DSA 8020 R Session 4: Multiple Linear Regression III

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      library(faraway)
      data(gala)

      galaNew <- gala[, -2]</td>
```

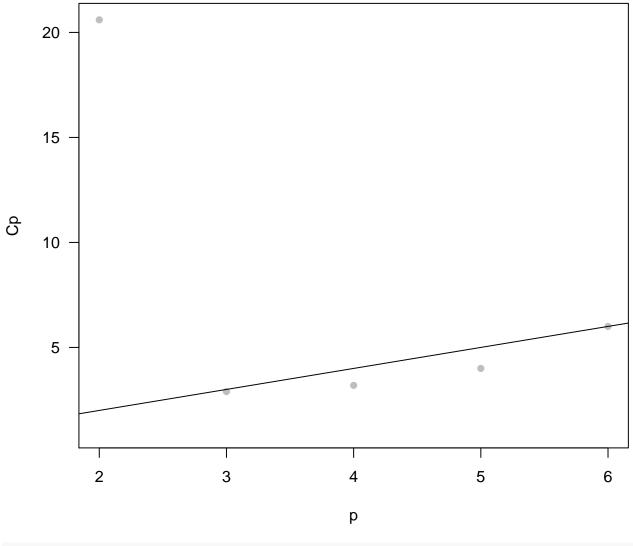
Model Selection

Best Subset Selection

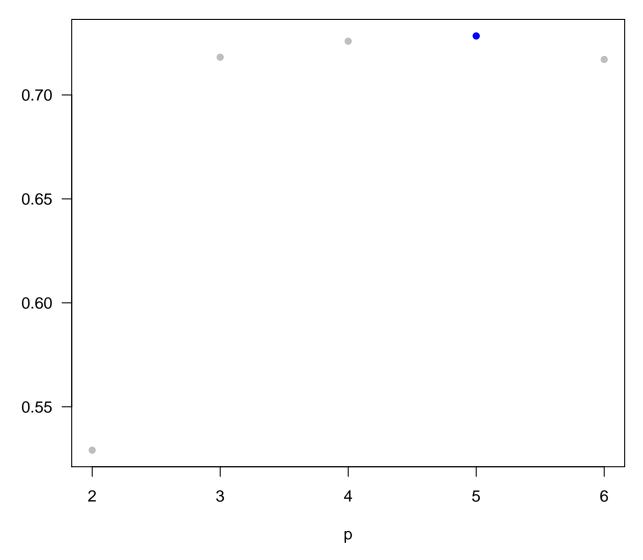
```
#install.packages(c("tidyverse", "caret", "leaps"))
library(tidyverse)
library(caret)
library(leaps)
models <- regsubsets(Species ~ ., data = galaNew)
summary(models)

## Subset selection object
## Call: regsubsets.formula(Species ~ ., data = galaNew)
## 5 Variables (and intercept)</pre>
```

