DSA 8020 R Session 7: Logistic Regression and Poisson Regression

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Logistic Regression: Horseshoe Crab Malting

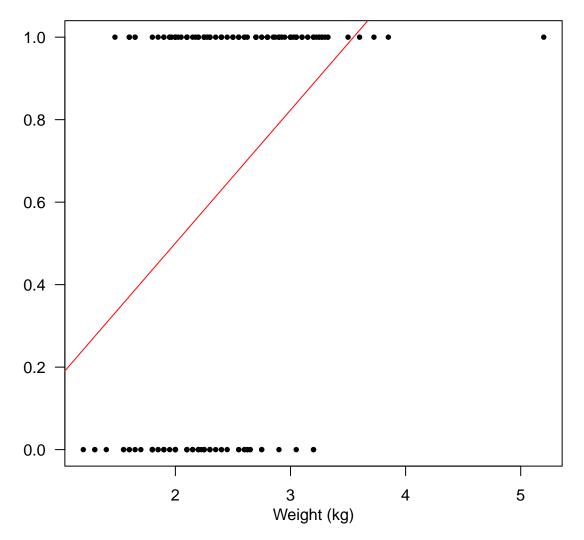
 $Data\ Source:$ Brockmann, H. J. (1996). Satellite male groups in horseshoe crabs, Limulus polyphemus. $Ethology,\ 102(1),\ 1\text{-}21.$

Load the data

```
crab <- read.table("http://users.stat.ufl.edu/~aa/cda/data/Crabs.dat", header = T)</pre>
```

Fit a Linear Regression

Let's fit a simple linear regression using weight as the predictor

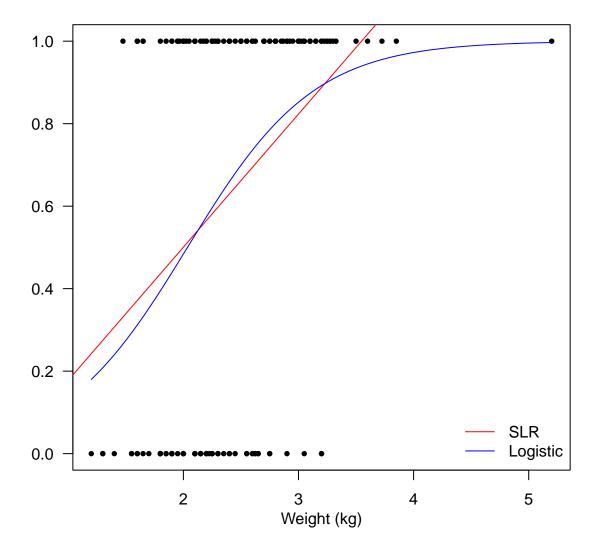


Fit a Logistic Regression

```
logitFit <- glm(y ~ weight, data = crab, family = "binomial")
summary(logitFit)

##
## Call:
## glm(formula = y ~ weight, family = "binomial", data = crab)
##
## Deviance Residuals:
## Min 1Q Median 3Q Max</pre>
```

```
## -2.1108 -1.0749 0.5426 0.9122
                                       1.6285
##
## Coefficients:
              Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) -3.6947
                           0.8802 -4.198 2.70e-05 ***
## weight
               1.8151
                            0.3767 4.819 1.45e-06 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 225.76 on 172 degrees of freedom
## Residual deviance: 195.74 on 171 degrees of freedom
## AIC: 199.74
##
## Number of Fisher Scoring iterations: 4
# Plot the fits
rg <- range(crab$weight)</pre>
xg \leftarrow seq(rg[1], rg[2], 0.01)
pred <- predict(logitFit, newdata = data.frame(weight = xg), type = "response")</pre>
par(mar = c(3.5, 3.5, 0.8, 0.6))
plot(crab$weight, crab$y, pch = 16, cex = 0.75, las = 1, xlab = "", ylab = "")
mtext("Weight (kg)", side = 1, line = 2)
abline(lmFit, col = "red")
lines(xg, pred, col = "blue")
legend("bottomright", legend = c("SLR", "Logistic"),
      col = c("red", "blue"), lty = 1, bty = "n")
```



