STAT 8020 R Lab 2: Simple Linear Regression II

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Contents

Maximum Heart Rate vs. Age Example

First Step: Load the data

```
dat <- read.csv('http://whitneyhuang83.github.io/STAT8010/Data/maxHeartRate.csv', header = T)
head(dat)</pre>
```

```
Age MaxHeartRate
##
## 1 18
                  202
## 2 23
                  186
## 3 25
                   187
## 4
      35
                   180
## 5
      65
                   156
## 6 54
                   169
```

attach(dat)

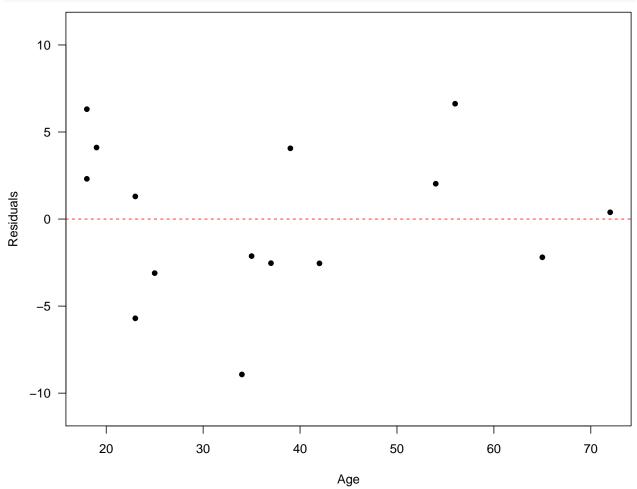
Fitting a simple linear regression

```
fit <- lm(MaxHeartRate ~ Age)</pre>
summary(fit)
## Call:
## lm(formula = MaxHeartRate ~ Age)
## Residuals:
##
       Min
                1Q Median
                                       Max
## -8.9258 -2.5383 0.3879 3.1867 6.6242
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
                                     73.27 < 2e-16 ***
## (Intercept) 210.04846
                            2.86694
                -0.79773
                            0.06996 -11.40 3.85e-08 ***
## Age
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 4.578 on 13 degrees of freedom
## Multiple R-squared: 0.9091, Adjusted R-squared: 0.9021
```

```
## F-statistic: 130 on 1 and 13 DF, p-value: 3.848e-08
```

Residual plots

```
par(las = 1, mar = c(4.1, 4.1, 1.1, 1.1))
plot(Age, fit$residuals, pch = 16, ylab = "Residuals", ylim = c(-11, 11))
abline(h = 0, col = "red", lty = 2)
```



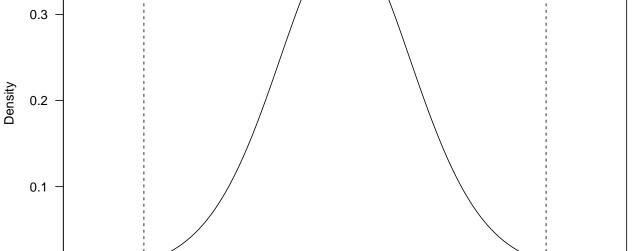
Hypothesis Tests for β_1

```
H_0: \beta_1 = -1 \text{ vs. } H_a: \beta_1 \neq -1 \text{ with } \alpha = 0.05
```

```
beta1_hat <- summary(fit)[["coefficients"]][, 1][2]
se_beta1 <- summary(fit)[["coefficients"]][, 2][2]
beta1_null <- -1
t_star <- (beta1_hat - beta1_null) / se_beta1
p_value <- 2 * pt(t_star, 13, lower.tail = F)
p_value

## Age
## 0.01262031</pre>
```

par(las = 1)



Test statistic

0

2

-2

Confidence Interval

0.0

```
\beta_1 alpha = 0.05  
CI_beta1 <- c(beta1_hat - qt(1 - alpha / 2, 13) * se_beta1, beta1_hat + qt(1 - alpha / 2, 13) * se_beta1)  
CI_beta1  
## Age Age ## -0.9488720 -0.6465811  
Y_h|X_h=40
```

```
Age_new = data.frame(Age = 40)
hat_Y <- fit$coefficients[1] + fit$coefficients[2] * 40</pre>
hat_Y
## (Intercept)
     178.1394
##
predict(fit, Age_new, interval = "confidence")
          fit
                   lwr
                             upr
## 1 178.1394 175.5543 180.7245
predict(fit, Age_new, interval = "predict")
          fit
                   lwr
## 1 178.1394 167.9174 188.3614
Check
sd <- sqrt((sum(fit$residuals^2) / 13))</pre>
ME \leftarrow qt(1 - alpha / 2, 13) * sd * sqrt(1 + 1 / 15 + (40 - mean(Age))^(2) / sum((Age - mean(Age))^2))
c(hat_Y - ME, hat_Y + ME)
## (Intercept) (Intercept)
      167.9174
                  188.3614
##
```