

Some Thoughts on Quantifying Storm Surge Risk

Whitney Huang

Joint work with SAMS1 Storm Surge Working Group



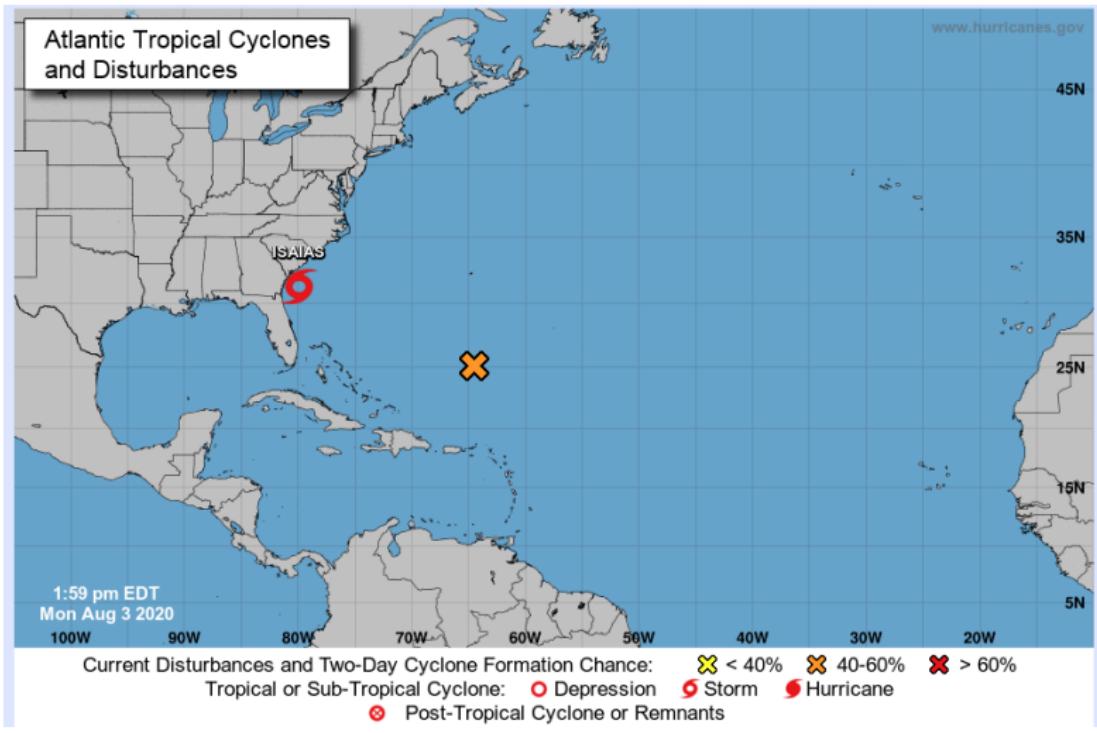
Uncertainty Quantification for Environmental Applications
August 6, 2020



SAMSI Storm Surge Working Group

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- ▶ Input modeling: Veronica Berrocal (UMich), **Qiuyi Wu (URochester)**, Anirban Mondal, **Kai Yin (CWRU)**
- ▶ Tail estimation: Richard Smith (UNC)
- ▶ SAMSI Volcanic Hazards Group: Bruce Pitman (SUNY Buffalo), Elaine Spiller (Marquette), Robert Wolpert (Duke), James Berger (Duke)

