STAT 8020 R Lab 2: Simple Linear Regression II

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Contents

Maximum Heart Rate vs. Age

Load the data

```
dat <- read.csv('http://whitneyhuang83.github.io/STAT8010/Data/maxHeartRate.csv', header = T)
head(dat)</pre>
```

```
## Age MaxHeartRate
## 1 18 202
## 2 23 186
## 3 25 187
## 4 35 180
## 5 65 156
## 6 54 169
```

attach(dat)

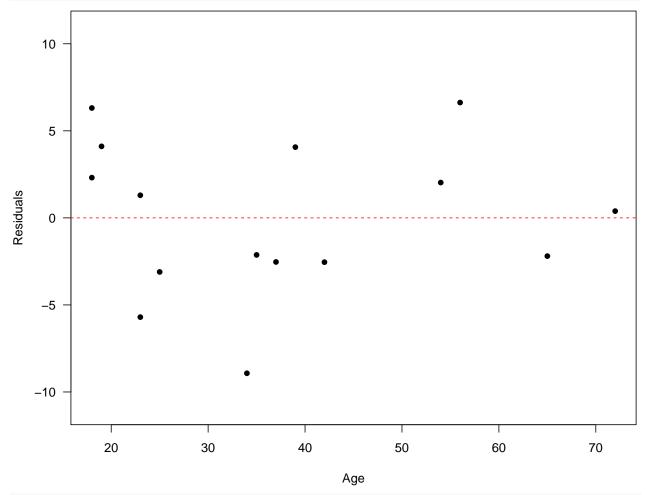
Fitting a simple linear regression

```
fit <- lm(MaxHeartRate ~ Age)
summary(fit)</pre>
```

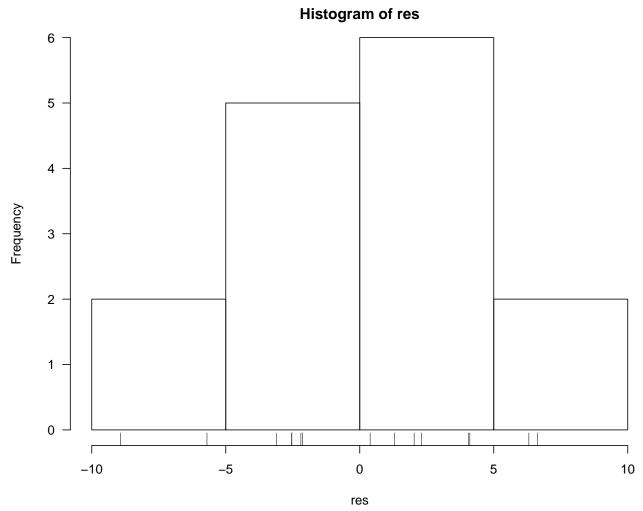
```
##
## Call:
## lm(formula = MaxHeartRate ~ Age)
##
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -8.9258 -2.5383 0.3879 3.1867 6.6242
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
                                     73.27 < 2e-16 ***
## (Intercept) 210.04846
                           2.86694
                           0.06996 -11.40 3.85e-08 ***
## Age
               -0.79773
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 4.578 on 13 degrees of freedom
## Multiple R-squared: 0.9091, Adjusted R-squared: 0.9021
## F-statistic: 130 on 1 and 13 DF, p-value: 3.848e-08
```

