DSA 8020 R Session 7: Logistic Regression and Poisson Regression

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Logistic Regression: Horseshoe Crab Malting

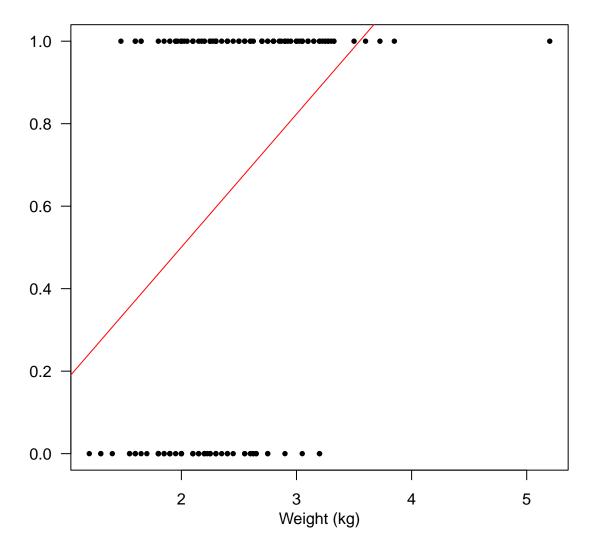
Data Source: Brockmann, H. J. (1996). Satellite male groups in horseshoe crabs, Limulus polyphemus. Ethology, 102(1), 1-21.

Load the data

```
crab <- read.table("http://users.stat.ufl.edu/~aa/cda/data/Crabs.dat", header = T)</pre>
```

Fit a Linear Regression

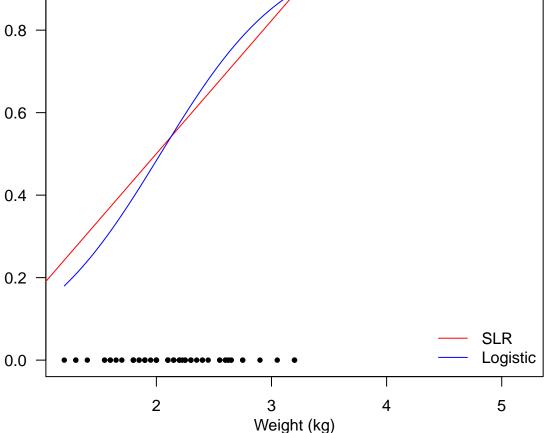
Let's fit a simple linear regression using weight as the predictor



Fit a Logistic Regression

```
logitFit <- glm(y ~ weight, data = crab, family = "binomial")</pre>
summary(logitFit)
##
## Call:
## glm(formula = y ~ weight, family = "binomial", data = crab)
## Deviance Residuals:
##
       Min
                 1Q
                     Median
                                   ЗQ
                                           Max
## -2.1108 -1.0749
                     0.5426
                               0.9122
                                        1.6285
##
## Coefficients:
##
              Estimate Std. Error z value Pr(>|z|)
## (Intercept) -3.6947
                            0.8802 -4.198 2.70e-05 ***
## weight
                 1.8151
                            0.3767 4.819 1.45e-06 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
```

