

DSA 8020 R Session 7: Logistic Regression and Poisson Regression

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Logistic Regression: Horseshoe Crab Malting

Data Source: Brockmann, H. J. (1996). Satellite male groups in horseshoe crabs, *Limulus polyphemus*. *Ethology*, 102(1), 1-21.

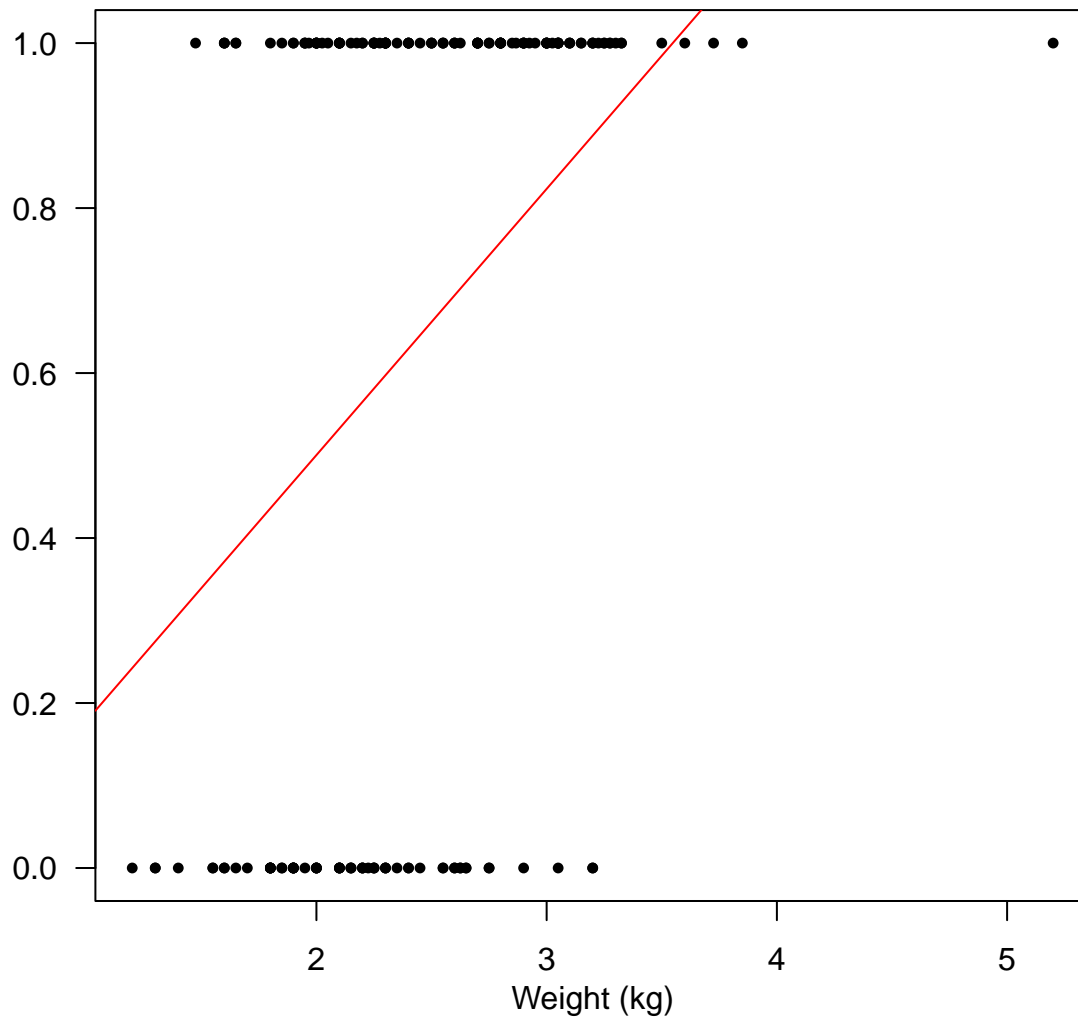
Load the data

```
crab <- read.table("http://users.stat.ufl.edu/~aa/cda/data/Crabs.dat", header = T)
```

Fit a Linear Regression

Let's fit a simple linear regression using `weight` as the predictor

```
lmFit <- lm(y ~ weight, data = crab)
par(mar = c(3.5, 3.5, 0.8, 0.6))
with(crab, plot(weight, y, pch = 16,
                cex = 0.75, las = 1, xlab = "", ylab = ""))
mtext("Weight (kg)", side = 1, line = 2)
abline(lmFit, col = "red")
```



