## Lecture 10

# Inference for One Population Mean

Text: Chapter 5

STAT 8010 Statistical Methods I February 18, 2020



Statistical Inferences

Estimation

Confidence Intervals

Hypothesis Testing

Whitney Huang Clemson University

Statistical Inferences

Point/Interval Estimation

Confidence Intervals

- Statistical Inferences
- Point/Interval Estimation
- 3 Confidence Intervals
- 4 Hypothesis Testing

#### Statistical Inference

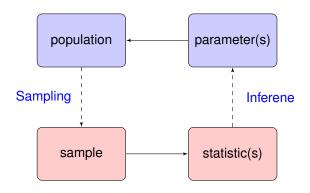


Statistical Infere

Confidence Intervals

For the rest of the semester, we will focus on conducting statistical inferences for the following tasks:

- Estimating one population mean
- Comparing two population means
- Comparing more than two population means
- Estimating population proportions
- Estimating relationship between two quantitative variables



• We use statistics of a sample to infer the population **Example:** sample mean  $(\bar{X})$ ; sample variance  $(s_X^2)$ 



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**Goal:** To estimate the population mean using a (representative) sample:

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• The sample mean,  $\bar{X}_n = \frac{\sum_i^n X_i}{n}$ , is a reasonable point estimate of the population mean  $\mu_X$ 





#### Statistical interences

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Hypothesis Testing

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- Need to quantify the level of uncertainty of the point estimate ⇒ Interval estimation
- Need to figure out the sampling distribution of  $\bar{X}_n$  in order to construct interval estimates  $\Rightarrow$  Central Limit Theorem (CLT)

#### **Central Limit Theorem (CLT)**

#### CLT

The sampling distribution of  $\bar{X}_n$  will become approximately normally distributed as the sample size (n) becomes "large", regardless of the shape of the population distribution!

Let  $X_1, X_2, \cdots, X_n$  be a random sample from a population X with  $\mu = \mathbb{E}[X]$  and  $\sigma^2 = \text{Var}[X]$ . Then  $\bar{X}_n = \frac{\sum_{i=1}^n X_i}{n} \stackrel{d}{\to} \mathbb{N}(\mu, \frac{\sigma^2}{n})$  as  $n \to \infty$ .

Statistical Inferences

stimation

#### **CLT In Action**

- Generate 100 (n) random numbers from an Exponential distribution (population distribution)
- Compute the sample mean of these 100 random numbers
- Repeat this process 120 times

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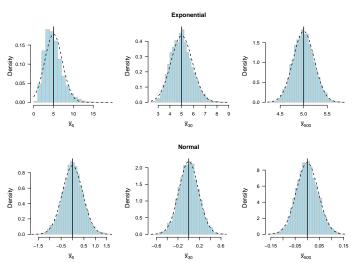
## **CLT:** Sample Size (n) and the Normal Approximation











#### Why CLT is important?

$$\bar{X}_n \approx \mathrm{N}(\mu, \frac{\sigma^2}{n})$$

- ullet The distribution of  $ar{X}_n$  is center around the true mean  $\mu$
- The variance of  $\bar{X}_n$  is decrease with n
- With normality approximation of the sampling distribution of  $\bar{X}_n$ , we can perform interval estimation about  $\mu$
- Applications: Confidence Interval, Hypothesis testing

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#### Confidence Intervals (CIs) for $\mu$

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 $\bullet$  Let's assume we know the population variance  $\sigma^2$  (will relax this assumption later on)

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- Let's assume we know the population variance  $\sigma^2$  (will relax this assumption later on)
- $(1-\alpha) \times 100\%$  CI for  $\mu$ :

$$\left[\bar{X}_n - z_{\frac{\alpha}{2}} \frac{\sigma}{\sqrt{n}}, \bar{X}_n + z_{\frac{\alpha}{2}} \frac{\sigma}{\sqrt{n}}\right],$$

where  $z_{(\frac{\alpha}{2})}$  is the  $1 - \frac{\alpha}{2}$  percentile of  $Z \sim N(0, 1)$ 



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•  $\frac{\sigma}{\sqrt{n}}$  is the standard error of  $\bar{X}_n$ , that is, the standard deviation of its sampling distribution

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#### For any $\alpha \in (0,1)$ :