Confidence Intervals

```
# Normal approximation
est <- summary(logitFit)$coefficients
(CI_norm <- est[2, 1] + c(-1, 1) * qnorm(0.975) * est[2, 2])

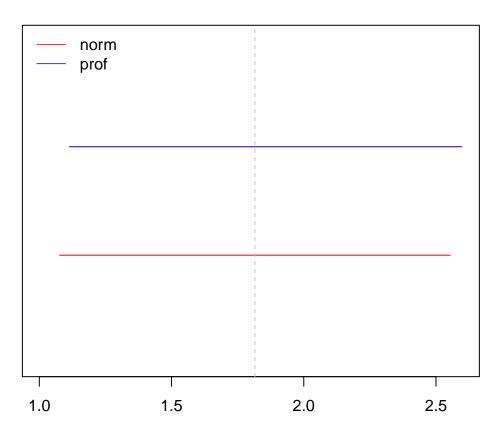
## [1] 1.076834 2.553455

# Profile likelihood CI
library(MASS)
(CI_prof <- confint(logitFit)[2,])

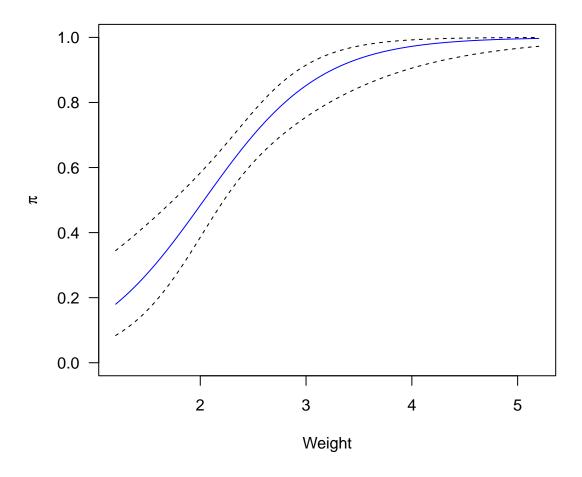
## Waiting for profiling to be done...

## 2.5 % 97.5 %
## 1.113790 2.597305</pre>
```

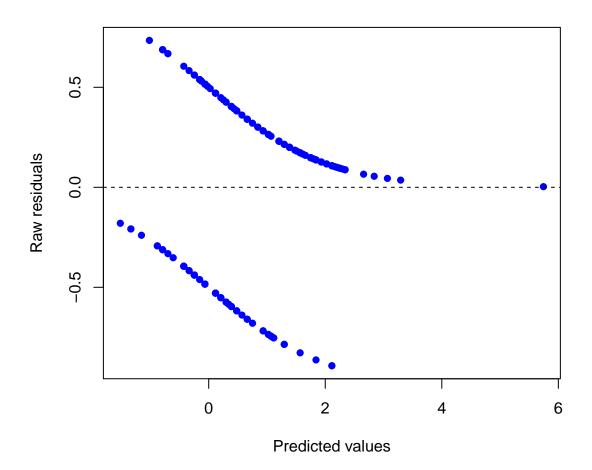




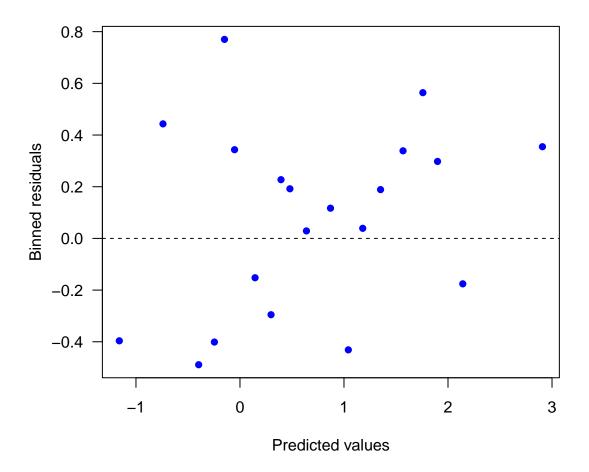
Prediction



Raw Residual plot



Binned Residuals



Model selection

```
logitFit2 <- glm(y ~ weight + width, data = crab, family = "binomial")</pre>
summary(logitFit2)
##
## Call:
## glm(formula = y ~ weight + width, family = "binomial", data = crab)
##
## Deviance Residuals:
##
       Min
                 1Q
                      Median
                                    3Q
                                            Max
## -2.1127 -1.0344
                      0.5304
                               0.9006
                                         1.7207
##
## Coefficients:
               Estimate Std. Error z value Pr(>|z|)
##
              -9.3547
                            3.5280
                                    -2.652 0.00801 **
## (Intercept)
## weight
                 0.8338
                            0.6716
                                      1.241
                                            0.21445
## width
                 0.3068
                            0.1819
                                      1.686
                                            0.09177 .
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 225.76 on 172 degrees of freedom
##
```

```
## Residual deviance: 192.89 on 170 degrees of freedom
## AIC: 198.89
##
## Number of Fisher Scoring iterations: 4
step(logitFit2)
## Start: AIC=198.89
## y ~ weight + width
##
##
           Df Deviance
                          AIC
## - weight 1
                194.45 198.45
## <none>
                 192.89 198.89
## - width 1
                195.74 199.74
##
## Step: AIC=198.45
## y ~ width
##
##
          Df Deviance
                         AIC
               194.45 198.45
## <none>
## - width 1 225.76 227.76
## Call: glm(formula = y ~ width, family = "binomial", data = crab)
##
## Coefficients:
## (Intercept)
                     width
##
      -12.3508
                     0.4972
##
## Degrees of Freedom: 172 Total (i.e. Null); 171 Residual
## Null Deviance:
                       225.8
## Residual Deviance: 194.5
                               AIC: 198.5
```

