Lecture 2

Data Summary/Visualization I

Text: Chapter 2 & Chapter 3

STAT 8010 Statistical Methods I January 14, 2020 Data Summary/Visualization



Sampling Techniques

Summarizing Categorical Dat

Numerical Data

Whitney Huang Clemson University

Agenda

Data Summary/Visualization



Sampling Techniques

Summarizing
Categorical Data

Summarizing Iumerical Data

Sampling Techniques

Summarizing Categorical Data

Last Lecture

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 Sampling Technique

 Supporting
 - Summarizing Categorical Data Summarizing

Data Summary/Visu-

- Numerical Data
- Stating the problem, identifying the variable(s) of interest, and gathering data
 - Types of variables and datasets
 - Observational vs. Experimental Studies
 - Methods of sampling
- Summarizing the data
- Analyzing the data
- Reporting and interpreting the results

Today's Lecture

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Data Summary/Visu-

- Sampling Techniques
- Categorical Data
- Numerical Data
- Stating the problem, identifying the variable(s) of interest, and gathering data
 - Types of variables and datasets
 - Observational vs. Experimental Studies
 - Sampling Techniques
- Summarizing the data
- Analyzing the data
- Reporting and interpreting the results

Collecting Data: Statistical Sampling

Statistical sampling is the procedure to select a subset from a statistical **population** that is representative of the population. There are several types of sampling:

 Simple random sampling (SRS): a sample selected such that each element in the population has the same probability of being selected

Simple random sample



Data Summary/Visualization



Sampling Techniques

Categorical Data

Collecting Data: Statistical Sampling

Statistical sampling is the procedure to select a subset from a statistical **population** that is representative of the population. There are several types of sampling:

 Simple random sampling (SRS): a sample selected such that each element in the population has the same probability of being selected

Simple random sample



 Stratified sample: elements in the population are first divided into groups and a simple random sample is then taken from each group

Stratified sample





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Sampling rechniques

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Sampling cont'd

 Cluster sampling: the elements in the population are first divided into separate groups called clusters and then a simple random sample of the clusters is taken that all elements in a selected cluster are part of a sample





Data Summary/Visualization



Sampling rechniques

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Sampling cont'd

 Cluster sampling: the elements in the population are first divided into separate groups called clusters and then a simple random sample of the clusters is taken that all elements in a selected cluster are part of a sample





 Systematic sampling: randomly select one of the first k elements from the population and then every k_{th} element thereafter is picked

Systematic sample



Data Summary/Visualization



Sampling recriniques

Categorical Data

Sampling cont'd

 Cluster sampling: the elements in the population are first divided into separate groups called clusters and then a simple random sample of the clusters is taken that all elements in a selected cluster are part of a sample

Cluster sample



 Systematic sampling: randomly select one of the first k elements from the population and then every k_{th} element thereafter is picked

Systematic sample



 Convenience sampling: elements selected from the population on the basis of convenience Data Summary/Visualization



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What type of sampling was used?

 A researcher randomly chooses houses in a town. Once a particular house is chosen everyone living in the house is surveyed

A school principal decides to performs an exit interview with every 14th name from a list of graduating seniors

A biologist knows that 40% of bats are male and that 60% are female so she randomly selects 20 males and randomly selects 30 females to be in her sample

A graduate student wants to do a study on why people like bluegrass music and uses the people she meets at the next show she attends as her sample

To get an idea of the average weight of his cattle, a rancher randomly chooses to weigh 25 from his list of the animals Data Summary/Visualization

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Sampling Techniques

Summarizing

Categorical Data

Summarizing



Sampling Techniques

Summarizing Categorical Data

Summarizing Numerical Data

Summarizing Categorical Variables

Example: Sport Injuries

The paper "Profile of sport/leisure injuries treated at emergency rooms of urban hospitals." by Pelletier et al. 1991 examined the nature and number of sport/leisure injuries treated in hospital emergency rooms in a large metropolitan city. They classified non-contact sports injuries by sport, resulting in the following data set:

Sport		
Soccer		
Basketball		
Others		
Basketball		
Touch Football		
Others		
Touch Football		
Volleyball		
Baseball/softball		
:		

Question: How to summarize this data set?