```
Forced in Forced out
              FALSE
                       FALSE
## Area
## Elevation
                FALSE
                         FALSE
## Nearest
                FALSE
                         FALSE
## Scruz
                FALSE
                          FALSE
## Adjacent
                FALSE
                          FALSE
## 1 subsets of each size up to 5
## Selection Algorithm: exhaustive
           Area Elevation Nearest Scruz Adjacent
## 1 ( 1 ) " " "*"
                         11 11
                                 11 11
                                       "*"
                          11 11
                                  11 11
## 2 (1)"" "*"
## 3 (1)"" "*"
                        11 11
                                  "*"
                                       "*"
## 4 ( 1 ) "*" "*"
                          11 11
                                  "*"
                                       "*"
                          "*"
## 5 (1) "*" "*"
                                 "*"
                                       "*"
res.sum <- summary(models)</pre>
criteria <- data.frame(</pre>
 Adj.R2 = res.sum$adjr2,
 Cp = res.sum$cp,
 BIC = res.sum$bic)
criteria
       Adj.R2
                     Ср
                              BIC
## 1 0.5291255 20.599003 -16.84525
## 2 0.7181425 2.897184 -29.93078
## 3 0.7258462 3.193068 -28.49317
## 4 0.7283816 4.000075 -26.54733
## 5 0.7170651 6.000000 -23.14622
plot(2:6, criteria$Cp, las = 1, xlab = "p", ylab = "Cp",
    pch = 16, col = "gray", ylim = c(1, max(criteria$Cp)))
abline(0, 1)
```

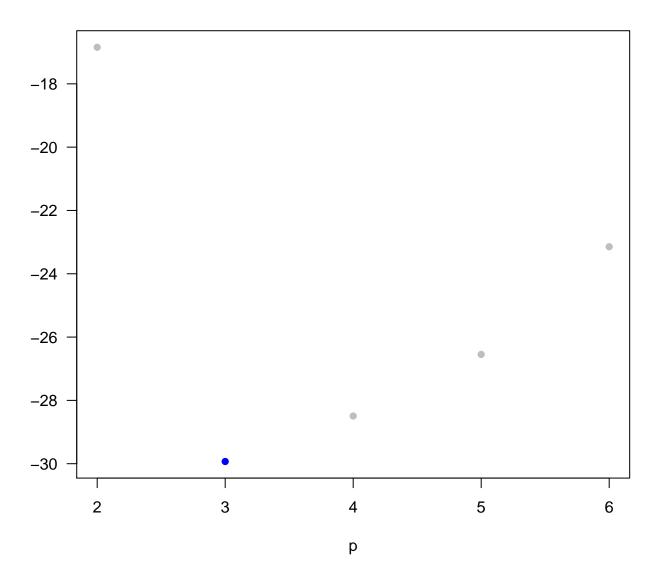






plot(2:6, criteria\$BIC, las = 1, xlab = "p", ylab = "", pch = 16, col = "gray", main = "BIC")
points(3, criteria\$BIC[2], col = "blue", pch = 16)

BIC



Backward Selection

- Elevation 1

```
full <- lm(Species ~ ., data = galaNew)</pre>
step(full, direction = "backward")
## Start: AIC=251.93
## Species ~ Area + Elevation + Nearest + Scruz + Adjacent
##
##
               Df Sum of Sq
                               RSS
                                       AIC
                             89232 249.93
## - Nearest
                1
## - Area
                       4238
                             93469 251.33
                1
## - Scruz
                       4636
                             93867 251.45
## <none>
                             89231 251.93
## - Adjacent
                1
                      66406 155638 266.62
```

131767 220998 277.14

```
##
## Step: AIC=249.93
## Species ~ Area + Elevation + Scruz + Adjacent
##
##
              Df Sum of Sq
                               RSS
## - Area
                      4436 93667 249.39
                1
## <none>
                             89232 249.93
                      7544 96776 250.37
## - Scruz
                1
## - Adjacent
                1
                      72312 161544 265.74
## - Elevation 1
                     139445 228677 276.17
## Step: AIC=249.39
## Species ~ Elevation + Scruz + Adjacent
##
##
              Df Sum of Sq
                               RSS
## - Scruz
                1
                       6336 100003 249.35
## <none>
                             93667 249.39
## - Adjacent
                1
                      69860 163527 264.11
## - Elevation 1
                     275784 369451 288.56
## Step: AIC=249.35
## Species ~ Elevation + Adjacent
##
              Df Sum of Sq
##
                               RSS
                                      AIC
## <none>
                            100003 249.35
## - Adjacent
                1
                     73251 173254 263.84
## - Elevation 1
                     280817 380820 287.47
##
## Call:
## lm(formula = Species ~ Elevation + Adjacent, data = galaNew)
## Coefficients:
## (Intercept)
                  Elevation
                                Adjacent
##
      1.43287
                    0.27657
                                -0.06889
```

Stepwise Selection

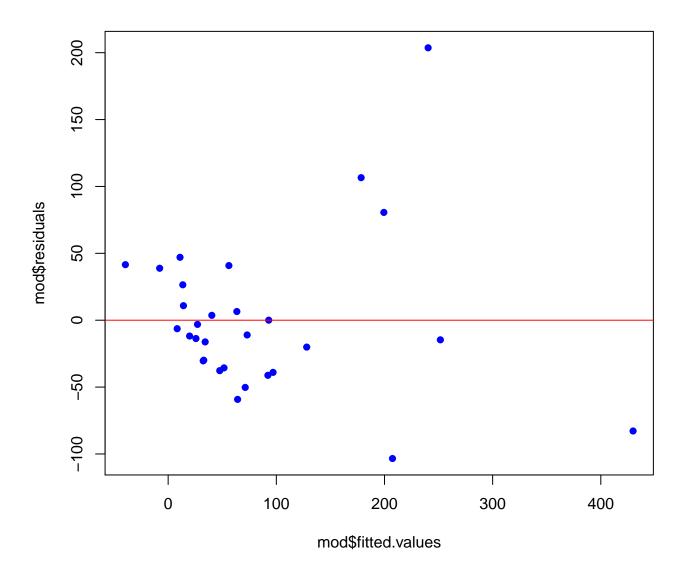
```
step(full, direction = "both")
## Start: AIC=251.93
## Species ~ Area + Elevation + Nearest + Scruz + Adjacent
##
                              RSS
##
              Df Sum of Sq
                                     AIC
## - Nearest
               1
                             89232 249.93
## - Area
                       4238 93469 251.33
                1
## - Scruz
                1
                       4636 93867 251.45
                             89231 251.93
## <none>
## - Adjacent
                1
                     66406 155638 266.62
## - Elevation 1
                    131767 220998 277.14
## Step: AIC=249.93
```