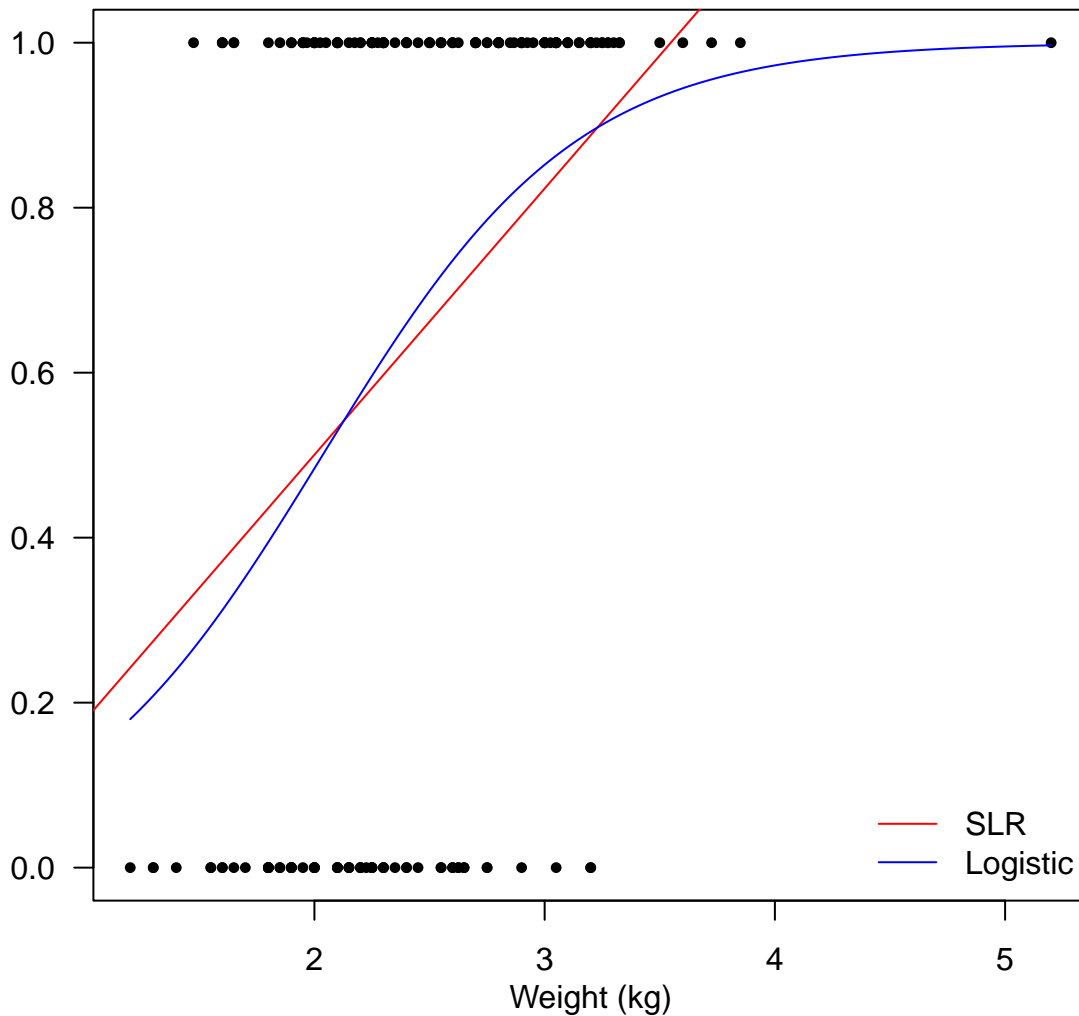
Fit a Logistic Regression

```
logitFit <- glm(y ~ weight, data = crab, family = "binomial")
summary(logitFit)
```

```
##
## Call:
## glm(formula = y ~ weight, family = "binomial", data = crab)
##
## Deviance Residuals:
```

```
##      Min      1Q   Median      3Q      Max
## -2.1108 -1.0749  0.5426   0.9122   1.6285
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)  -3.6947     0.8802  -4.198 2.70e-05 ***
## weight       1.8151     0.3767   4.819 1.45e-06 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 225.76  on 172  degrees of freedom
## Residual deviance: 195.74  on 171  degrees of freedom
## AIC: 199.74
##
## Number of Fisher Scoring iterations: 4
```

```
# Plot the fits
rg <- range(crab$weight)
xg <- seq(rg[1], rg[2], 0.01)
pred <- predict(logitFit, newdata = data.frame(weight = xg), type = "response")
par(mar = c(3.5, 3.5, 0.8, 0.6))
plot(crab$weight, crab$y, pch = 16, cex = 0.75, las = 1, xlab = "", ylab = "")
mtext("Weight (kg)", side = 1, line = 2)
abline(lmFit, col = "red")
lines(xg, pred, col = "blue")
legend("bottomright", legend = c("SLR", "Logistic"),
      col = c("red", "blue"), lty = 1, bty = "n")
```



Confidence Intervals

```
# Normal approximation
est <- summary(logitFit)$coefficients
(CI_norm <- est[2, 1] + c(-1, 1) * qnorm(0.975) * est[2, 2])
```

```
## [1] 1.076834 2.553455
```

```
# Profile likelihood CI
library(MASS)
(CI_prof <- confint(logitFit)[2,])
```

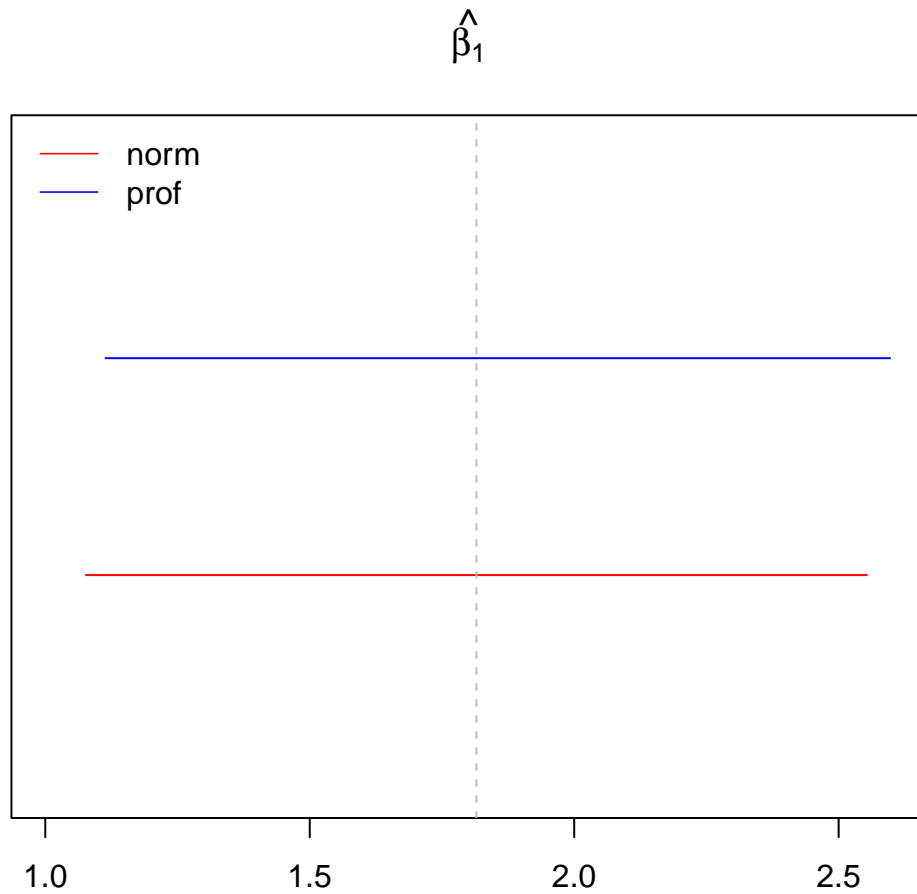
```
## Waiting for profiling to be done...
```

```
##    2.5 %    97.5 %
## 1.113790 2.597305
```

```

plot(1, type = "n", xlab = "", ylab = "",
     xlim = c(1, 2.6), ylim = c(-0.05, 0.1),
     yaxt = "n", main = expression(hat(beta)[1]))
segments(CI_norm[1], 0, CI_norm[2], col = "red")
segments(CI_prof[1], 0.05, CI_prof[2], col = "blue")
abline(v = est[2, 1], lty = 2, col = "gray")
legend("topleft", legend = c("norm", "prof"),
      col = c("red", "blue"), lty = 1,
      lwd = 0.8, bty = "n")