Hurricane ISAIAS



Hurricane, storm surge, and flooding

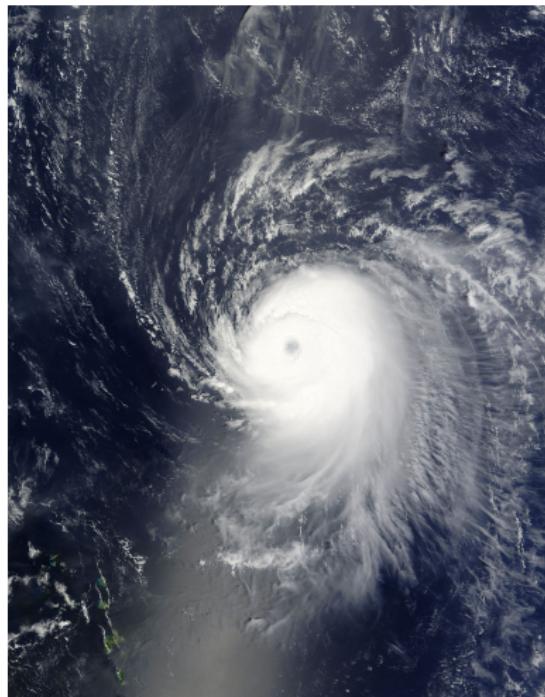


Figure: Source: NASA



Figure: Courtesy of NOAA

The problem: Storm surge height estimation

Applications

- ▶ **Flood insurance:** The Federal Emergency Management Agency (FEMA) requires an estimation of the magnitude of surges in terms of 10-, 50-, 100-, and 500-year return levels for coastal areas to determine insurance rates
- ▶ **Flood mitigation:** To assess whether coastal nuclear plants meet 1 in 10,000 year flood protection criteria.

One could use tide gauge observations to estimate, say, 100-year return level at a given location. But

1) Limited data coverage; 2) Hurricane are rare

The problem: Storm surge height estimation

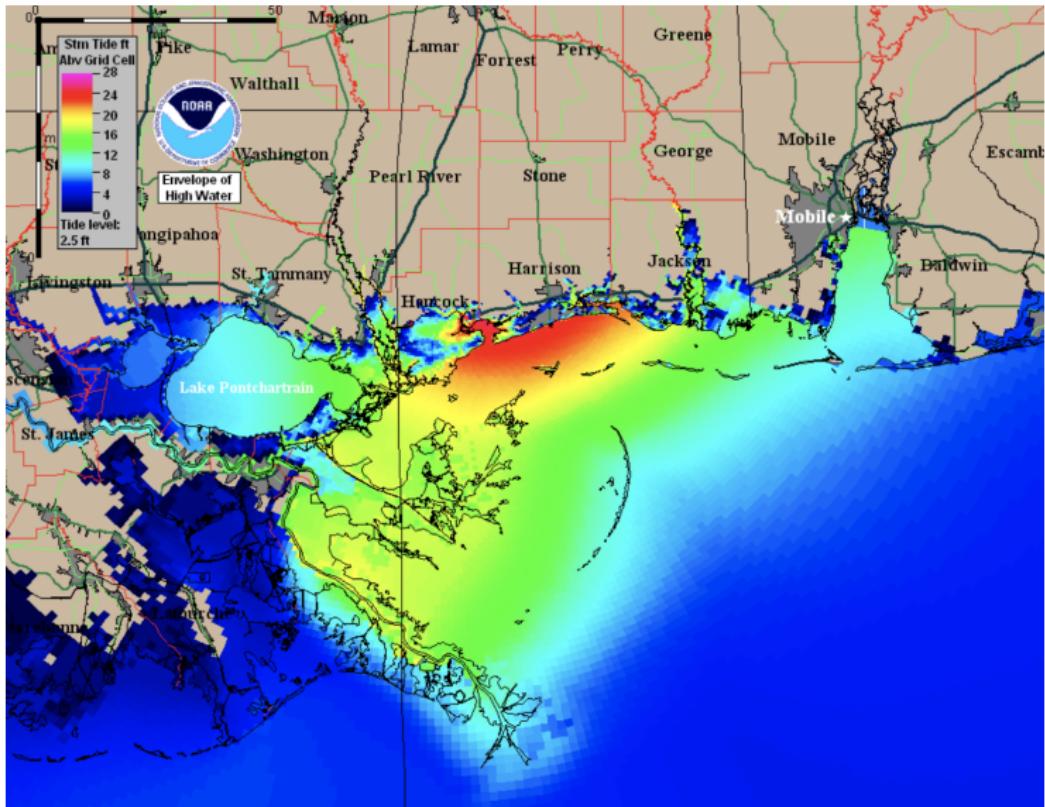
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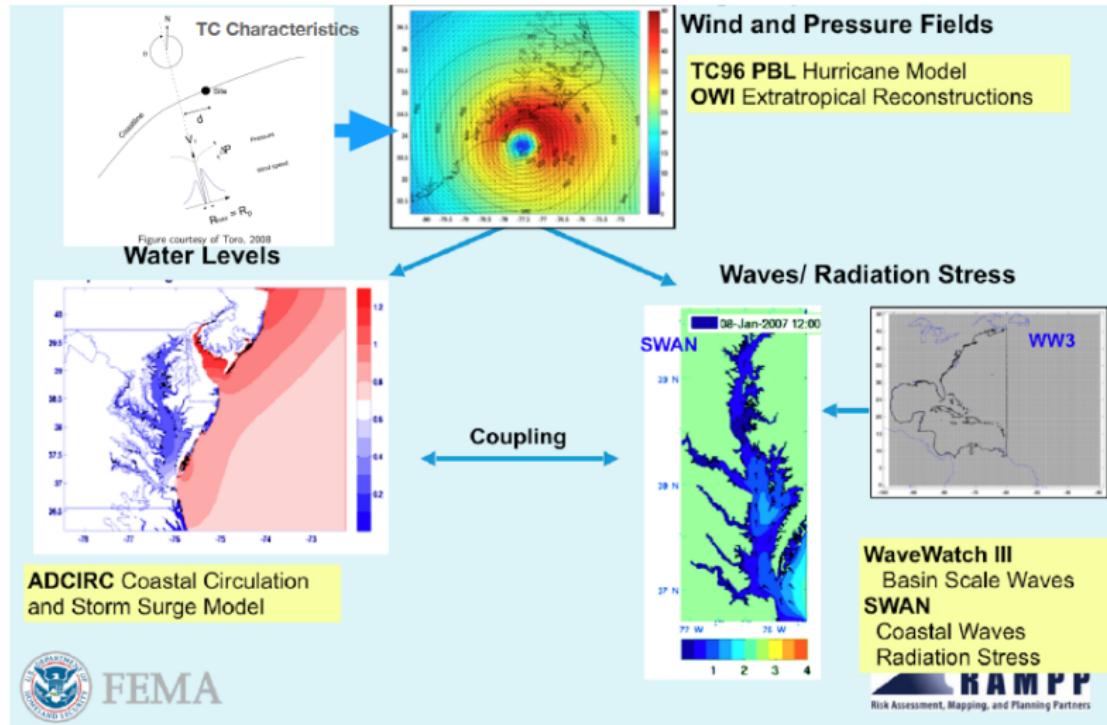
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This is what National Hurricane Center (NHC) will use