```
## Species ~ Area + Elevation + Scruz + Adjacent
##
##
              Df Sum of Sq
                               RSS
                            93667 249.39
## - Area
               1
                      4436
## <none>
                             89232 249.93
## - Scruz
                      7544 96776 250.37
               1
## + Nearest
                          0 89231 251.93
               1
## - Adjacent
                1
                     72312 161544 265.74
                     139445 228677 276.17
## - Elevation 1
##
## Step: AIC=249.39
## Species ~ Elevation + Scruz + Adjacent
              Df Sum of Sq
##
                               RSS
                                      AIC
## - Scruz
                       6336 100003 249.35
               1
## <none>
                             93667 249.39
## + Area
                       4436 89232 249.93
                1
## + Nearest
               1
                       198 93469 251.33
## - Adjacent
                     69860 163527 264.11
                1
## - Elevation 1
                     275784 369451 288.56
##
## Step: AIC=249.35
## Species ~ Elevation + Adjacent
##
##
              Df Sum of Sq
                               RSS
                                      AIC
## <none>
                            100003 249.35
## + Scruz
                       6336 93667 249.39
               1
                       3227 96776 250.37
## + Area
               1
## + Nearest
                      1550 98453 250.88
               1
## - Adjacent 1
                     73251 173254 263.84
                     280817 380820 287.47
## - Elevation 1
##
## Call:
## lm(formula = Species ~ Elevation + Adjacent, data = galaNew)
##
## Coefficients:
## (Intercept)
                  Elevation
                                Adjacent
                                -0.06889
##
       1.43287
                    0.27657
```

Model Diagnostics

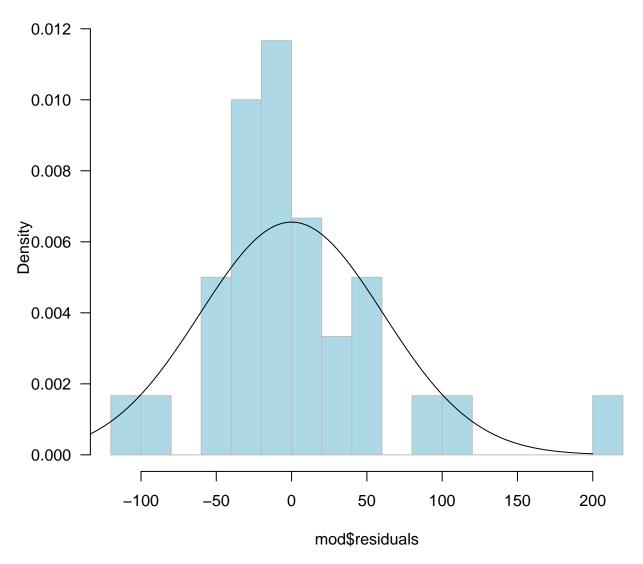
Residual Plot

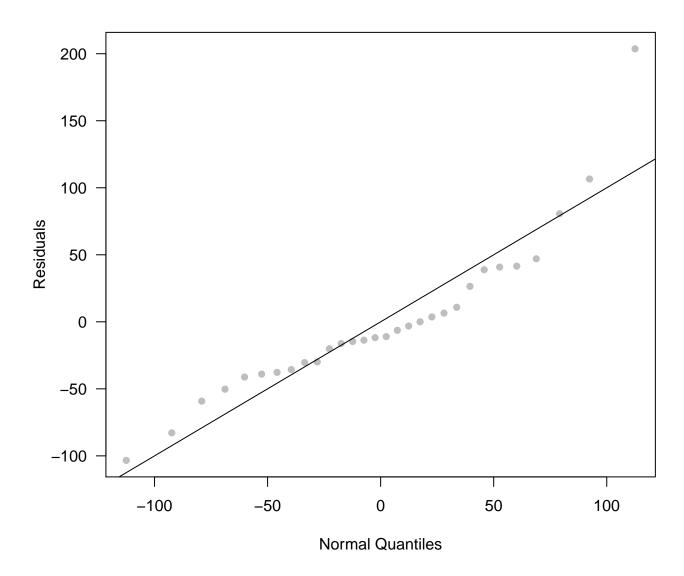
```
mod <- lm(Species ~ Elevation + Adjacent, data = galaNew)
plot(mod$fitted.values, mod$residuals, pch = 16, col = "blue")
abline(h = 0, col = "red")</pre>
```



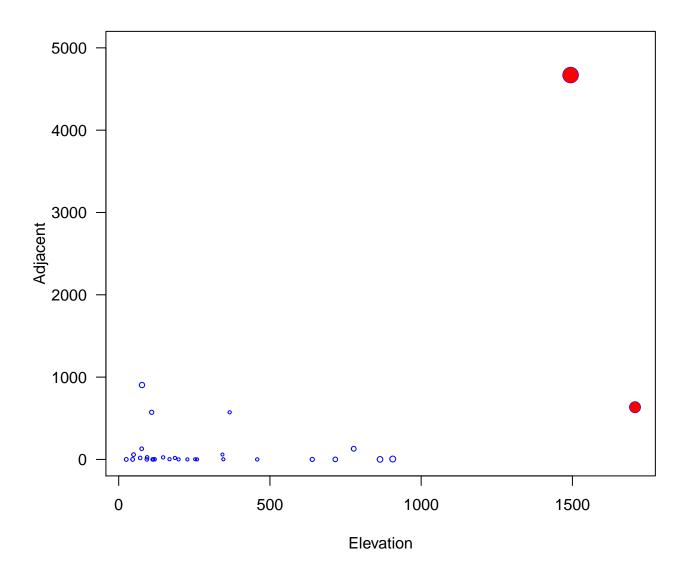
${\bf Residual\ Histogram/QQplot}$

Histogram of mod\$residuals



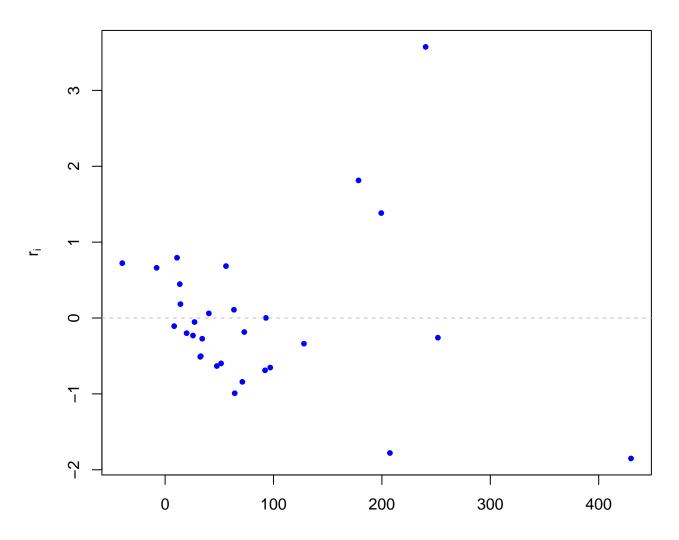


Leverage



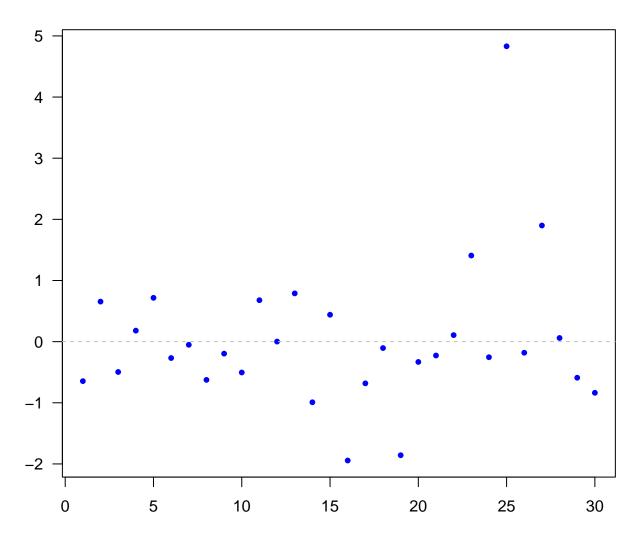
${\bf Studentized\ Residuals}$

Studentized Residuals



Jackknife Residuals

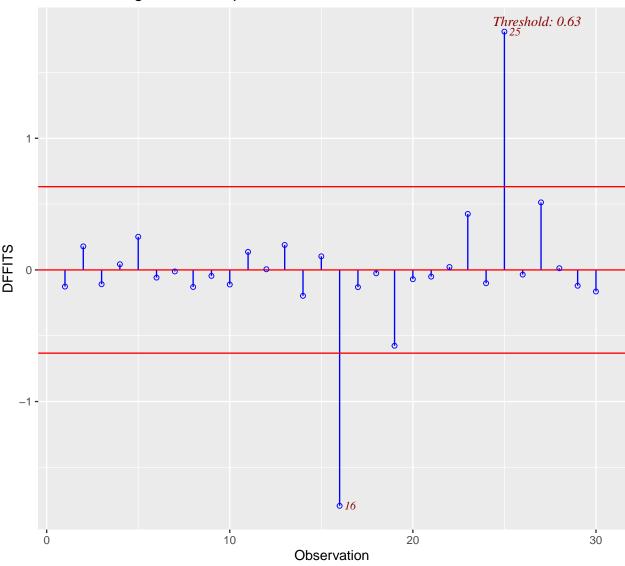
Jacknife Residuals



Identifying Influential Observations: DFFITS