# $\mathbb{P}\left(\bar{X}_n - z_{\frac{\alpha}{2}} \frac{\sigma}{\sqrt{n}} \le \mu \le \bar{X}_n + z_{\frac{\alpha}{2}} \frac{\sigma}{\sqrt{n}}\right)$ $= \mathbb{P}\left(-z_{\frac{\alpha}{2}} \frac{\sigma}{\sqrt{n}} \le \bar{X}_n - \mu \le z_{\frac{\alpha}{2}} \frac{\sigma}{\sqrt{n}}\right)$ $= \mathbb{P}\left(-z_{\frac{\alpha}{2}} \le \frac{\bar{X}_n - \mu}{\frac{\sigma}{\sqrt{n}}} \le z_{\frac{\alpha}{2}}\right)$ $=\mathbb{P}\left(-z_{\alpha} \leq Z \leq z_{\alpha}\right)$ $=\Phi(z_{\frac{\alpha}{2}})-\Phi(-z_{\frac{\alpha}{2}})$ $=1-\frac{\alpha}{2}-\frac{\alpha}{2}=1-\alpha$

#### Making Sense of Confidence Intervals Cont'd

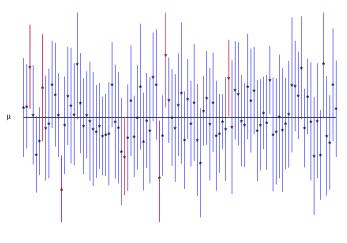


Inference for One



Point/Interval

#### Estimation



#### **Example: Average Height**



We measure the heights of 40 randomly chosen men, and get a mean height of 5'9" (≈175cm). Suppose we know the standard deviation of men's heights is 4" (≈10cm). Find the 95% confidence interval of the true mean height of ALL men.

Point/Interval

Confidence Intervals

#### WORLD HEIGHT CHART(MALE)



#### Average Height Example Cont'd

**Population Mean** 

Inference for One

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**Population Mean** 

Inference for One

- **Output** Point estimate:  $\bar{X}_{40} = \frac{\sum_{i=1}^{40} X_i}{40} = 69$  inches
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- **95%CI**: Need to find  $z_{0.05/2}$  = 1.96 from the Z-table

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Point/Interval

Confidence Intervals

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- **95%** CI for  $\mu_X$  is:

$$[69 - 1.96 \times 0.63, 69 + 1.96 \times 0.63]$$
  
= [67.77, 70.23]

#### **Properties of Confidence Intervals**

• In contrast with the point estimate,  $\bar{X}_n$ , a  $(1-\alpha)\%$  CI is an interval estimate, where the **length of CI** reflects our estimation uncertainty

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• Typical  $\alpha$  values: 0.01, 0.05, 0.1  $\Rightarrow$  99%, 95%, 90% confidence intervals. Interpretation: If we were to take random samples over and over again, then  $(1-\alpha)\%$  of these confidence intervals will contain the true  $\mu$ 

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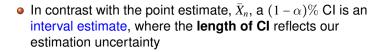
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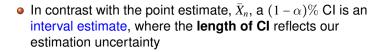
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Estimation

Confidence Intervals



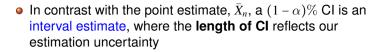
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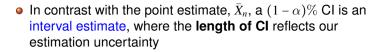


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Confidence Intervals

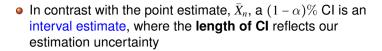


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- The length of a CI depends on
  - Population Standard Deviation:  $\sigma$
  - Confidence Level:  $1 \alpha$
  - Sample Size: n



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## **Sample Size Calculation**



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- We may want to estimate  $\mu$  with a confidence interval with a predetermined margin of error (i.e.  $z_{\alpha/2} \frac{\sigma}{\sqrt{n}}$ )
- For example, in estimating the true mean height of All men we may want our CI to be just 0.5 inches in width
- The question is then, "how many observations do we need to take so that we have the desired margin of error?"

## Sample Size Calculation Cont'd



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Estimation

Confidence Intervals

Hypothesis Testing

To compute the sample size needed to get a CI for 
$$\mu$$
 with a specified margin of error, we use the formula below

$$n = \left(\frac{z_{\alpha/2} \times \sigma}{\text{Margin of error}}\right)^2$$

**Exercise**: Derive this formula using margin of error =  $z_{\alpha/2} \frac{\sigma}{\sqrt{n}}$ 

#### **Average Height Example Revisited**



Compute the sample size needed in order to estimate the true mean height of All men such that the 95% CI to be 0.5 inches in width

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Confidence Intervals

## **Average Height Example Revisited**



Compute the sample size needed in order to estimate the true mean height of All men such that the 95% CI to be 0.5 inches in width

