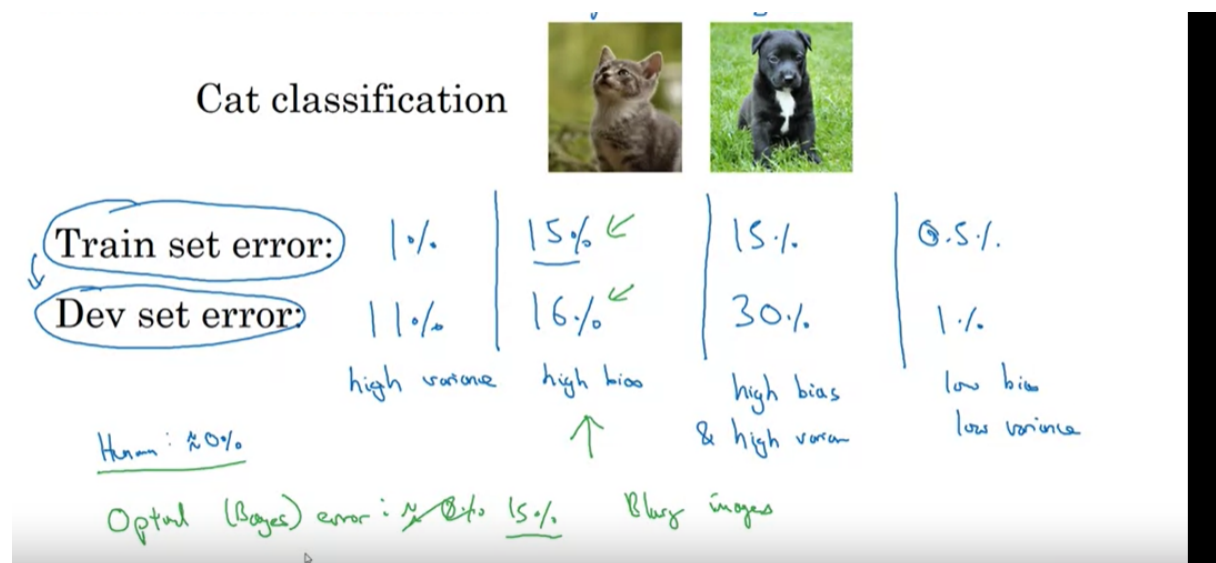
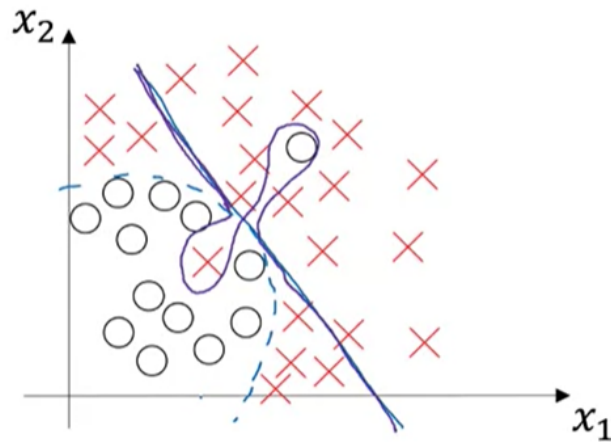


dL.ai_Improvements in Nueral Network

a) Bias-Variance



- High bias means we assume a lot of things about the classifier, we dont consider eenough dimensions.
- High variance means the data is too sensitive to each individual instance in the training data
- They are not antogonistic to each other
- A classifier having high bias and variance will look like the purple line



b) Regularization

i) L1 and L2

- L1 and L2 tries to prevent overfitting by penalizing the model for having high weights..
- We do this by adding weights into the loss function.
- example for logistic loss

$$J(w, b) = \frac{1}{m} \sum_{i=1}^m \ell(y^{(i)}, \hat{y}^{(i)}) + \frac{\lambda}{2m} \|w\|_2^2$$

$$\text{L}_2 \text{ regularization} \quad \|w\|_2^2 = \sum_{j=1}^{n_x} w_j^2 = w^T w \leftarrow$$

$$\text{L}_1 \text{ regularization} \quad \frac{\lambda}{2m} \sum_{i=1}^{n_x} |w| = \frac{\lambda}{2m} \|w\|_1$$

- where lambda is the regularization parameter.
- In nueral network $\|w\|$ by the frobenius norm gives

$$\|w^{(l)}\|_F^2 = \sum_{i=1}^{n^{(l+1)}} \sum_{j=1}^{n^{(l)}} (w_{ij}^{(l)})^2$$

- during backpropagation when we find dw an additional term $\frac{\lambda}{m}w$ is also considered this leads to the magnitude of weight decreasing. Hence L2 is also called weight decay.