```



Prediction

```

rg <- range(crab$weight)
xg <- seq(rg[1], rg[2], 0.01)

pred <- predict(logitFit, newdata = data.frame(weight = xg), se.fit = TRUE)

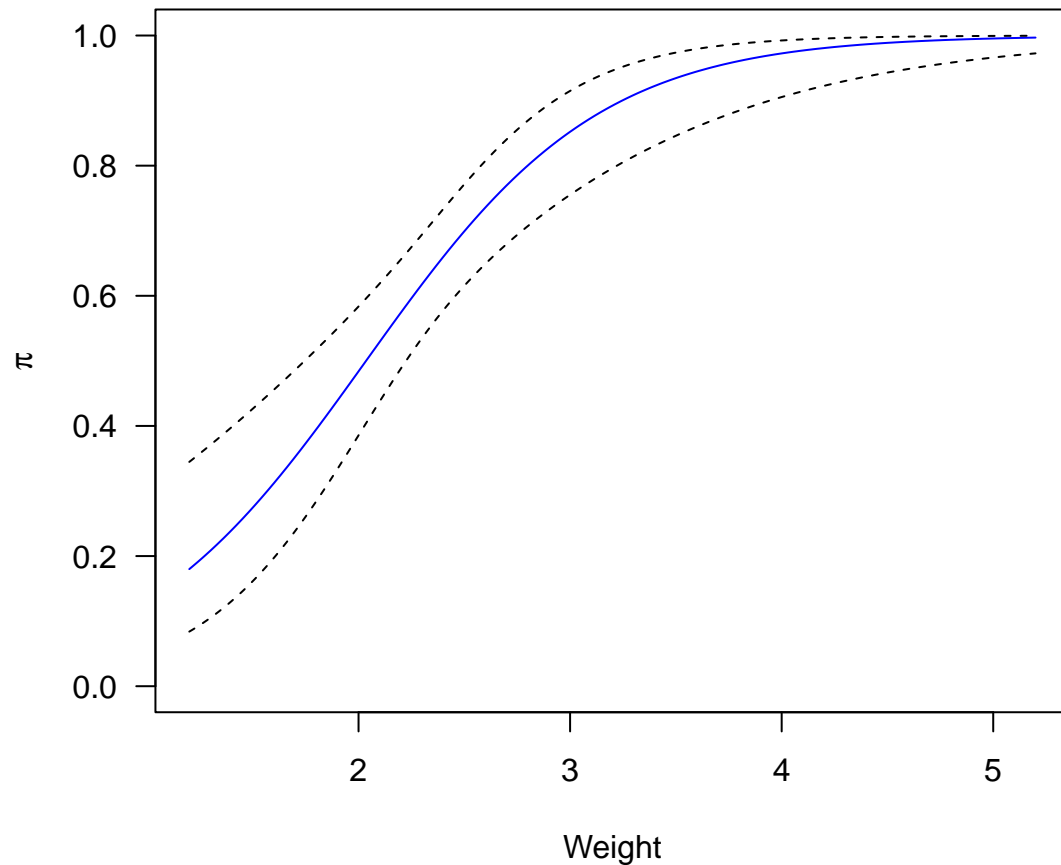
```

```

fit <- pred$fit; se <- pred$se.fit

plot(xg, exp(fit) / (1 + exp(fit)),
     type = "l", col = "blue", ylim = c(0, 1),
     las = 1, xlab = "Weight", ylab = expression(pi))
lines(xg, exp(fit + 1.96 * se) / (1 + exp(fit + 1.96 * se)), lty = 2)
lines(xg, exp(fit - 1.96 * se) / (1 + exp(fit - 1.96 * se)), lty = 2)

