Introduction to Design of Experiments



Definitions and Preliminaries

Principles of
Experimental Design

Experimental Unit

History of Experimental Desig

Lecture 8

Introduction to Design of Experiments

Reading: Oehlert Chapters 1, 2; Dean-Voss-Draguljić Chapters 1, 2

DSA 8020 Statistical Methods II February 22-26, 2021

> Whitney Huang Clemson University

Agenda

- Introduction to Design of Experiments
- CLEMS N
 - Pefinitions and Preliminaries
- Principles of Experimental Design
- Experimental Unit

History of Experimental Design

- Definitions and Preliminaries
- Fundamental Principles of Experimental Design
- Experimental Unit



Preliminaries

Principles of Experimental Design

Experimental Offic

- Specific question: How do battery types vary with respect to life-per-unit cost?
- Response: Time (per unit cost) to exhaust battery under standard load
- Comparative: Difference between 4 battery types
- Controlled: All compared using the same device
- Replication: Four batteries of each type tested

Some Definitions



- Factor: variable whose influence upon a response variable is being studied in the experiment
- Factor level: numerical values or settings for a factor
- Treatment: set of values for all factors.
- Experimental unit: object to which a treatment is applied
- Randomization: using a chance mechanism to assign treatments to experimental units

An experiment applies treatments to experimental units and measures responses.

- Want to learn about treatments (e.g., dose of drug; nano-tech coating for a fabric)
- Responses tell us how the treatment worked (patient get better; stain resistance)
- Experimenter assigns treatments to experimental units (e.g., a patient; a bolt of fabric)

 An observational study has the same triple of treatment, unit, and response, but one observes the assignment of treatments to units (e.g., human health studies on cigarette smoke and adverse health effects) Introduction to Design of Experiments



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- What makes an experimental study special is control. The experimenter gets to control the assignment of treatments to the experimental units

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Experiments can make causal inference while observational studies find association

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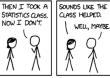
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Source: Slide 5 at http://users.stat.umn.edu/~gary/classes/5303/lectures/Introduction.pdf

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Why Designed Experiments?

Experiments

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- Design for direct comparison of treatments
- Design to reduce bias in comparisons
- Design to reduce and estimate the variability



Definitions and

Fundamental Principles of Experimental Design

Experimental Unit

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Fundamental Principles: Replication, Randomization, and Blocking

- Each treatment is applied to (experimental) units that are representative of the population
- Enable the estimation/quantification of experimental error using standard deviation
- Decrease variance of estimates and increase the power to detect significant differences: for independent y'is,

$$\operatorname{Var}(\frac{1}{n}\sum_{i=1}^{n}y_{i}) = \frac{1}{n}\operatorname{Var}(y_{1})$$

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History of Experimental Design

Use of a chance mechanism such as random number generators to assign treatments to (experimental) units. It has the following advantages:

- Protect against latent variables or "lurking" variables
- Reduce influence of subjective bias in treatment assignments (e.g., clinical trials)
- Ensure validity of statistical inference

A **block** refers to a collection of homogeneous units. Effective blocking: larger between-block variations than within-block variations.

Examples: hours, batches, lots, pairs of twins.

- Run and compare treatments within the same blocks to eliminate block-block variation and reduce variability of treatment effects estimates
- Block what you can and randomize what you cannot

- Perhaps the most important concept in statistical design
- The experimental unit is the unit (subject, plant, pot, animal) which is randomly assigned to a treatment
- The experimental unit defines the unit to be replicated to increase degrees of freedom

If a group of "units" must have the same treatment, they are likely measurement units (MUs) rather than experimental units (EUs)

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Experimental Unit

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Examples

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Preliminaries Fundamental

Experimental Unit

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Examples

Fertilizer is applied to the pots. Plants are not the EUs

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Definitions and Preliminaries

Experimental Unit

If a group of "units" must have the same treatment, they are likely measurement units (MUs) rather than experimental units (EUs)

Examples

- Fertilizer is applied to the pots. Plants are not the EUs
- Different food placed in tanks containing the fish. Fish are not the EUs

A Brief History of Experimental Design

- 1. Agricultural Era:
 - R.A. Fisher, Rothamsted Agricultural Experimental Station (1930, England)
 - Introduced statistical experimental design and data analysis
 - Summarized the fundamental principles: replication, randomization, and blocking
 - An influential book, The Design of Experiments
 The Design of Experiments

by RA Fisher



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A Brief History of Experimental Design Cont'd

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- 2. Industrial Era:
 - Process modeling and optimization
 - George Box and coworkers in chemical industries and other processing industries
 - Empirical modeling, response surface methodologies, central composite design
- 3. Quality Era:
 - Quality improvement and variation reduction
 - Taguchi and robust parameter design

A Brief History of Experimental Design Cont'd

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Experimental Design

4. Current State of Experimental Design:

- Popular outside statistics, and an indispensable tool in many scientific/engineering endeavors
- New challenges:
 - Large and complex experiments, e.g., screening design in pharmaceutical industry, experimental design in biotechnology
 - Computer experiments: efficient ways to model complex systems based on computer simulation
 - ...

Plans for the Next Three Weeks

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Experimental Design

- Completely Randomized Designs
- Randomized Complete Block Designs, Factorial Designs, and Split-Plot Designs
- Random and Mixed Effects Models, Computer Experiments