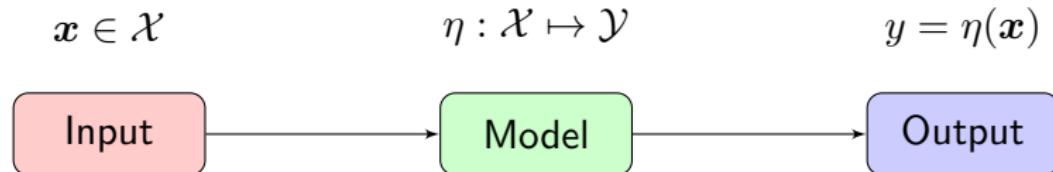


Modeling storm surge using computer simulations



Courtesy of Gangai (Dewberry) & Danforth (FEMA)

Workflow for Quantifying Storm Surge Risk



TC Characteristics

- ▶ limited data
- ▶ sparse in space and time

Task: Estimating $f(x)$

Computer Model

- ▶ deterministic
- ▶ computationally extensive

Task: Estimating $\eta(x)$

Surge Level

- ▶ focus on extremes
- ▶ r-year return level y_r

Task: Estimating y_r

Requires proper propagation of estimation uncertainties to obtain a sensible statistical inference for y_r

Estimating $\eta(\mathbf{x})$

- ▶ **Goal:** Build a statistical emulator based on (limited) compute model runs $\{\mathbf{x}_i, y_i = \eta(\mathbf{x}_i)\}_{i=1}^N$ to infer $\eta(\mathbf{x}), \mathbf{x} \in \mathcal{X}$, the surge response function, especially for large surge values
- ▶ **Strategy: assume** $\eta(\mathbf{x})$ is a realization of a stochastic process, typically a **Gaussian Process (GP)**, that interpolates $\{\mathbf{x}_i, y_i = \eta(\mathbf{x}_i)\}_{i=1}^N$.