```



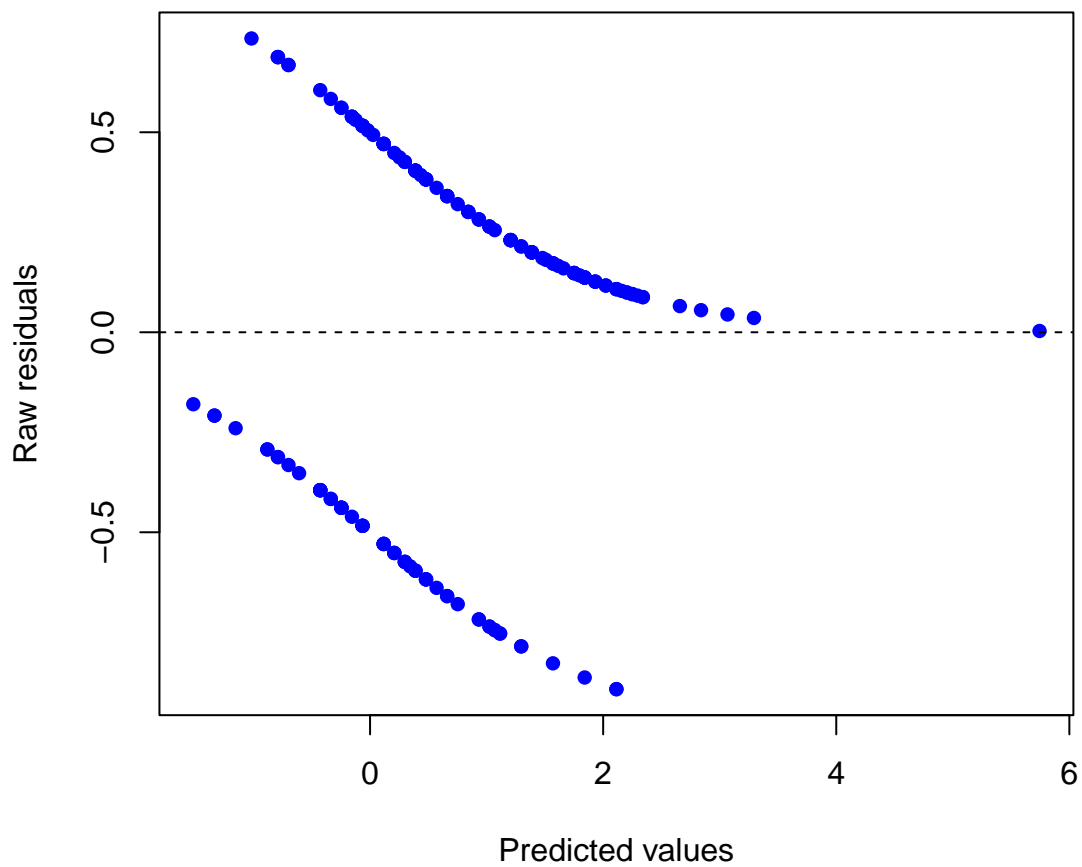
Raw Residual plot

```

res <- resid(logitFit, type = "response")
pred <- predict(logitFit)

plot(pred, res, col = "blue", pch = 16,
     xlab = "Predicted values",
     ylab = "Raw residuals")
abline(h = 0, lty = 2)

```

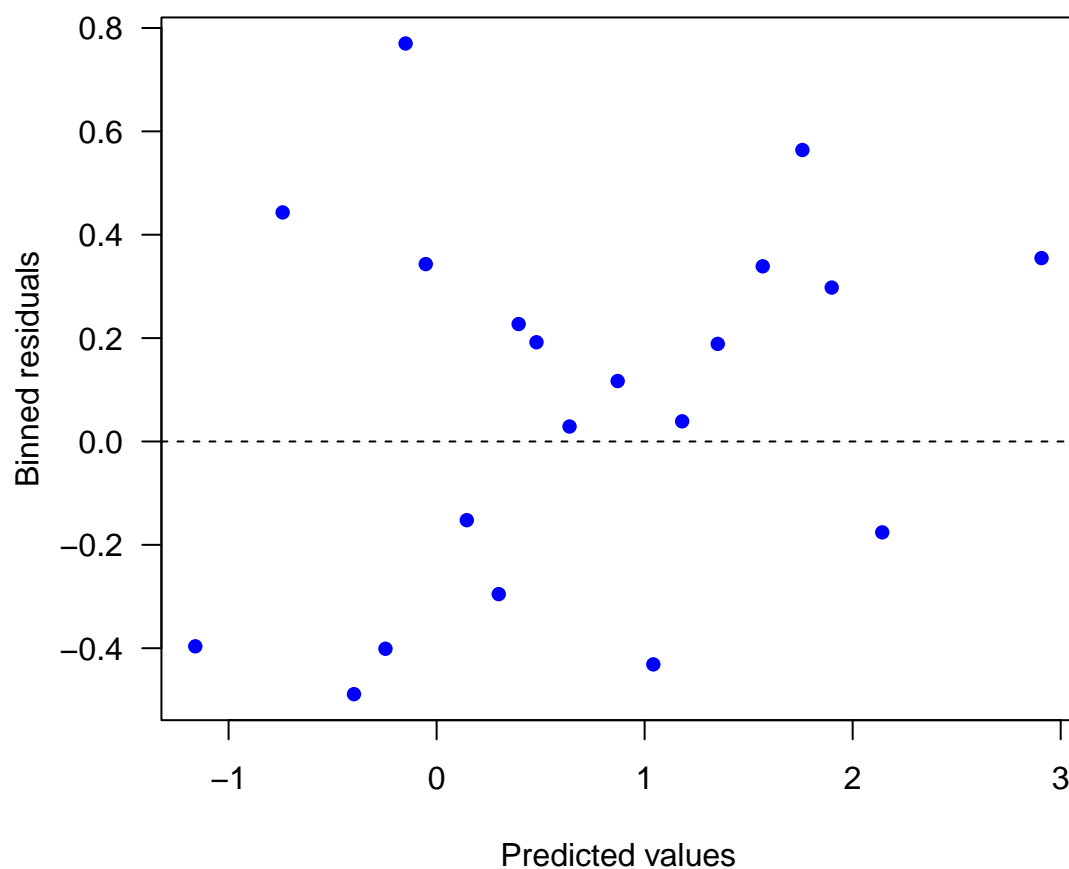


Binned Residuals

```
wt_bin <- findInterval(crab$weight, unique(quantile(crab$weight, seq(0, 1, length.out = 20 + 1))), right = FALSE)
library(dplyr)
crab.res <- mutate(crab, residuals = residuals(logitFit), Linpred = predict(logitFit), bin = wt_bin)

res_bin <- tapply(crab.res$residuals, crab.res$bin, mean)
Lpred_bin <- tapply(crab.res$Linpred, crab.res$bin, mean)

plot(res_bin ~ Lpred_bin, xlab = "Predicted values",
     ylab = "Binned residuals", col = "blue", pch = 16, las = 1)
abline(h = 0, lty = 2)
```