Frequency Table

 A frequency table for categorical data is a table that displays the possible categories along with the associated frequencies or relative frequencies

- The frequency for a particular category is the number of times the category appears in the data set
- The relative frequency for a particular category is the fraction or proportion of the time that the category appears in the data set. It is calculated as:

relative frequency =



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Categorical Data

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Frequencies and Relative Frequencies

<pre>> table(sport) sport</pre>					
Baseball/softball	Basketball	Bicycling	Jogging/running		
11	19	11	11		
Others	Soccer	Touch Football	Volleyball		
47	24	38	17		
<pre>> table(sport) / dim(sport)[1] sport</pre>					
Baseball/softball	Basketball	Bicycling	Jogging/running		
0.06179775	0.10674157	0.06179775	0.06179775		
Others	Soccer	Touch Football	Volleyball		
0.26404494	0.13483146	0.21348315	0.09550562		

Data Summary/Visualization



Sampling Techniques

Summarizing Categorical Data

Frequencies and Relative Frequencies

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Sampling Technique
Summarizing
Categorical Data

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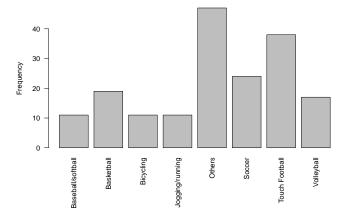
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How could we visualize these information?

⇒ Making a bar chart and/or a pie chart

Bar Charts

A bar chart draws a bar with a height proportional to the count in the table:



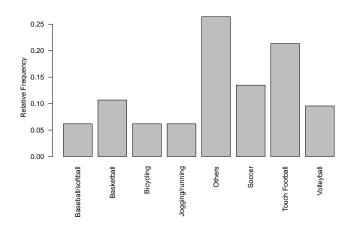
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Bar Charts cont'd



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Pie Charts



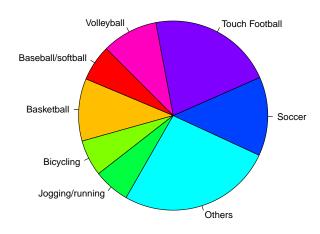
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Pie Charts cont'd



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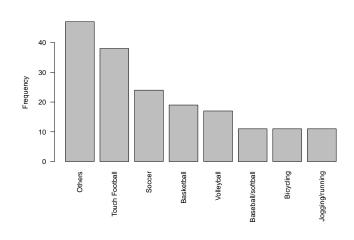
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Categorical Data

Summarizing Numerical Data

Discussion: Which one you prefer to visualize categorical variables. Why?

A Good Bar Chart



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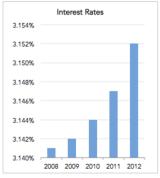


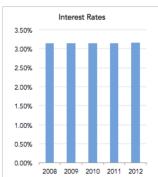
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Summarizing Categorical Data

A (Potential) Misleading Bar Chart

Same Data, Different Y-Axis





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Summarizing Categorical Data

Example: O'Hare Airport Flight Data



	carrier	origin
1	UA	EWR
2	AA	LGA
3	AA	LGA
4	AA	LGA
5	UA	LGA
6	UA	EWR

In this example, we have two categorical variables, carrier and origin, respectively. How to summarize/visualize this dataset?

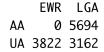




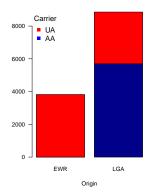
Sampling Techniques

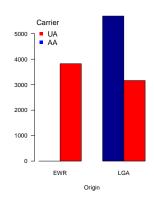
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ORD Flight Data Cont'd



EWR LGA AA 0.00 0.45 UA 0.30 0.25





Data Summary/Visualization



Sampling Techniques

Summarizing Categorical Data

Summarizing Numerical Data

Summarizing Numerical Variables

Example: Murder arrests (per 100,000) in US States in 1973

Data Summary/Visualization

Sampling Technique

Data: 13.2, 10.0, 8.1, 8.8, 9.0, 7.9, 3.3, 5.9, 15.4, 17.4, 5.3, 2.6, 10.4, 7.2, 2.2, 6.0, 9.7, 15.4, 2.1, 11.3, 4.4, 12.1, 2.7, 16.1, 9.0, 6.0, 4.3, 12.2, 2.1, 7.4, 11.4, 11.1, 13.0, 0.8, 7.3, 6.6, 4.9, 6.3, 3.4, 14.4, 3.8, 13.2, 12.7, 3.2, 2.2, 8.5, 4.0, 5.7, 2.6, 6.8.