Poisson Regression

Flying-Bomb Hits on London During World War II [Clarke, 1946; Feller, 1950]

7.1

1.6

```
count <- c(229, 211, 93, 35, 7, 1)
grids <- 576
hits <- 537
lambda <- hits / grids
count_expected <- c(grids * dpois(0:4, lambda = lambda), grids * ppois(4, lambda = lambda, lower.tail = round(count_expected, 1)</pre>
```

US Landfalling Hurriances

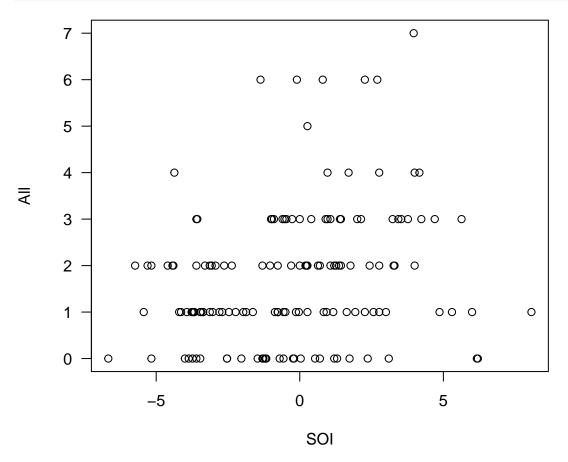
[1] 226.7 211.4 98.5 30.6

```
# load the hurriance count
con = "http://myweb.fsu.edu/jelsner/Book/Chap07/US.txt"
hurricanes = read.table(con, header = T)
head(hurricanes)
     Year All MUS G FL E
##
## 1 1851
             1
                 1 0
                      1 0
## 2 1852
             3
                 1 1
                      2 0
## 3 1853
             0
                      0 0
## 4 1854
## 5 1855
                      0 0
                 1 1
             1
## 6 1856
                     1 0
                 1 1
par(las = 1, mar = c(4.6, 3.9, 0.8, 0.6))
layout(matrix(c(1, 2), 1, 2, byrow = TRUE), widths = c(0.57, 0.43))
plot(hurricanes$Year, hurricanes$All, type = "h", xlab = "Year", ylab = "Hurricane count")
barplot(table(hurricanes$All), xlab = "Hurricane Count", ylab = "Number of years", main = "")
       7
                                                       40
       6
       5
                                                       30
                                                  Number of years
Hurricane count
       4
       3
                                                       20
       2
                                                       10
       1
                                                        0
          1850
                    1900
                               1950
                                         2000
                                                              0
                                                                    2
                                                                          4
                                                                               6
```