Residual Analysis

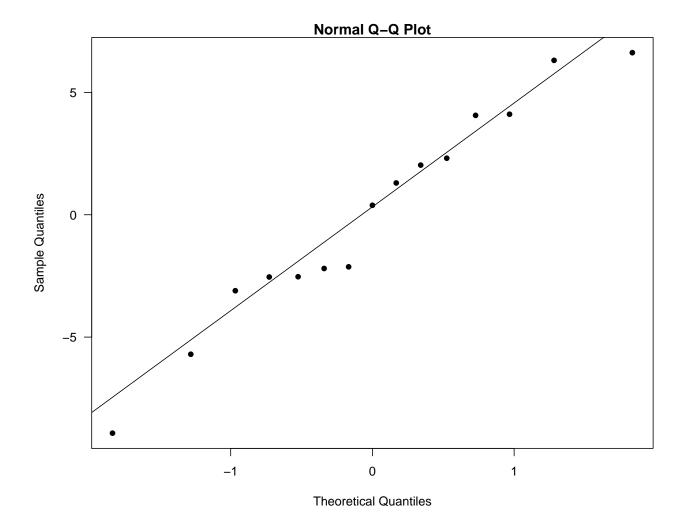
```
par(las = 1, mar = c(4.1, 4.1, 1.1, 1.1))
plot(Age, fit$residuals, pch = 16, ylab = "Residuals", ylim = c(-11, 11))
abline(h = 0, col = "red", lty = 2)
```



```
res <- fit$residuals
# histogram
hist(res, las = 1)
rug(res)</pre>
```



```
# QQ plot
qqnorm(res, pch = 16, las = 1)
qqline(res)
```



Confidence Interval

```
\beta_1
beta1_hat <- summary(fit)[["coefficients"]][, 1][2]</pre>
se_beta1 <- summary(fit)[["coefficients"]][, 2][2]</pre>
alpha = 0.05
CI_beta1 \leftarrow c(beta1_hat - qt(1 - alpha / 2, 13) * se_beta1,
               beta1_hat + qt(1 - alpha / 2, 13) * se_beta1)
CI_beta1
##
          Age
## -0.9488720 -0.6465811
confint(fit)
##
                     2.5 %
                                 97.5 %
## (Intercept) 203.854813 216.2421034
## Age
                 -0.948872 -0.6465811
Y_h|X_h = 40
```

```
Age_new = data.frame(Age = 40)
hat_Y <- fit$coefficients[1] + fit$coefficients[2] * 40
hat_Y
## (Intercept)
      178.1394
predict(fit, Age_new, interval = "confidence")
          fit
                    lwr
                              upr
## 1 178.1394 175.5543 180.7245
predict(fit, Age_new, interval = "predict")
          fit
                    lwr
## 1 178.1394 167.9174 188.3614
Check
sd <- sqrt((sum(fit$residuals^2) / 13))</pre>
ME <- qt(1 - alpha / 2, 13) * sd * sqrt(1 + 1 / 15 + (40 - mean(Age))^(2) / sum((Age - mean(Age))^2))
c(hat_Y - ME, hat_Y + ME)
## (Intercept) (Intercept)
      167.9174
                   188.3614
##
Hypothesis Tests for \beta_1
H_0: \beta_1 = -1 \text{ vs. } H_a: \beta_1 \neq -1 \text{ with } \alpha = 0.05
beta1 null <- -1
t_star <- (beta1_hat - beta1_null) / se_beta1</pre>
p_value <- 2 * pt(t_star, 13, lower.tail = F)</pre>
p_value
           Age
## 0.01262031
par(las = 1)
x_{grid} \leftarrow seq(-3.75, 3.75, 0.01)
y_grid <- dt(x_grid, 13)</pre>
plot(x_grid, y_grid, type = "l", xlab = "Test statistic", ylab = "Density", xlim = c(-3.75, 3.75))
polygon(c(x grid[x grid < -t star], rev(x grid[x grid < -t star])),</pre>
        c(y_grid[x_grid < -t_star], rep(0, length(y_grid[x_grid < -t_star]))), col = "skyblue")</pre>
polygon(c(x_grid[x_grid > t_star], rev(x_grid[x_grid > t_star])),
        c(y_grid[x_grid > t_star], rep(0, length(y_grid[x_grid > t_star]))), col = "skyblue")
abline(v = t_star, lty = 2)
abline(v = -t_star, lty = 2)
abline(h = 0)
```