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Confidence Intervals

- Length of CI:  $2 \times z_{0.025} \frac{\sigma}{\sqrt{n}} = 2 \times$  margin of error
- **a** Want to find *n* s.t.  $z_{0.025} \frac{\sigma}{\sqrt{n}} = 0.25$
- **••** We have  $n = \left(\frac{1.96 \times 4}{0.25}\right)^2 = 983.4496$

Therefore, the required sample size is 984

#### Confidence Intervals When $\sigma$ Unknown



• In practice, it is unlikely that  $\sigma$  is available to us

• One reasonable option is to replace  $\sigma$  with s, the sample standard deviation

 We need to account for this added uncertainty with a (slightly) different sampling distribution that has fatter tails

⇒ Student t Distribution (William Gosset, 1908)

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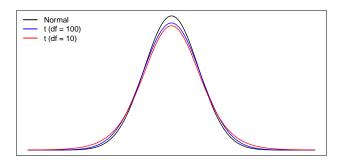
Confidence Intervals

#### **Student t Distribution**



Point/Interval

#### Confidence Intervals



- $\bullet$  Recall the standardize sampling distribution  $\frac{\bar{X}_n \mu}{\frac{\sigma}{\sqrt{n}}} \sim N(0,1)$
- Similarly , the studentized sampling distribution  $\frac{\bar{X}_n-\mu}{\frac{\bar{X}_n}{2}}\sim t_{df=n-1}$

## Confidence Intervals (CIs) for $\mu$ When $\sigma$ is Unknown

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•  $(1-\alpha) \times 100\%$  Cl for  $\mu$ :

$$\left[\bar{X}_n - t_{\frac{\alpha}{2}, n-1} \frac{s}{\sqrt{n}}, \bar{X}_n + t_{\frac{\alpha}{2}, n-1} \frac{s}{\sqrt{n}}\right],\,$$

where  $t_{\frac{\alpha}{2},n-1}$  is the  $1-\frac{\alpha}{2}$  percentile of a student t distribution with the degrees of freedom = n-1

ullet is an estimate of the standard error of  $ar{X}_n$ 

#### **Average Height Example Revisited**



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Hypothesis Testing

We measure the heights of 40 randomly chosen men, and get a mean height of 5'9" ( $\approx$ 175cm), and a standard deviation of 4.5" ( $\approx$ 11.4cm). Find the 95% confidence interval of the true mean height of ALL men.

#### Average Height Example Cont'd

O Point estimate:  $\bar{X}_{40} = \frac{\sum_{i=1}^{40} X_i}{40} = 69$  inches

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- **95%** CI for  $\mu_X$  is:

$$[69 - 2.02 \times 0.71, 69 + 2.02 \times 0.71]$$
  
= [67.57, 70.43]

# **Hypothesis Testing**

• **Hypothesis Testing**: A method for using sample data to decide between two competing claims (hypotheses) about a population characteristic (a parameter. e.g.  $\mu$ )

#### • Examples:

- The true mean starting salary for graduates of four-year business schools is \$4,500 per month  $\Rightarrow \mu$  = 4,500
- The true mean monthly income for systems analysts is at least \$6,000  $\Rightarrow \mu \ge 6,000$

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#### **Hypotheses**

- Null Hypothesis: A claim about a parameter that is initially assumed to be true. We use H<sub>0</sub> to denote a null hypothesis
- Alternative Hypothesis: The competing claim, denoted by H<sub>a</sub>
- In carrying out a test of  $H_0$  versus  $H_a$ , the hypothesis  $H_0$  will be rejected in favor of  $H_a$  only if sample evidence strongly suggests that  $H_0$  is false. If the sample data does not contain such evidence,  $H_0$  will not be rejected
- Therefore, the two possible decisions in a hypothesis test are:
  - Reject  $H_0$  (and go with  $H_a$ )
  - Fail to Reject H<sub>0</sub>



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#### **Hypotheses**



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# Be careful setting up hypotheses:

- A statistical hypothesis test is only capable of demonstrating strong support for the alternative hypothesis  $H_a$  (by rejecting the null hypothesis  $H_0$ )
- Failing to reject  $H_0$  does not show strong support for the null hypothesis only a lack of strong evidence against  $H_0$ , the null hypothesis

## The $2 \times 2$ Decision Paradigm for Hypothesis Testing

True State	Decision	
	Reject $H_0$	Fail to reject $H_0$
$H_0$ is true	Type I error	Correct
$H_0$ is false	Correct	Type II error

#### **Errors in Hypothesis Testing**

- $\bullet$  The probability of a type I error is denoted by  $\alpha$
- The probability of a type II error is denoted by  $\beta$



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