Question: How to graphically summarize this data set?

Stem-and-Leaf Plot

```
The decimal point is at the I
   18
   | 1122667
    2348
     0349
   1 379
   1 00368
   1 2349
    158
     007
    04
    134
12 | 127
    022
16
```

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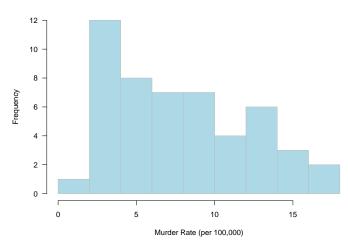


Sampling Techniques

Summarizing Categorical Data

Histogram

Histogram of US Murder Rate in 1973



Data Summary/Visualization

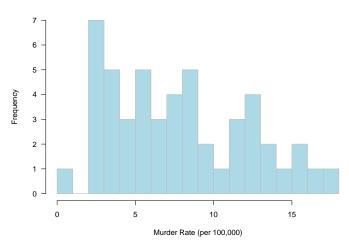


Sampling Techniques

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Categorical Data

Histogram

Histogram of US Murder Rate in 1973



Data Summary/Visualization

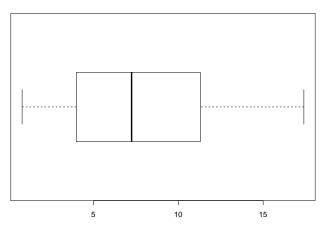


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Box-and-Whisker Plot

Murder Rate (per 100,000)



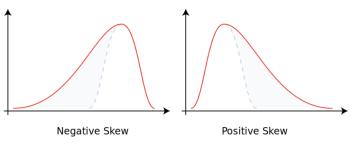
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Summarizing Categorical Data

Shape of Distributions



Source: Skewness - Wikipedia

In the rest of the class, we will talk about how to summarize a numerical variable in terms of its center and spread

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Measures of Center

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 Sampling Techniques
 - Summarizing Numerical Data
- A measure of center attempts to report a "typical" value for the variable
- When a measure of center is calculated with sample data it is a statistic
- When a measure of center is calculated with popular (e.g., census data) it is a parameter
- Measures: Mean, Median, Mode

• The population mean, denoted by μ_X , is the sum of all the population values $(\{X_i, \dots, X_N\})$ divided by the size of the population (N). That is,

$$\mu_X = \frac{\sum_{i=1}^N X_i}{N}$$

• The sample mean, denoted by X is the sum of all the sample values $(\{X_1, \dots, X_n\})$ divided by the sample size (n). That is,

$$\bar{X} = \frac{\sum_{i=1}^{n} X_i}{n}$$

Median



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The median is the value separating the higher half from the lower half of a data sample

How to compute the median: Order the n observations in a data set from smallest to largest, then

 $\mbox{Median} = \left\{ \begin{array}{ll} \mbox{the single middle value,} & \mbox{n odd} \\ \mbox{the average of the middle two values,} & \mbox{n even} \end{array} \right.$

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Mode

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The mode is the value of the observation that appears most frequently

How to compute the mode(s): Order the observations in a data set from smallest to largest, then find the number that is repeated more often than any other

Example

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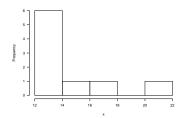
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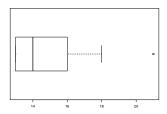
Categorical Data

Summarizing Numerical Data

Suppose we have the following list of values: 13, 18, 13, 14, 13, 16, 14, 21, 13

 Plot this "data set" and describe the shape of the distribution





Data Summary/Visualization



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Summarizing
Categorical Data

Summarizing Numerical Data

Suppose we have the following list of values: 13, 18, 13, 14, 13, 16, 14, 21, 13

$$\bar{X} = \sum_{i=1}^{9} \frac{13 + 18 + 13 + 14 + 13 + 16 + 14 + 21 + 13}{9} = 15$$