Model selection

```
logitFit2 <- glm(y ~ weight + width, data = crab, family = "binomial")
summary(logitFit2)
```

```
##
## Call:
## glm(formula = y ~ weight + width, family = "binomial", data = crab)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -2.1127  -1.0344   0.5304   0.9006   1.7207
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)  -9.3547     3.5280  -2.652  0.00801 **
## weight         0.8338     0.6716   1.241  0.21445
## width         0.3068     0.1819   1.686  0.09177 .
```



```
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 225.76  on 172  degrees of freedom
## Residual deviance: 192.89  on 170  degrees of freedom
## AIC: 198.89
##
## Number of Fisher Scoring iterations: 4
```

```
step(logitFit2)
```

```
## Start:  AIC=198.89
## y ~ weight + width
##
##           Df Deviance    AIC
## - weight  1    194.45 198.45
## <none>           192.89 198.89
## - width   1    195.74 199.74
##
## Step:  AIC=198.45
## y ~ width
##
##           Df Deviance    AIC
## <none>           194.45 198.45
## - width  1    225.76 227.76
##
##
## Call:  glm(formula = y ~ width, family = "binomial", data = crab)
##
## Coefficients:
## (Intercept)          width
##    -12.3508         0.4972
##
## Degrees of Freedom: 172 Total (i.e. Null);  171 Residual
## Null Deviance:      225.8
## Residual Deviance: 194.5    AIC: 198.5
```

Poisson Regression

Flying-Bomb Hits on London During World War II [Clarke, 1946; Feller, 1950]

```
count <- c(229, 211, 93, 35, 7, 1)
grids <- 576
hits <- 537
lambda <- hits / grids
count_expected <- c(grids * dpois(0:4, lambda = lambda), grids * ppois(4, lambda = lambda, lower.tail =
round(count_expected, 1)
```

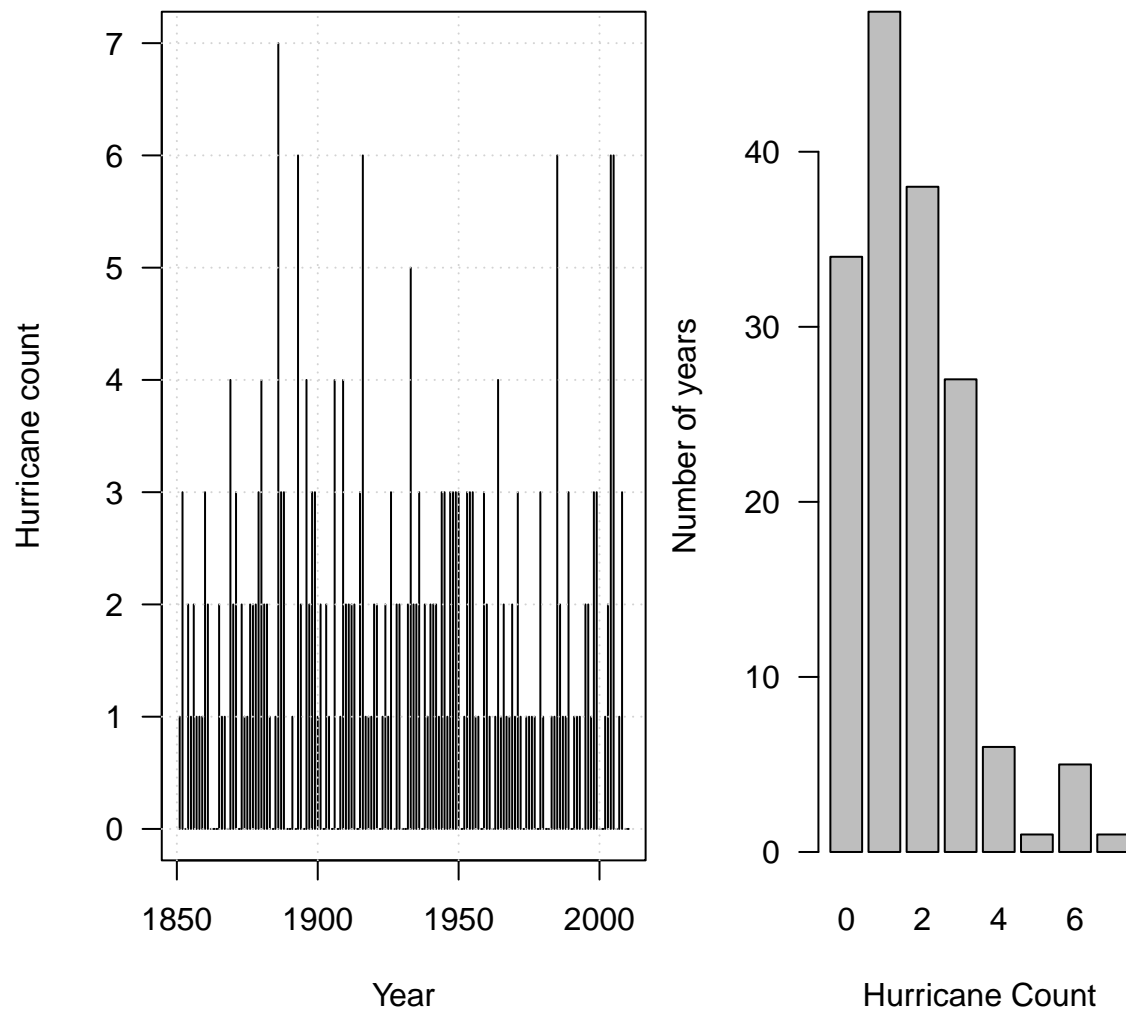
```
## [1] 226.7 211.4 98.5 30.6 7.1 1.6
```

US Landfalling Hurriances

```
# load the hurriance count
con = "http://myweb.fsu.edu/jelsner/Book/Chap07/US.txt"
hurricanes = read.table(con, header = T)
head(hurricanes)
```