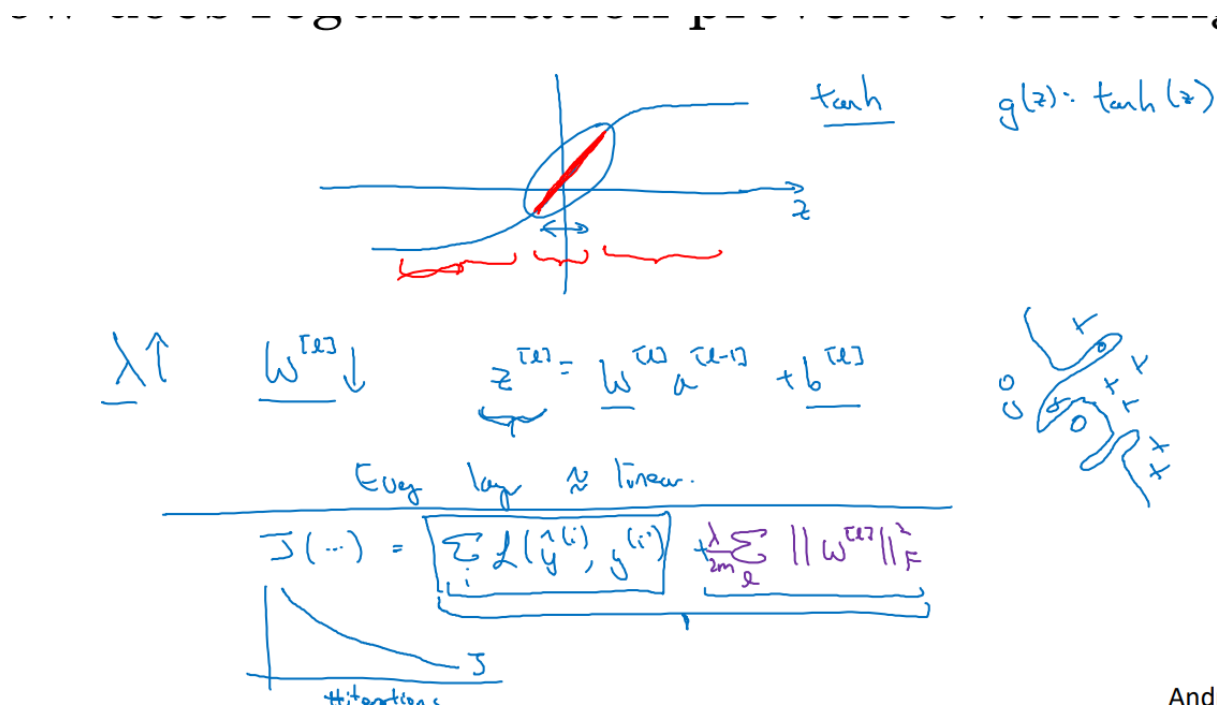
$$\begin{aligned}
 dW^{[2]} &= (\text{from backprop}) + \frac{\lambda}{m} W^{[2]} \\
 W^{[2]} &:= W^{[2]} - \alpha dW^{[2]} \\
 \text{decay: } W^{[2]} &:= W^{[2]} - \alpha \left[(\text{from backprop}) + \frac{\lambda}{m} W^{[2]} \right] \\
 &= W^{[2]} - \left(\frac{\alpha \lambda}{m} \right) W^{[2]} - \alpha (\text{from backprop}) \\
 &= \left(1 - \frac{\alpha \lambda}{m} \right) W^{[2]} - \alpha (\text{from backprop})
 \end{aligned}$$

Ar

- L1 regularization leads to sparsity in the model. It completely makes some of the weights zero which leads to some nodes being always inactivated leading to a smaller model. I hope this because when we

$$\begin{aligned}
 J &= CE + \frac{\lambda}{m} |w| \\
 dw &= (bpterm) + \frac{\lambda}{m} w \\
 w^{[l]} - dw^{[l]} &= w^{[l]} - a(bpterm) - a \frac{\lambda}{m} w
 \end{aligned}$$

- let $w^{[l]}$ be [1,2,3,4,5] then each weight in w will be decreased by the same constant value till they reach zero or no of epochs complete.
- However in L2 since $\frac{\lambda}{m}w$ is proportional to weight the extreme values are penalised more and the lower values are penalised lesser. It tends to make all the weights smaller but not exactly zero.
- Even though variance and bias are not perfectly complementary we can say that if a model is closer to a linear regressor it would decrease the variance
- so if value of w is less the value of z would be less, if the value of z is less then sigmoid function will more or less converge to a linear $y-x$ graph. Hence the whole model comes closer to a linear regressor.