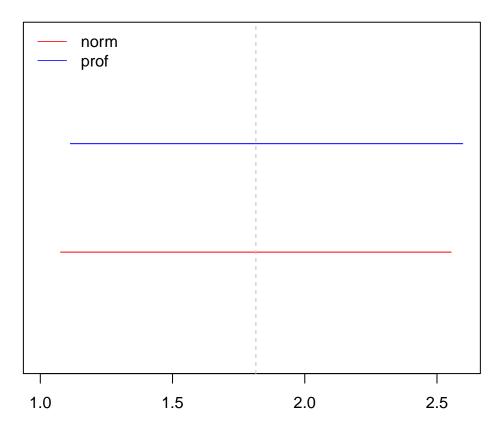
```
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 225.76 on 172 degrees of freedom
##
## Residual deviance: 195.74 on 171 degrees of freedom
## AIC: 199.74
##
## Number of Fisher Scoring iterations: 4
# Plot the fits
rg <- range(crab$weight)</pre>
xg \leftarrow seq(rg[1], rg[2], 0.01)
pred <- predict(logitFit, newdata = data.frame(weight = xg), type = "response")</pre>
par(mar = c(3.5, 3.5, 0.8, 0.6))
plot(crab$weight, crab$y, pch = 16, cex = 0.75, las = 1, xlab = "", ylab = "")
mtext("Weight (kg)", side = 1, line = 2)
abline(lmFit, col = "red")
lines(xg, pred, col = "blue")
legend("bottomright", legend = c("SLR", "Logistic"),
       col = c("red", "blue"), lty = 1, bty = "n")
1.0
```



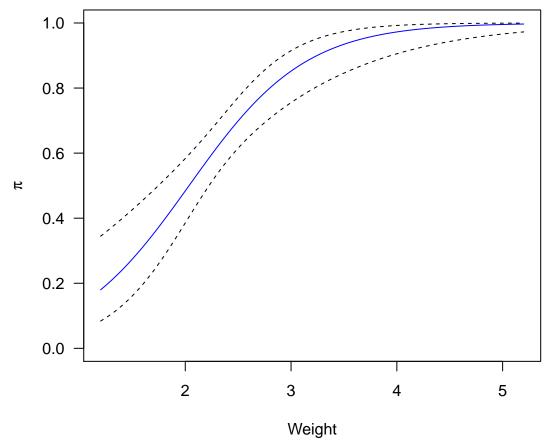
Confidence Intervals

```
# Normal approximation
est <- summary(logitFit)$coefficients</pre>
(CI_norm \leftarrow est[2, 1] + c(-1, 1) * qnorm(0.975) * est[2, 2])
## [1] 1.076834 2.553455
# Profile likelihood CI
library(MASS)
(CI_prof <- confint(logitFit)[2,])</pre>
## Waiting for profiling to be done...
      2.5 % 97.5 %
## 1.113790 2.597305
plot(1, type = "n", xlab = "", ylab = "",
     xlim = c(1, 2.6), ylim = c(-0.05, 0.1),
     yaxt = "n", main = expression(hat(beta[1])))
segments(CI_norm[1], 0, CI_norm[2], col = "red")
segments(CI_prof[1], 0.05, CI_prof[2], col = "blue")
abline(v = est[2, 1], lty = 2, col = "gray")
legend("topleft", legend = c("norm", "prof"),
       col = c("red", "blue"), lty = 1,
       lwd = 0.8, bty = "n")
```