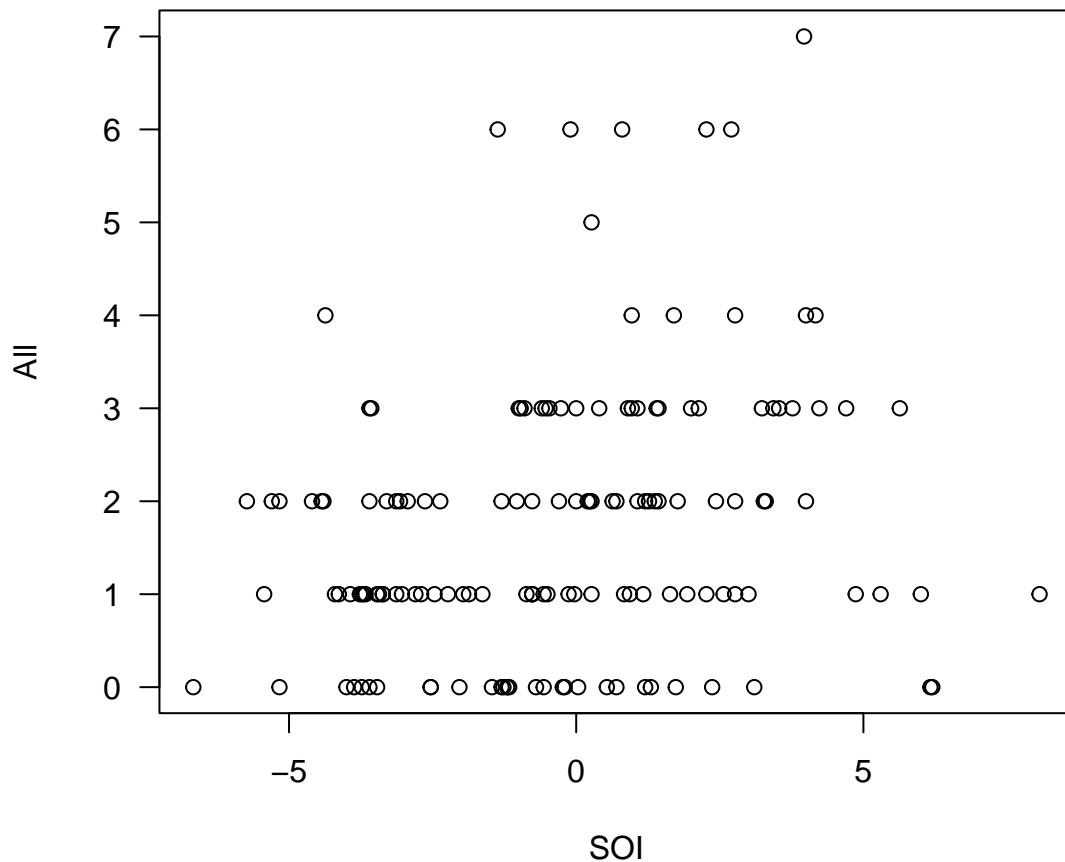
```
##   Year All MUS G FL E
## 1 1851   1   1 0  1 0
## 2 1852   3   1 1  2 0
## 3 1853   0   0 0  0 0
## 4 1854   2   1 1  0 1
## 5 1855   1   1 1  0 0
## 6 1856   2   1 1  1 0
```

```
par(las = 1, mar = c(4.6, 3.9, 0.8, 0.6))
layout(matrix(c(1, 2), 1, 2, byrow = TRUE), widths = c(0.57, 0.43))
plot(hurricanes$Year, hurricanes$All, type = "h", xlab = "Year", ylab = "Hurricane count")
grid()
barplot(table(hurricanes$All), xlab = "Hurricane Count", ylab = "Number of years", main = "")
```



