# STAT 8010 R Lab 15: Simple Linear Regression I

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## Example: Maximum Heart Rate vs. Age

The maximum heart rate ( $HR_{max}$ ) of a person is often said to be related to age (Age) by the equation:

$$HR_{max} = 220 - Age$$

Let's use a dataset to assess this statement.

#### Load the dataset

There are several ways to load a dataset into R:

• Importing Data over the Internet

```
dat <- read.csv('http://whitneyhuang83.github.io/STAT8010/Data/maxHeartRate.csv', header = T)</pre>
```

Let's take a look at the data

dat

```
Age MaxHeartRate
##
## 1
       18
                     202
## 2
       23
                     186
       25
## 3
                     187
## 4
       35
                     180
## 5
       65
                     156
## 6
       54
                     169
## 7
       34
                     174
## 8
       56
                     172
## 9
       72
                     153
## 10
       19
                     199
## 11
       23
                     193
## 12
       42
                     174
## 13
       18
                     198
## 14
       39
                     183
       37
                     178
## 15
```

• Read the dataset from you computer

```
dat <- read.csv('maxHeartRate.csv', header = T)</pre>
```

• If the dataset is not too big, you can type the data into R

```
age <- c(18, 23, 25, 35, 65, 54, 34, 56, 72, 19, 23, 42, 18, 39, 37)

maxHeartRate <- c(202, 186, 187, 180, 156, 169, 174, 172, 153,

199, 193, 174, 198, 183, 178)

dat <- data.frame(cbind(age, maxHeartRate))
```

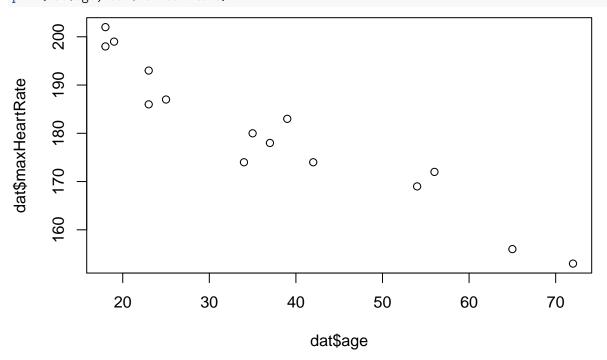
Examine the data before fitting models

```
summary(dat)
##
                      maxHeartRate
         age
           :18.00
##
                            :153.0
    1st Qu.:23.00
                     1st Qu.:173.0
##
##
    Median :35.00
                     Median :180.0
##
    Mean
           :37.33
                     Mean
                             :180.3
##
    3rd Qu.:48.00
                     3rd Qu.:190.0
           :72.00
                     Max.
                             :202.0
   {\tt Max.}
var(dat$age); var(dat$maxHeartRate)
## [1] 305.8095
## [1] 214.0667
cov(dat$age, dat$maxHeartRate)
## [1] -243.9524
cor(dat$age, dat$maxHeartRate)
## [1] -0.9534656
```

## Plot the data before fitting models

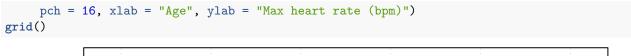
This is what the scatterplot would look like by default. Put predictor (age) to the first argument and response (maxHeartRate) to the second argument.

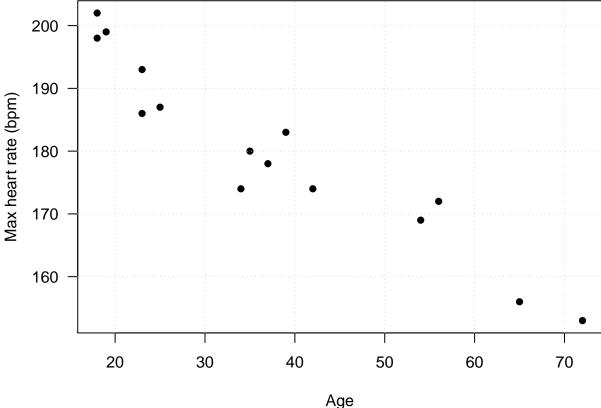
plot(dat\$age, dat\$maxHeartRate)



Let's make the plot look nicer (type ?plot to learn more).

```
par(las = 1, mar = c(4.1, 4.1, 1.1, 1.1))
plot(dat$age, dat$maxHeartRate,
```





Question: Describe the direction, strength, and the form of the relationship.