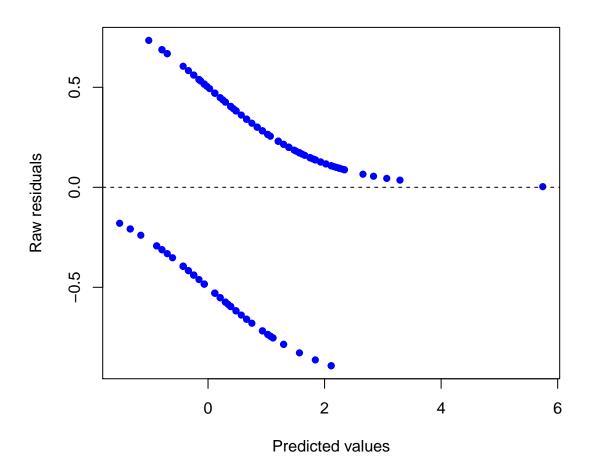




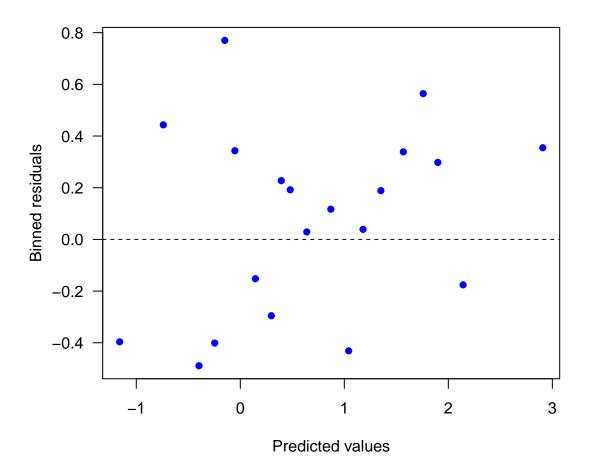
Prediction



Raw Residual plot



Binned Residuals



Model selection

```
logitFit2 <- glm(y ~ weight + width, data = crab, family = "binomial")</pre>
summary(logitFit2)
##
## glm(formula = y ~ weight + width, family = "binomial", data = crab)
##
## Deviance Residuals:
##
       Min
                 1Q
                      Median
                                   3Q
                                           Max
                      0.5304
## -2.1127 -1.0344
                               0.9006
                                        1.7207
##
## Coefficients:
               Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) -9.3547
                            3.5280 -2.652 0.00801 **
## weight
                 0.8338
                            0.6716
                                     1.241 0.21445
## width
                 0.3068
                            0.1819
                                     1.686 0.09177 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 225.76 on 172 degrees of freedom
## Residual deviance: 192.89 on 170 degrees of freedom
```

```
## AIC: 198.89
##
## Number of Fisher Scoring iterations: 4
step(logitFit2)
## Start: AIC=198.89
## y ~ weight + width
##
##
           Df Deviance
                          AIC
## - weight 1 194.45 198.45
## <none>
                192.89 198.89
## - width 1 195.74 199.74
##
## Step: AIC=198.45
## y ~ width
##
##
          Df Deviance
                         AIC
               194.45 198.45
## <none>
## - width 1 225.76 227.76
## Call: glm(formula = y ~ width, family = "binomial", data = crab)
##
## Coefficients:
## (Intercept)
                     width
     -12.3508
                    0.4972
##
##
## Degrees of Freedom: 172 Total (i.e. Null); 171 Residual
## Null Deviance:
                       225.8
## Residual Deviance: 194.5
                             AIC: 198.5
```

Poisson Regression

Flying-Bomb Hits on London During World War II [Clarke, 1946; Feller, 1950]

```
count <- c(229, 211, 93, 35, 7, 1)
grids <- 576
hits <- 537
lambda <- hits / grids
count_expected <- c(grids * dpois(0:4, lambda = lambda), grids * ppois(4, lambda = lambda, lower.tail = round(count_expected, 1)
## [1] 226.7 211.4 98.5 30.6 7.1 1.6</pre>
```

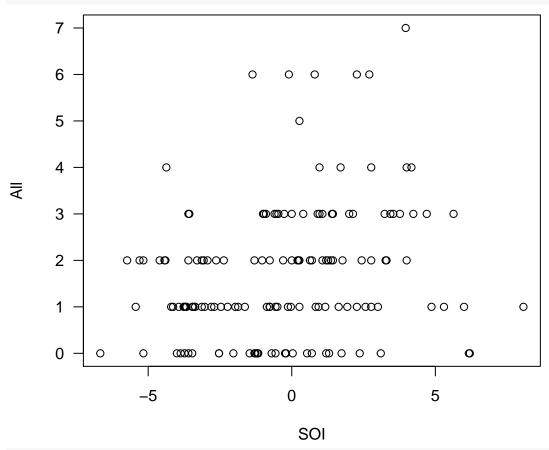
US Landfalling Hurriances

```
# load the hurriance count
con = "http://myweb.fsu.edu/jelsner/Book/Chap07/US.txt"
hurricanes = read.table(con, header = T)
head(hurricanes)
```