```
library(olsrr)
ols_plot_dffits(step_gala)
```

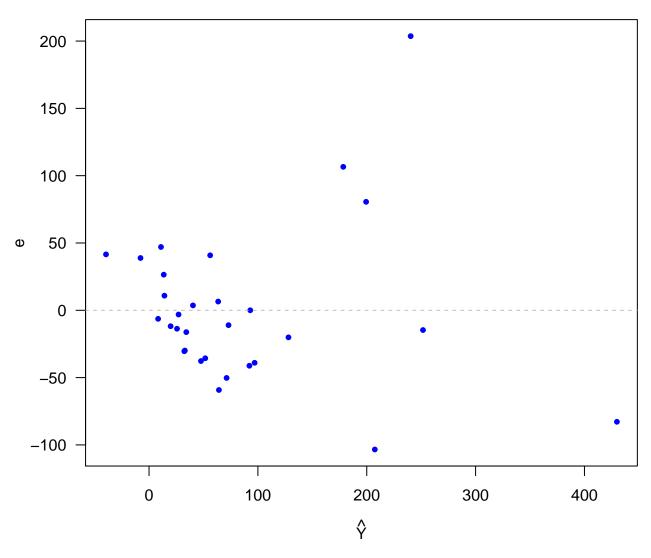
Influence Diagnostics for Species



Transformation

```
par(las = 1)
plot(step_gala$fitted.values, step_gala$residuals,
    pch = 16, cex = 0.8, col = "blue", main =" Residuals ",
    xlab = expression(hat(Y)), ylab = expression(e))
abline(h = 0, lty = 2, col = "gray")
```

Residuals



```
sqrt_fit <- lm(sqrt(Species) ~ Elevation + Adjacent)

par(las = 1)
plot(sqrt_fit$fitted.values, sqrt_fit$residuals,
     pch = 16, cex = 0.8, col = "blue", main =" Residuals ",
     xlab = expression(hat(Y)), ylab = expression(e))
abline(h = 0, lty = 2, col = "gray")</pre>
```

Residuals