- Find the sample median
 - Order the data first: 13, 13, 13, 13, 14, 14, 16, 18, 21

Data Summary/Visualization



Sampling Techniques

Summarizing
Categorical Data

Summarizing Numerical Data

Suppose we have the following list of values: 13, 18, 13, 14, 13, 16, 14, 21, 13

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- Find the sample median
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Data Summary/Visualization



Sampling Techniques

Summarizing
Categorical Data

Summarizing Numerical Data

Suppose we have the following list of values: 13, 18, 13, 14, 13, 16, 14, 21, 13

$$\bar{X} = \sum_{i=1}^{9} \frac{13 + 18 + 13 + 14 + 13 + 16 + 14 + 21 + 13}{9} = 15$$

- Find the sample median
 - Order the data first: 13, 13, 13, 13, 14, 14, 16, 18, 21
 - Compute the sample size n and identify (or compute) the median value

Data Summary/Visualization



Sampling Techniques

Summarizing
Categorical Data

Summarizing Numerical Data

Suppose we have the following list of values: 13, 18, 13, 14, 13, 16, 14, 21, 13

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Data Summary/Visualization



Sampling Techniques

Summarizing
Categorical Data

Summarizing Numerical Data

Suppose we have the following list of values: 13, 18, 13, 14, 13, 16, 14, 21, 13

$$\bar{X} = \sum_{i=1}^{9} \frac{13 + 18 + 13 + 14 + 13 + 16 + 14 + 21 + 13}{9} = 15$$

- Find the sample median
 - Order the data first: 13, 13, 13, 13, 14, 14, 16, 18, 21
 - Compute the sample size n and identify (or compute) the median value
 - 0 $n = 9 \Rightarrow$ the median is the 5th number, which is 14

Data Summary/Visualization



Sampling Techniques

Summarizing Categorical Data

- Find the mode
 - Order the data first: 13, 13, 13, 13, 14, 14, 16, 18, 21

Data Summary/Visualization



Sampling Techniques

Summarizing Categorical Data

- Find the mode
 - Order the data first: 13, 13, 13, 13, 14, 14, 16, 18, 21

Data Summary/Visualization



Sampling Techniques

Summarizing
Categorical Data

- Find the mode
 - Order the data first: 13, 13, 13, 13, 14, 14, 16, 18, 21
 - ② We have 3 13 and 2 14 \Rightarrow 13 is the mode

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Sampling Techniques

Categorical Data

Numerical Data

Suppose we have the following list of values: 13, 18, 13, 14, 13, 16, 14, 210, 13

$$\bar{X} = \sum_{i=1}^{9} \frac{13 + 18 + 13 + 14 + 13 + 16 + 14 + 210 + 13}{9} = 36$$

- Find the sample median
 - Order the data first: 13, 13, 13, 13, 14, 14, 16, 18, 210

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Sampling Techniques

Categorical Data

Numerical Data

Suppose we have the following list of values: 13, 18, 13, 14, 13, 16, 14, 210, 13

$$\bar{X} = \sum_{i=1}^{9} \frac{13 + 18 + 13 + 14 + 13 + 16 + 14 + 210 + 13}{9} = 36$$

- Find the sample median
 - Order the data first: 13, 13, 13, 13, 14, 14, 16, 18, 210

Data Summary/Visualization



Sampling Techniques

Categorical Data

Summarizing Numerical Data

Suppose we have the following list of values: 13, 18, 13, 14, 13, 16, 14, 210, 13

$$\bar{X} = \sum_{i=1}^{9} \frac{13 + 18 + 13 + 14 + 13 + 16 + 14 + 210 + 13}{9} = 36$$

- Find the sample median
 - Order the data first: 13, 13, 13, 13, 14, 14, 16, 18, 210
 - Compute the sample size n and identify (or compute) the median value

Data Summary/Visualization



Sampling Techniques

Categorical Data

Summarizing Numerical Data

Suppose we have the following list of values: 13, 18, 13, 14, 13, 16, 14, 210, 13

$$\bar{X} = \sum_{i=1}^{9} \frac{13 + 18 + 13 + 14 + 13 + 16 + 14 + 210 + 13}{9} = 36$$