Year All MUS G FL E

```
## 1 1851
                      2 0
## 2 1852
             3
## 3 1853
                      0 1
## 4 1854
             2
                 1 1
## 5 1855
## 6 1856
             2
                 1 1
                      1 0
par(las = 1, mar = c(4.6, 3.9, 0.8, 0.6))
layout(matrix(c(1, 2), 1, 2, byrow = TRUE), widths = c(0.57, 0.43))
plot(hurricanes$Year, hurricanes$All, type = "h", xlab = "Year", ylab = "Hurricane count")
grid()
barplot(table(hurricanes$All), xlab = "Hurricane Count", ylab = "Number of years", main = "")
                                                        40
       6
       5
                                                        30
                                                  Number of years
Hurricane count
       4
       3
                                                        20
       2
                                                        10
       0
                                                         0
          1850
                                          2000
                    1900
                               1950
                                                               0
                                                                     2
                                                                          4
                                                                                6
                           Year
                                                                 Hurricane Count
```

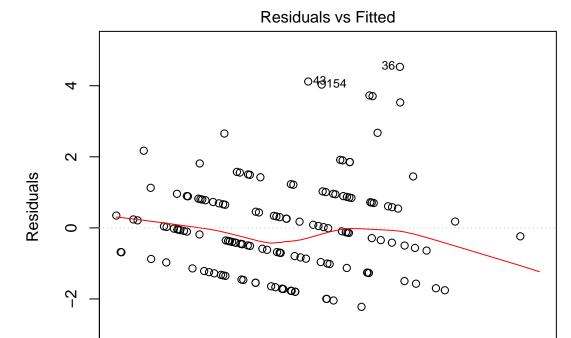
Load the environmetal variables



```
H <- hurricanes
par(mfrow = c(2, 2), mar = c(4.5, 4, 1, 0.6))
plot(range(annual$sst, na.rm = TRUE), c(0, 7), type = "n", ylab = "Hurricane count", xlab = "SST",
     las = 1)
for(i in 0:7){
  points(fivenum(annual$sst[H$All == i])[3], i, pch = 19)
  lines(c(fivenum(annual$sst[H$All == i])[1], fivenum(annual$sst[H$All == i])[2]), c(i, i))
  lines(c(fivenum(annual$sst[H$All == i])[4], fivenum(annual$sst[H$All == i])[5]), c(i, i))
plot(range(annual$soi, na.rm = TRUE), c(0, 7), type = "n", ylab = "Hurricane count", xlab = "SOI",
     las = 1)
for(i in 0:7){
  points(fivenum(annual$soi[H$All == i])[3], i, pch=19)
  lines(c(fivenum(annual$soi[H$All == i])[1], fivenum(annual$soi[H$All == i])[2]), c(i, i))
  lines(c(fivenum(annual$soi[H$All == i])[4], fivenum(annual$soi[H$All == i])[5]), c(i, i))
plot(range(annual$nao, na.rm = TRUE), c(0, 7), type = "n", ylab = "Hurricane count", xlab = "NAO",
     las = 1)
for(i in 0:7){
  points(fivenum(annual$nao[H$All == i])[3], i, pch=19)
  lines(c(fivenum(annual$nao[H$All == i])[1], fivenum(annual$nao[H$All == i])[2]), c(i, i))
  lines(c(fivenum(annual$nao[H$All == i])[4], fivenum(annual$nao[H$All == i])[5]), c(i, i))
```

```
plot(range(annual$ssn, na.rm = TRUE), c(0, 7), type = "n", ylab = "Hurricane count",
      xlab = "Sunspot number", las = 1)
for(i in 0:7){
  points(fivenum(annual$ssn[H$All == i])[3], i, pch = 19)
  lines(c(fivenum(annual$ssn[H$All == i])[1], fivenum(annual$ssn[H$All == i])[2]), c(i, i))
  lines(c(fivenum(annual$ssn[H$All == i])[4], fivenum(annual$ssn[H$All == i])[5]), c(i, i))
}
      7
      6
Hurricane count
                                                Hurricane count
      5
                                                      5
      4
      3
                                                      3
      2
                                                      2
      1
                                                      1
      0
                                                      0
                                                                         0
                                                                                    5
             -0.4
                         0.0
                              0.2
                                    0.4
                                          0.6
                                                             -5
                         SST
                                                                         SOI
      7
                                                      7
      6
                                                      6
Hurricane count
                                                Hurricane count
      5
                                                      5
      4
      3
                                                      3
      2
                                                      2
      1
      0
                                                      0
              -2
                    -1
                           0
                                 1
                                      2
                                            3
                                                          0
                                                                 50
                                                                       100
                                                                              150
                                                                                     200
                         NAO
                                                                   Sunspot number
```