Load the environmental variables

```
load("annual.RData")
data <- data.frame(All = hurricanes$All, SOI = annual$soi,
                  NAO = annual$nao, SST = annual$sst,
                  SSN = annual$ssn)
data <- data[-(1:15),]
with(data, plot(All ~ SOI, las = 1))
```



```
H <- hurricanes

par(mfrow = c(2, 2), mar = c(4.5, 4, 1, 0.6))
plot(range(annual$sst, na.rm = TRUE), c(0, 7), type = "n", ylab = "Hurricane count", xlab = "SST",
     las = 1)
for(i in 0:7){
  points(fivenum(annual$sst[H$All == i])[3], i, pch = 19)
  lines(c(fivenum(annual$sst[H$All == i])[1], fivenum(annual$sst[H$All == i])[2]), c(i, i))
  lines(c(fivenum(annual$sst[H$All == i])[4], fivenum(annual$sst[H$All == i])[5]), c(i, i))
}
plot(range(annual$soi, na.rm = TRUE), c(0, 7), type = "n", ylab = "Hurricane count", xlab = "SOI",
     las = 1)

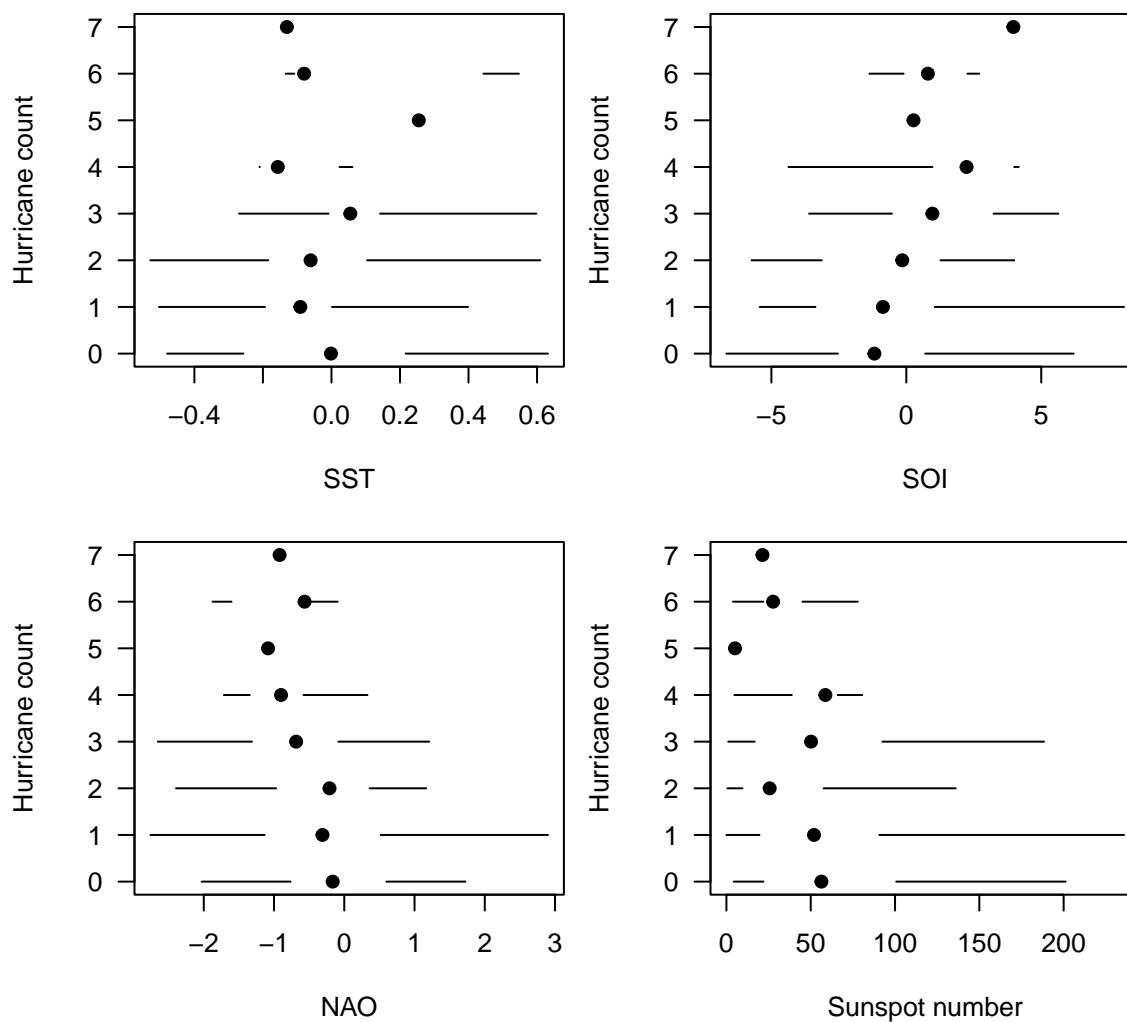
for(i in 0:7){
  points(fivenum(annual$soi[H$All == i])[3], i, pch=19)
  lines(c(fivenum(annual$soi[H$All == i])[1], fivenum(annual$soi[H$All == i])[2]), c(i, i))
  lines(c(fivenum(annual$soi[H$All == i])[4], fivenum(annual$soi[H$All == i])[5]), c(i, i))
}
plot(range(annual$nao, na.rm = TRUE), c(0, 7), type = "n", ylab = "Hurricane count", xlab = "NAO",
     las = 1)
```

```

for(i in 0:7){
  points(fivenum(annual$nao[H$All == i])[3], i, pch=19)
  lines(c(fivenum(annual$nao[H$All == i])[1], fivenum(annual$nao[H$All == i])[2]), c(i, i))
  lines(c(fivenum(annual$nao[H$All == i])[4], fivenum(annual$nao[H$All == i])[5]), c(i, i))
}
plot(range(annual$ssn, na.rm = TRUE), c(0, 7), type = "n", ylab = "Hurricane count",
      xlab = "Sunspot number", las = 1)

for(i in 0:7){
  points(fivenum(annual$ssn[H$All == i])[3], i, pch = 19)
  lines(c(fivenum(annual$ssn[H$All == i])[1], fivenum(annual$ssn[H$All == i])[2]), c(i, i))
  lines(c(fivenum(annual$ssn[H$All == i])[4], fivenum(annual$ssn[H$All == i])[5]), c(i, i))
}