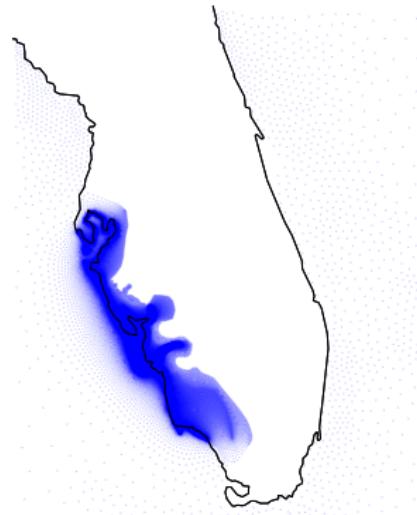
Next, I will present a quick (and incomplete) case study

Estimating $\eta(\mathbf{x})$

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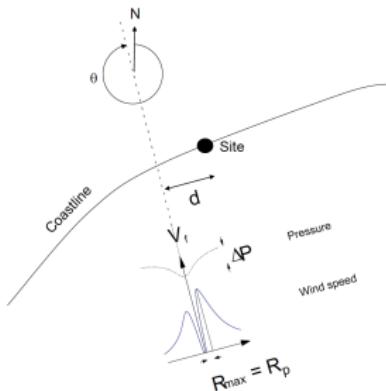
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Southwest Florida storm surge case study



- ▶ 148,055 nodes ($\sim 120,000$ in/near study region)
- ▶ Peak surge of 3,156 storms (200 input configurations)

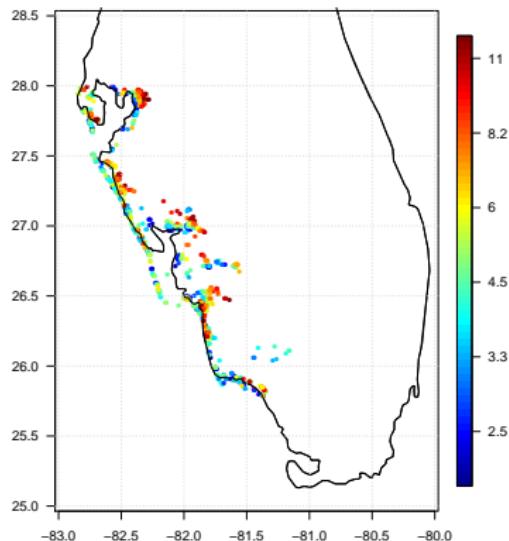
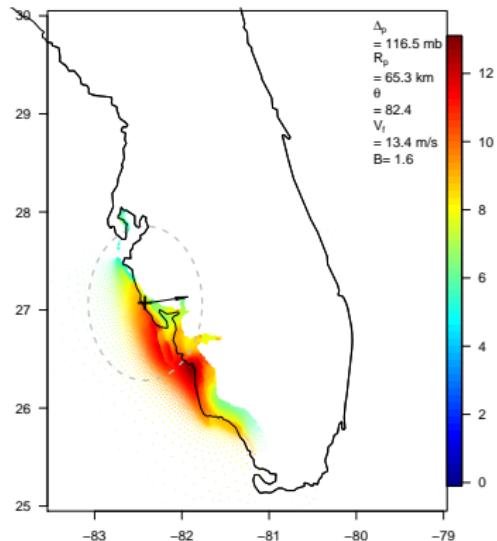
Model input



```
> summary(input_par[, 3:9])
```