Linear Regression



0

3.0

plot(lmFull, which = 3)

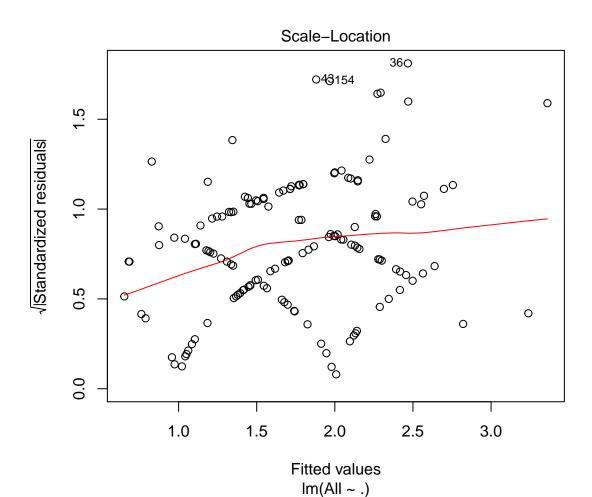
1.0

1.5

2.0

Fitted values Im(All ~ .)

2.5



Poisson Regression

```
PoiFull <- glm(All ~ ., data = data, family = "poisson")
summary(PoiFull)
##
## Call:
## glm(formula = All ~ ., family = "poisson", data = data)
##
## Deviance Residuals:
                     Median
##
       Min
                 1Q
                                   3Q
                                          Max
   -2.8530 -0.8984 -0.1376
                               0.6027
                                        2.4720
##
## Coefficients:
##
                Estimate Std. Error z value Pr(>|z|)
## (Intercept) 0.595288
                          0.103342
                                     5.760 8.39e-09 ***
## SOI
                0.061863
                          0.021319
                                     2.902 0.00371 **
                                    -2.586 0.00972 **
## NAO
               -0.166595
                          0.064427
## SST
               0.228972
                          0.255289
                                     0.897 0.36977
## SSN
               -0.002306
                          0.001372 -1.681 0.09284 .
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
## (Dispersion parameter for poisson family taken to be 1)
##
##
       Null deviance: 197.89 on 144 degrees of freedom
## Residual deviance: 174.81 on 140 degrees of freedom
## AIC: 479.64
## Number of Fisher Scoring iterations: 5
plot(data$SOI, hurricanes$All[-(1:15)], cex = 0.75, col = "gray",
     xlab = "", ylab = "", las = 1)
mtext("Hurricane Count", side = 2, line = 2)
mtext("Year", side = 1, line = 2)
points(data$SOI, predict(lmFull), col = "red",
       cex = 0.5, pch = 16)
points(data$SOI, predict(PoiFull, type = "response"), col = "blue", cex = 0.5, pch = 16)
    7
    6
    5
Hurricane Count
    4
                                                      \odot
    3
    2
    1
    0
                           0
                -5
                                                          5
                                     0
                                       Year
```