```

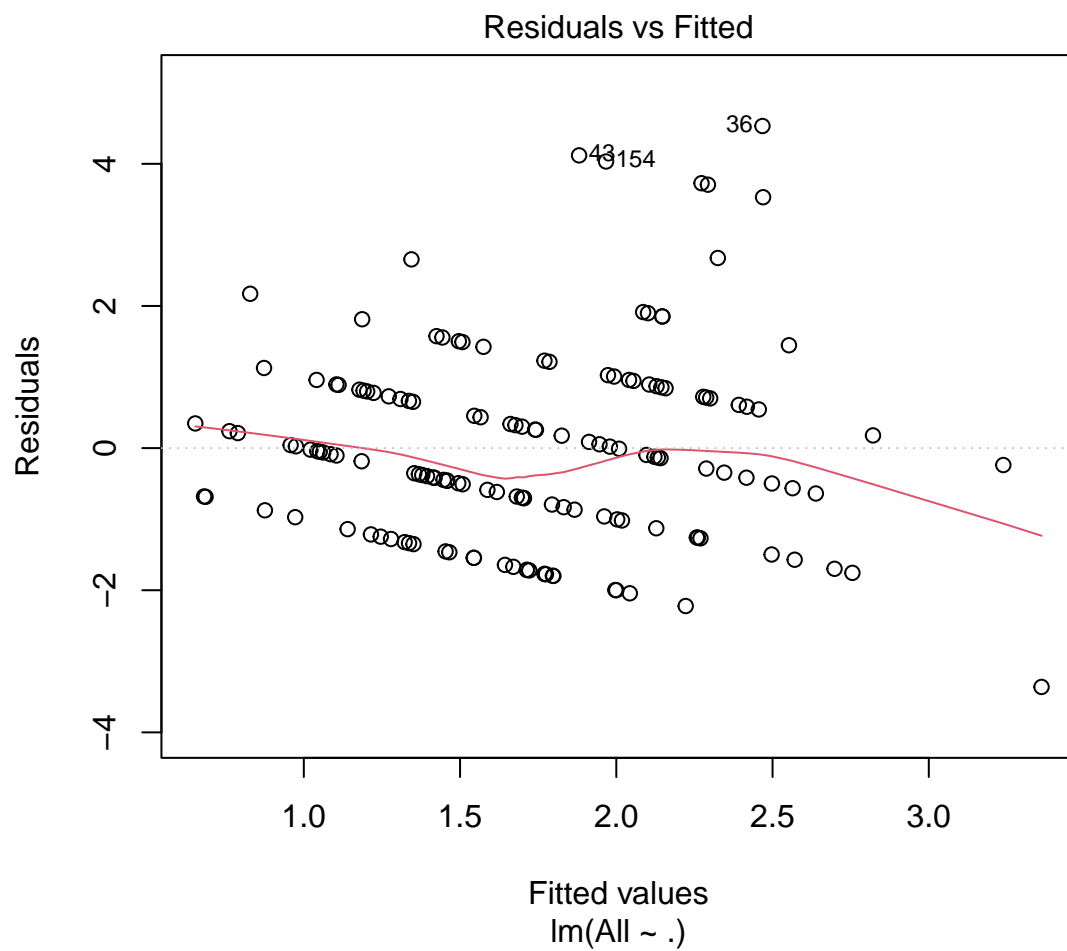


Linear Regression

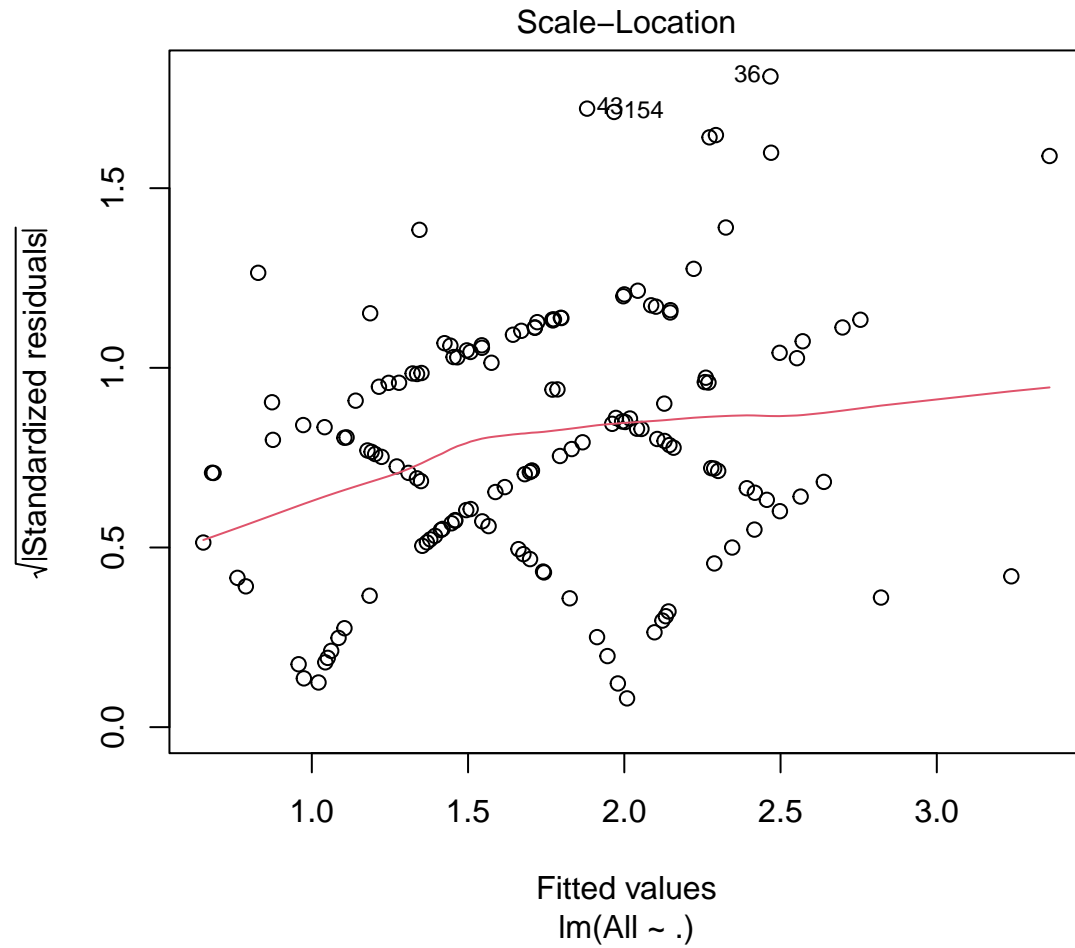
```
lmFull <- lm(All ~ ., data = data)
predict(lmFull, newdata = data.frame(SOI = -3, NAO = 3, SST = 0, SSN = 250))
```

```
##          1
## -0.318065
```

```
plot(lmFull, which = 1)
```



```
plot(lmFull, which = 3)
```



Poisson Regression

```
PoiFull <- glm(All ~ ., data = data, family = "poisson")
summary(PoiFull)
```

```
##
## Call:
## glm(formula = All ~ ., family = "poisson", data = data)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -2.8530  -0.8984  -0.1376   0.6027   2.4720
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)  0.595288   0.103342   5.760 8.39e-09 ***
## SOI          0.061863   0.021319   2.902 0.00371 **
## NAO         -0.166595   0.064427  -2.586 0.00972 **
```

```
## SST          0.228972  0.255289  0.897  0.36977
## SSN          -0.002306  0.001372 -1.681  0.09284 .
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for poisson family taken to be 1)
##
## Null deviance: 197.89  on 144  degrees of freedom
## Residual deviance: 174.81  on 140  degrees of freedom
## AIC: 479.64
##
## Number of Fisher Scoring iterations: 5
```

```
plot(data$SOI, hurricanes$All[-(1:15)], cex = 0.75, col = "gray",
     xlab = "", ylab = "", las = 1)
mtext("Hurricane Count", side = 2, line = 2)
mtext("Year", side = 1, line = 2)
points(data$SOI, predict(lmFull), col = "red",
       cex = 0.5, pch = 16)
points(data$SOI, predict(PoiFull, type = "response"), col = "blue", cex = 0.5, pch = 16)
```