dp.mb.coast.	rp.nmi.offshore.	Vf.m.s.	theta.deg.	B
Min. : 13.71	Min. : 5.985	Min. : 1.049	Min. : 5.125	Min. : 0.515
1st Qu.: 41.70	1st Qu.:14.589	1st Qu.: 4.490	1st Qu.: 35.208	1st Qu.:0.880
Median : 67.93	Median :30.190	Median : 8.521	Median : 69.846	Median :1.270
Mean : 69.15	Mean :34.759	Mean : 8.419	Mean : 64.430	Mean :1.256
3rd Qu.: 98.00	3rd Qu.:54.136	3rd Qu.:12.325	3rd Qu.: 92.700	3rd Qu.:1.613
Max. :122.71	Max. :80.362	Max. :14.970	Max. :119.930	Max. :1.984
X_Land.deg.	Y_Land.deg.			
Min. :-83.87	Min. :25.00			
1st Qu.:-82.76	1st Qu.:26.17			
Median :-82.43	Median :27.08			
Mean :-82.31	Mean :27.25			
3rd Qu.:-81.83	3rd Qu.:28.15			
Max. :-81.06	Max. :30.00			

Surge response



Goal: to emulate the **storm-wise maximum surge** (Note: one could also emulate the spatial location where the storm-wise maximum will occur)

Emulation setup

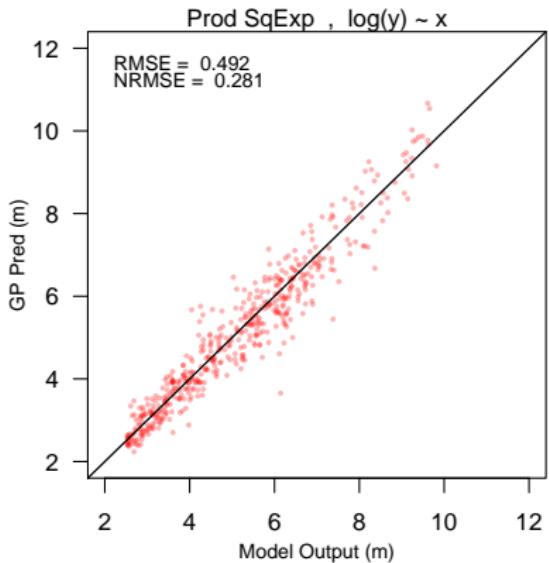
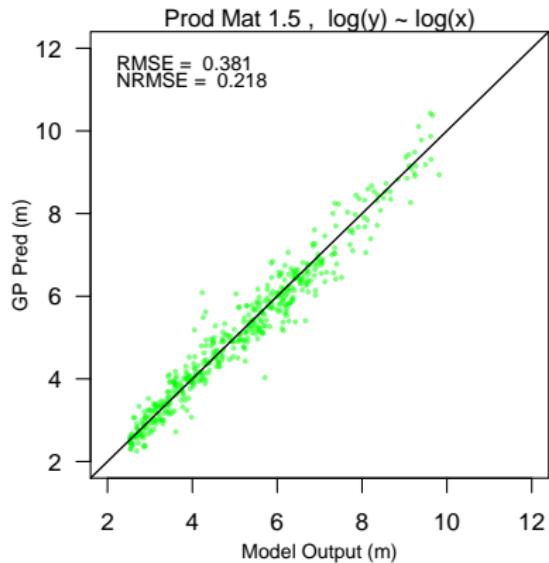
- ▶ Constant mean, (product) exponential (Exp), Matérn $\nu = 1.5$ (Mat32), Matérn $\nu = 2.5$ (Mat52), or squared-exponential (SqExp) covariance functions. Include (and estimate) nugget effect.
- ▶ Explore the use of logarithm transform:
 $(y \sim x)$, $(\log(y) \sim x)$, $(y \sim \log(x))$, $(\log(y) \sim \log(x))$
- ▶ Use normalized root mean squared prediction error (NRMSPE) to assess out-of-sample prediction performance:

$$\text{NRMSPE} = \frac{\text{RMSPE}}{\text{RMSPE}_0},$$

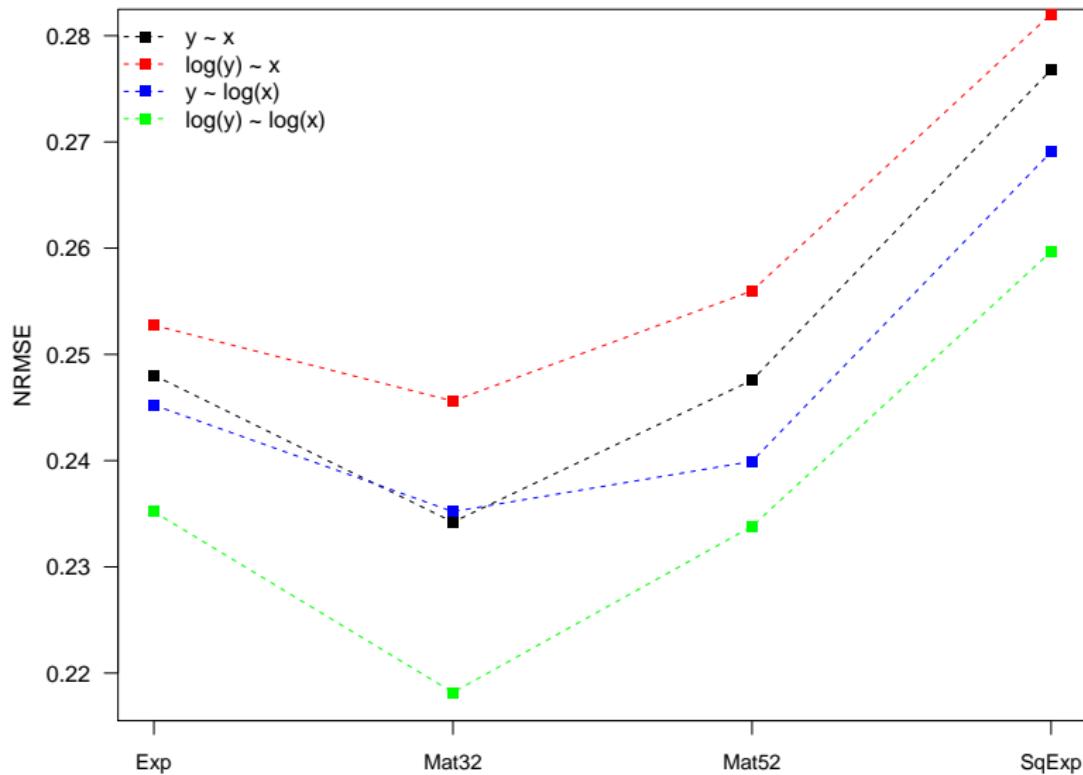
where $\text{RMSPE}_0 = \sqrt{\frac{1}{N_{test}} \sum_{i=1}^N (\bar{y} - y^{(i)})^2}$

Out-of-sample prediction

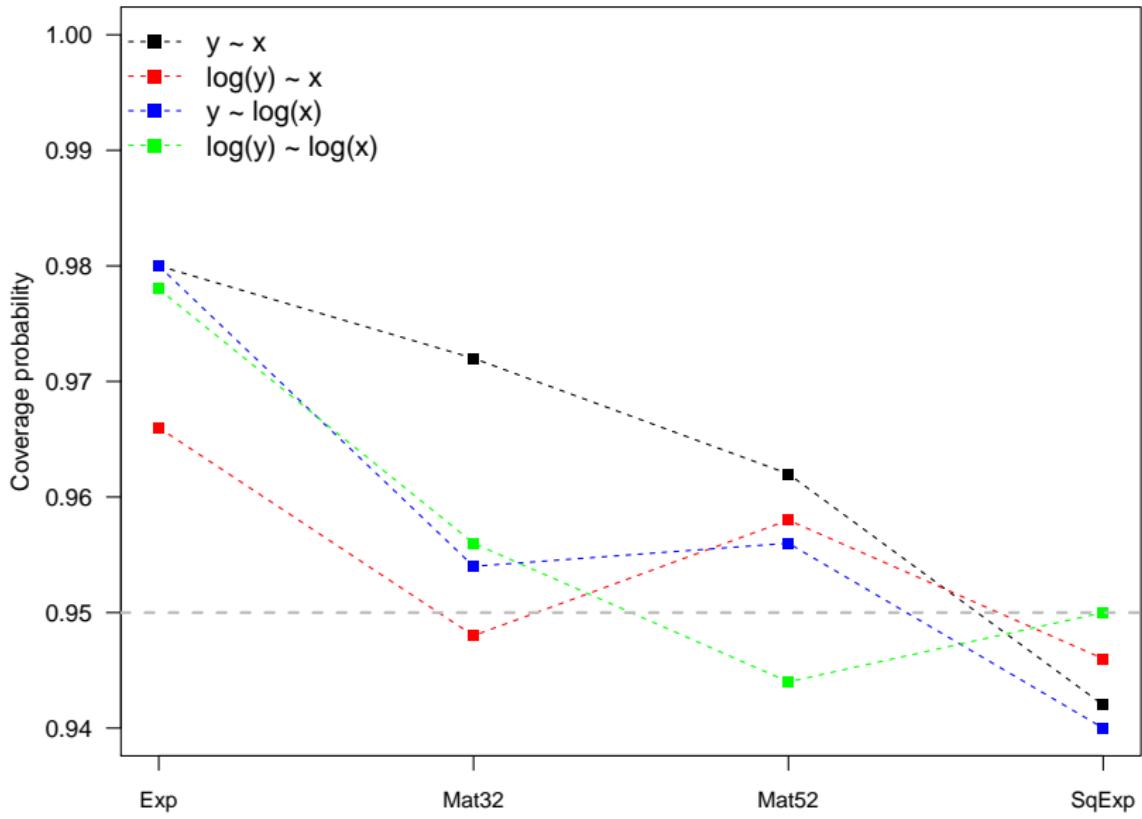
- ▶ Focus on $2m \leq y \leq 12m$
- ▶ $N = 1458, N_{test} = 500$