Andi

ii) Inverted Dropout

- During training in a given layer all the nodes are not taken a fixed ratio of nodes are always dropped out.

Illustrate with layer $l=3$. keep-prob = 0.8 0.2

$\rightarrow d3 = \text{np.random.rand}(a3.\text{shape}[0], a3.\text{shape}[1]) < \text{keep-prob}$

$a3 = \text{np.multiply}(a3, d3)$ # $a3 \neq d3$.

$\rightarrow a3 /= \text{keep-prob}$

50 units. \rightarrow 10 units shut off

$z^{[4]} = w^{[4]} \cdot a^{[3]} + b^{[4]}$

\uparrow reduced by 20% Test

\uparrow $= 0.8$

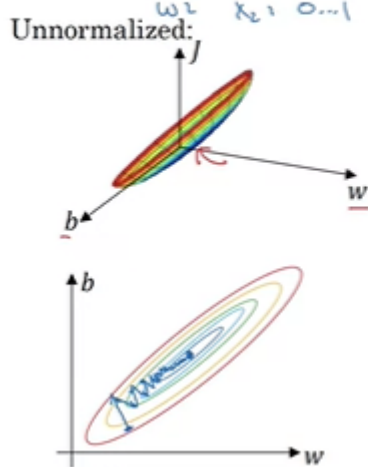
- Understand how the value of z doesn't change even though several $a3$ have become zero
- Dropout reduces the dependence of a model on a single node
- Dropout makes Loss function more vague

- Drop out ensures that the network can't depend entirely on any one feature. This ensures that the weights are spread out more. This has a similar effect to L2 regularization.
- During each iteration of training the input data only passes through a smaller nn.

c) Normalizing

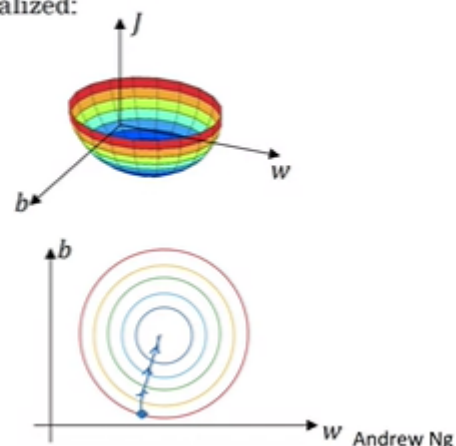
Why normalize inputs?

Unnormalized:
 $w_1, x_1: 1 \dots 1000$
 $w_2, x_2: 0 \dots 1$



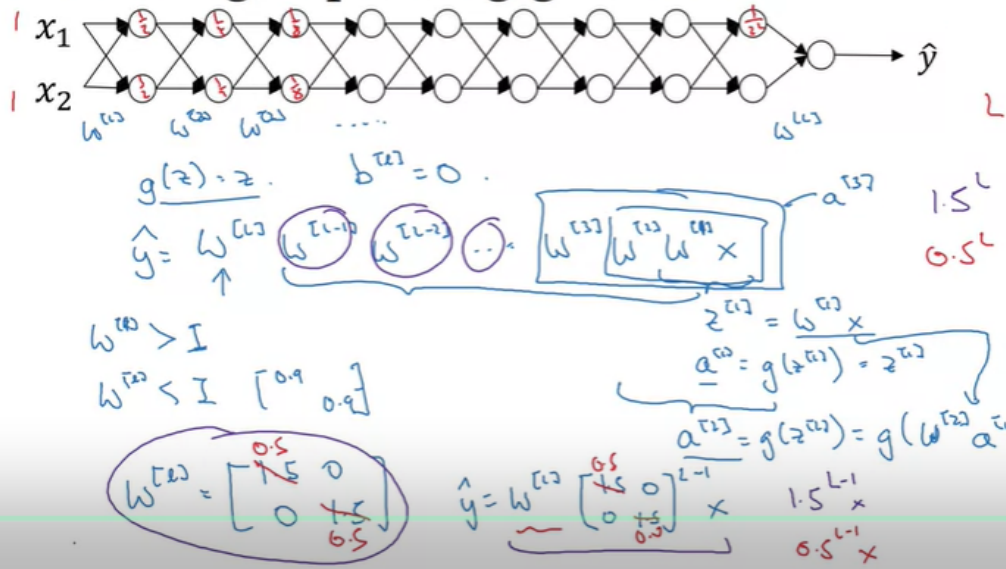
$$J(w, b) = \frac{1}{m} \sum_{i=1}^m \mathcal{L}(\hat{y}^{(i)}, y^{(i)})$$

Normalized:



d) Vanishing/Exploding Gradient

Vanishing/exploding gradients



Andrew Ng