- Find the sample median
 - Order the data first: 13, 13, 13, 13, 14, 14, 16, 18, 210
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Data Summary/Visualization



Sampling Techniques

Categorical Data

Numerical Data

Suppose we have the following list of values: 13, 18, 13, 14, 13, 16, 14, 210, 13

$$\bar{X} = \sum_{i=1}^{9} \frac{13 + 18 + 13 + 14 + 13 + 16 + 14 + 210 + 13}{9} = 36$$

- Find the sample median
 - Order the data first: 13, 13, 13, 13, 14, 14, 16, 18, 210
 - Compute the sample size n and identify (or compute) the median value

- Find the mode
 - Order the data first: 13, 13, 13, 13, 14, 14, 16, 18, 210

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Summarizing Categorical Data

- Find the mode
 - Order the data first: 13, 13, 13, 13, 14, 14, 16, 18, 210

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- Find the mode
 - Order the data first: 13, 13, 13, 13, 14, 14, 16, 18, 210
 - ② We have 3 13 and 2 14 \Rightarrow 13 is (still) the mode

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- Find the mode
 - Order the data first: 13, 13, 13, 13, 14, 14, 16, 18, 210
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Sampling Techniques

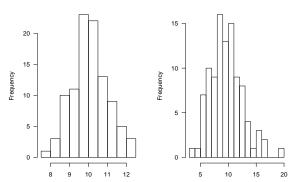
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Summarizing Numerical Data

- Find the mode
 - Order the data first: 13, 13, 13, 13, 14, 14, 16, 18, 210
 - 2 We have 3 13 and 2 14 \Rightarrow 13 is (still) the mode

What is the take-home message?

Measures of Spread



 Measures: Range, Variance/Standard Deviation, Interquartile range (IQR) Data Summary/Visualization



Sampling Techniques

Summarizing Categorical Data

Range

The range of a dataset is the difference between the largest and smallest values

Range = Largest Value - Smallest Value

 Compute the range of the following list of values: 13, 18, 13, 14, 13, 16, 14, 21, 13

 Compute the range of the following list of values: 13, 18, 13, 14, 13, 16, 14, 210, 13

Question: Is Range a robust statistic?



Sampling Techniques

Summarizing Categorical Data

Standard Deviation/Variance

- The sample standard deviation (variance), denoted by s (s^2), is a measure of the amount of variation of data. s (s^2) can be used as the estimate of the population standard deviation (varaince), denoted by σ (σ^2)
- s is calculated in the following way:
 - igotimes Calculate the sample mean \bar{X}
 - ② Calculate the deviation (from the sample mean) for each observation (i.e., $X_i \bar{X}$, $i = 1, \dots, n$)
 - **3** Square each deviation and add them (i.e., $\sum_{i=1}^{n} (X_i \bar{X})^2$)
 - O Divide by n-1 and take the square root, that is,

$$s = \sqrt{\frac{\sum_{i=1}^{n} (X_i - \bar{X})^2}{n-1}}$$



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Numerical Data

Example

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Sampling Techniques

Summarizing Categorical Data

Summarizing Numerical Data

 Compute s of the following list of values: 13, 18, 13, 14, 13, 16, 14, 21, 13

• Compute *s* of the following list of values: 13, 18, 13, 14, 13, 16, 14, 210, 13

Question: Is standard deviation a robust statistic?

Interguartile range (IQR)



• IQR = $Q_3 - Q_1$, where Q_1 is the Lower Quartile (the median of the lower half of the data) and Q_3 is the Upper Quartile (the median of the upper half of the data)

 Compute the IQR of the following list of values: 13, 18, 13, 14, 13, 16, 14, 21, 13

 Compute the IQR of the following list of values: 13, 18, 13, 14, 13, 16, 14, **210**, 13

Question: Is IQR a robust statistic?

Summary

In this lecture, we learned

- Sampling Techniques
- Summarizing Categorical Data
- Summarizing Numerical Data

In next lecture we will learn

- How to construct a boxplot
- How to visualize numerical + categorical variables and numerical + numerical variables
- How to visualize time series, cross-sectional, and spatio-temporal Data sets





Sampling Techniques

Categorical Dat