Normalized Root Mean Squared Prediction Error (NRMSE)



Empirical coverage probabilities



Summary and discussion

- ▶ Combining Physical and Statistical modeling in the context of storm surges risk modeling
- ▶ Emulating storm-wise maximum
 - ▶ Nugget
 - ▶ Covariance function matters, taking logs of both sides help
- ▶ Things not Addressed
 - ▶ Estimating $f(\mathbf{x})$, the joint distribution of input (i.e., TC characterise)
 - ▶ Make use of Dimensional Analysis to build a better emulator; emulating the whole surge field; nonstationarity; non-GP emulator
 - ▶ Other sources of uncertainty: e.g. wind field parameterization.

Our storm surge working group would not have been possible without the support from SAMSI. In particular the following programs:

- ▶ Model Uncertainty: Mathematical and Statistical (MUMS) 2018-2019
- ▶ Mathematical and Statistical Methods for Climate and the Earth System (CLIM) 2017-2018
- ▶ Development, Assessment and Utilization of Complex Computer Models 2006-2007

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Backup Slides

Input Modeling: Estimating $f(\mathbf{x})$ and $\lambda(s)$

Main effort: Utilizing all sources of information to better estimate TC characteristics and its estimation uncertainty

- ▶ **Data fusion:** Combining historical storms and synthetic storms (high resolution GCM, even higher resolution RCM, Kerry Emanuel's simulation) to better estimate $f(\mathbf{x})$ and $\lambda(s)$
- ▶ **Borrow information across space:** Exploit and explicitly model the spatial pattern of $\{f_s(\mathbf{x})\}_{s \in S}$ (e.g., Regional Frequency Analysis, Model-based Geostatistics).
- ▶ **Estimation Uncertainty:** Using **posterior predictive distribution**: $[\mathbf{X}_{new} | \mathbf{X}_{obs}] = \int_{\Theta} [\mathbf{X}_{new} | \theta][\theta | \mathbf{X}_{obs}] d\theta$ instead of the plug-in estimate $f_{\hat{\theta}}(\mathbf{x}) ([\mathbf{X}_{new} | \hat{\theta}])$

Estimating y_r

- ▶ Should be relatively straightforward given that one can estimate $f(\mathbf{x})$, $\lambda(s)$, and $\eta(\mathbf{x})$ reasonably well and properly account for their estimation uncertainties
- ▶ Still worthwhile to exploit extreme value theory-based methods for estimating return levels with longer return periods e.g. NRC probabilistic risk assessment
- ▶ It would be of interest to compare the estimates of y_r based on EVA at locations with long/reliable enough observations to assess the “gain” by using the JPM-type of approach