Hurricane Count

Year

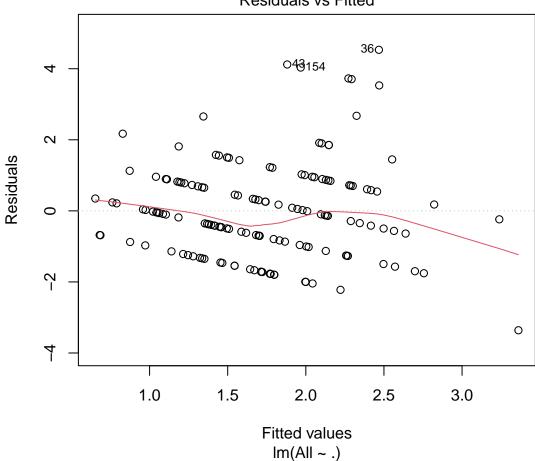
Load the environmetal variables



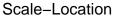
```
\label{lines} lines(c(fivenum(annual\$soi[H\$All == i])[4], fivenum(annual\$soi[H\$All == i])[5]), \ c(i, i))
}
plot(range(annual$nao, na.rm = TRUE), c(0, 7), type = "n", ylab = "Hurricane count", xlab = "NAO",
     las = 1)
for(i in 0:7){
  points(fivenum(annual$nao[H$All == i])[3], i, pch=19)
  lines(c(fivenum(annual$nao[H$All == i])[1], fivenum(annual$nao[H$All == i])[2]), c(i, i))
  lines(c(fivenum(annual$nao[H$All == i])[4], fivenum(annual$nao[H$All == i])[5]), c(i, i))
plot(range(annual$ssn, na.rm = TRUE), c(0, 7), type = "n", ylab = "Hurricane count",
     xlab = "Sunspot number", las = 1)
for(i in 0:7){
  points(fivenum(annual$ssn[H$All == i])[3], i, pch = 19)
  lines(c(fivenum(annual$ssn[H$All == i])[1], fivenum(annual$ssn[H$All == i])[2]), c(i, i))
  lines(c(fivenum(annual$ssn[H$All == i])[4], fivenum(annual$ssn[H$All == i])[5]), c(i, i))
}
      7
      6
                                                    6
                                              Hurricane count
Hurricane count
      5
                                                    5
      4
                                                    4
      3
                                                    3
      2
                                                    2
      1
                                                    1
      0
                                                    0
            -0.4
                        0.0
                             0.2
                                   0.4
                                        0.6
                                                                       0
                                                                                 5
                                                           -5
                        SST
                                                                       SOI
      7
                                                    7
      6
                                                    6
                                              Hurricane count
Hurricane count
      5
                                                    5
      4
                                                    4
      3
                                                    3
      2
                                                    2
      1
                                                    1
      0
                                                    0
              -2
                          0
                                     2
                                           3
                                                        0
                                                              50
                                                                                  200
                   -1
                                                                     100
                                                                           150
                        NAO
                                                                 Sunspot number
```

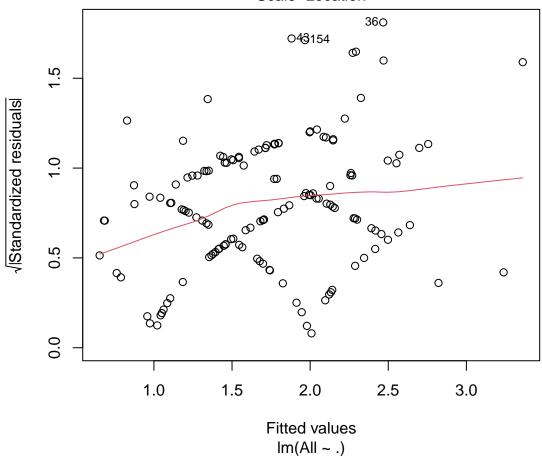
Linear Regression

Residuals vs Fitted



plot(lmFull, which = 3)





Poisson Regression

```
PoiFull <- glm(All ~ ., data = data, family = "poisson")
summary(PoiFull)</pre>
```

```
##
## Call:
  glm(formula = All ~ ., family = "poisson", data = data)
##
## Deviance Residuals:
                 1Q
                      Median
                                   3Q
                                           Max
## -2.8530 -0.8984 -0.1376
                               0.6027
                                         2.4720
##
## Coefficients:
                Estimate Std. Error z value Pr(>|z|)
## (Intercept) 0.595288
                           0.103342
                                      5.760 8.39e-09 ***
## SOI
                0.061863
                           0.021319
                                      2.902 0.00371 **
                                    -2.586 0.00972 **
## NAO
               -0.166595
                           0.064427
## SST
                0.228972
                           0.255289
                                      0.897
                                             0.36977
## SSN
               -0.002306
                           0.001372 -1.681 0.09284 .
## ---
```

```
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## (Dispersion parameter for poisson family taken to be 1)
##
       Null deviance: 197.89 on 144 degrees of freedom
## Residual deviance: 174.81 on 140 degrees of freedom
## AIC: 479.64
##
## Number of Fisher Scoring iterations: 5
plot(data$SOI, hurricanes$All[-(1:15)], cex = 0.75, col = "gray",
     xlab = "", ylab = "", las = 1)
mtext("Hurricane Count", side = 2, line = 2)
mtext("Year", side = 1, line = 2)
points(data$SOI, predict(lmFull), col = "red",
       cex = 0.5, pch = 16)
points(data$SOI, predict(PoiFull, type = "response"), col = "blue", cex = 0.5, pch = 16)
    7
    6
    5
Hurricane Count
    4 -
    3
                       0
                                         @ O @
```

2

1

0

033330

-5

0 0 000 00 00 00 0 0

0

Year

00

5