available and has a guarantee of long-term availability. The code must come with full documentation and with all instructions on how to install and run it.



# Ethical issues

- ▶ One should not claim or announce a result without having a complete proof and having checked it (as far as possible, since mistakes are always possible);
- ▶ Priority for proving a result is not directly linked to publication, and may be established by making available a (fully detailed) preprint, or by having a thesis manuscript;
- ▶ All authors of a research paper must have made a *significant scientific contribution* to the new results that it contains;
- ▶ All results that are used or other information or insights that have been involved in the research represented by the paper must be properly acknowledged.

# Citation guidelines

- ▶ The following guidelines apply (at least) to pure mathematics and statistics. For more details and examples, see the MathBIB Moodle module.
- ▶ Citations must have a sound scientific purpose, and in particular an author should not cite his or her own work, or that of friends or colleagues, without good reason.
- ▶ Any citation of a specific, precise, result, must be accompanied with a precise location in the paper or book that is referenced.

## Standard result

The citation need not belong to the original paper where the result is proved, but to a later account. It is then usually clear to the reader that the authors of the work referenced are not the discoverers of the theorem.

**Example.** To cite the Banach-Steinhaus Theorem, supposing that one wishes to use Bourbaki's "Elements of Mathematics" as the reference, one should write:

By the Banach-Steinhaus Theorem ([1, EVT, III, §4, Cor. 2]), we have...

and not

By the Banach-Steinhaus Theorem [1], we have...

# Background information

If a book or paper is cited only to provide background information, it may be cited without more precision.

## **Example.**

Signs of Fourier coefficients of cusp forms have also been studied by Matomäki [Mat] and Ghosh-Sarnak [G-S].

For a general introduction to Hodge theory, see for instance the book of Voisin [V].

# Spelling out names

When citing for the first time, it is often best to spell out the names of the author(s) explicitly.

## **Example.**

It was proved by Fouvry [13] and Bombieri, Friedlander and Iwaniec [5] that certain arithmetic functions have exponent of distribution strictly larger than  $1/2$ ...

instead of

It was proved in [5,13] that certain arithmetic functions have exponent of distribution strictly larger than  $1/2$ ...

# Attribution

A theorem which is stated without specific attribution is *usually supposed to have been proved by the author of the text*. If this is not the case, precise attribution is needed.

## Example.

Write

We will prove in this text:

**Theorem** (Dirichlet). *Let  $a$  be an integer and let  $q \geq 1$  be an integer such that  $a$  and  $q$  are coprime. Then there are infinitely many primes  $p$  congruent to  $a$  modulo  $q$ .*

and not

**Theorem.** *Let  $a$  be an integer and let  $q \geq 1$  be an integer such that  $a$  and  $q$  are coprime. Then there are infinitely many primes  $p$  congruent to  $a$  modulo  $q$ .*

# Adapting previous arguments

It is acceptable in a *research paper* to follow closely the proof of an already published work to prove *an analogue result*, but this fact must be clearly indicated with proper reference.

## **Example.**

This lemma is a slight variant of a result of Helfgott [H2004, Lemma 5.1], and our proof follows his argument closely.

# Acknowledging input from other works

A mathematical text should also cite and acknowledge works or ideas which have had an important influence in the search for the proof.

## **Example.**

The proof of this theorem was inspired by the analogy pointed out by Deligne [8] between Hodge theory and Galois representations.

or

The author learned about the technique in this proof from discussions with Venkatesh concerning sparse equidistribution problems.



# References

- ▶ “Scientific works in mathematics”, and these slides, available from MathBIB

[www.math.ethz.ch/library/services/schulungen](http://www.math.ethz.ch/library/services/schulungen)

- ▶ MathBIB Schulung (26.11.2014), “Recherchieren in der Mathematik”, registration on

[www.math.ethz.ch/library/services/schulungen](http://www.math.ethz.ch/library/services/schulungen)

- ▶ MathBIB Moodle

[moodle-app2.let.ethz.ch/course/view.php?id=519](http://moodle-app2.let.ethz.ch/course/view.php?id=519)

- ▶ “Richtlinien für Integrität in der Forschung und gute wissenschaftliche Praxis an der ETH Zürich”,  
Rechtssammlung, RS 414, available in German and English translation from

[www.share.ethz.ch/sites/rechtssammlung/  
Rechtssammlung](http://www.share.ethz.ch/sites/rechtssammlung/Rechtssammlung)