### Simple linear regression

• Fitted values:  $\hat{y} = \hat{\beta}_0 + \hat{\beta}_1 x$  Y\_hat <- beta\_0 + beta\_1 \* X

Y\_hat

Let's do the calculations to figure out the regression coefficients as well as the standard deviation of the random error.

```
• Slope: \hat{\beta}_1 = \frac{\sum_{i=1}^n (y_i - \bar{y})(x_i - \bar{x})}{\sum_{i=1}^n (x_i - \bar{x})^2}

X <- dat$age; Y <- dat$maxHeartRate
Y_diff <- Y - mean(Y)
X_diff <- X - mean(X)
beta_1 <- sum(Y_diff * X_diff) / sum((X_diff)^2)
beta_1

## [1] -0.7977266

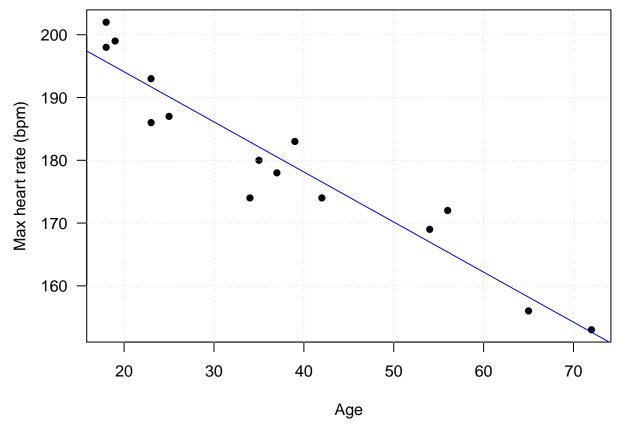
• Intercept: \hat{\beta}_0 = \bar{y} - \bar{x}\hat{\beta}_1
beta_0 <- mean(Y) - mean(X) * beta_1

## [1] 210.0485
```

```
## [1] 195.6894 191.7007 190.1053 182.1280 158.1962 166.9712 182.9258 165.3758 ## [9] 152.6121 194.8917 191.7007 176.5439 195.6894 178.9371 180.5326  \hat{\sigma} : \hat{\sigma}^2 = \frac{\sum_{i=1}^n (y_i - \hat{y}_i)^2}{n-2}  sigma2 <- sum((Y - Y_hat)^2) / (length(Y) - 2) sqrt(sigma2)
```

## ## [1] 4.577799

Add the fitted regression line to the scatterplot



#### Let R do all the work

```
fit <- lm(maxHeartRate ~ age, data = dat)
summary(fit)

##
## Call:
## lm(formula = maxHeartRate ~ age, data = dat)
##</pre>
```

```
## Residuals:
##
      Min
               1Q Median
                            3Q
                                     Max
## -8.9258 -2.5383 0.3879 3.1867 6.6242
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 210.04846 2.86694 73.27 < 2e-16 ***
               ## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 4.578 on 13 degrees of freedom
## Multiple R-squared: 0.9091, Adjusted R-squared: 0.9021
                130 on 1 and 13 DF, p-value: 3.848e-08
## F-statistic:
  • Regression coefficients
fit$coefficients
## (Intercept)
                      age
## 210.0484584 -0.7977266
  • Fitted values
fit$fitted.values
                  2
                           3
                                   4
                                            5
                                                    6
## 195.6894 191.7007 190.1053 182.1280 158.1962 166.9712 182.9258 165.3758
         9
                 10
                         11
                                  12
                                           13
                                                   14
                                                            15
## 152.6121 194.8917 191.7007 176.5439 195.6894 178.9371 180.5326
  • \hat{\sigma}
summary(fit)$sigma
```

## [1] 4.577799