Lecture 1

Course Infromation and Overview

DSA 8070 Multivariate Analysis

Whitney Huang Clemson University



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Agenda

- Instructor Background
- 2 Class Policies
- Course Overview



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About the Instructor

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About the Instructor

- Assistant Professor of Applied Statistics and Data Science
- Born in Laramie, WY, and grew up in Taiwan





• Obtained a B.S. in Mechanical Engineering and switched to Statistics in graduate school





 Earned a Ph.D. in Statistics in 2017 from Purdue University.







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How to Reach Me?

- Email ☑: wkhuang@clemson.edu

 Please include [DSA 8070] in your email subject line
- Office: O-221 Martin Hall
- Office Hours: Wednesday 8-9 pm and by appointment



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Class Policies



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Logistics

• There will be two projects. The due dates are:

Project I: Oct. 17, ThursdayProject II: Dec. 12, Thursday

- There will be biweekly R Labs:
 - To be uploaded to Canvas by 11:59 pm ET on the due dates
 - Worst grade will be dropped
- No lectures during Thanksgiving week (Nov. 25-29)

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Course Materials at CANVAS

- Course syllabus / Announcements
- Lecture slides/notes/videos
- R Labs/Projects
- Data sets for lectures and labs



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Reference Books

- Applied Multivariate Statistics with R, Daniel Zelterman, 2015 [Link]
- Modern Multivariate Statistical Techniques: Regression, Classification, and Manifold Learning, Alan Izenman, 2008, [Link]
- $\hbox{\it Methods of Multivariate Analysis, 3_{rd} Edition, Alvin } \hbox{\it Rencher and William Christensen, 2012 [Link]}$
- Applied Multivariate Statistical Methods, 6th Edition, Richard Johnson and Dean Wichern, 2008 [Link]

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Evaluation

Grades will be weighted as follows:

R Lab	s	20%
Projec	t I	40%
Projec	t II	40%

Final course grades will be assigned using the following grading scheme:

>= 90.00	Α
$88.00\sim89.99$	A-
$85.00\sim87.99$	B+
$80.00\sim84.99$	В
$78.00\sim79.99$	B-
$75.00\sim77.99$	C+
$70.00\sim74.99$	С
$68.00\sim69.99$	C-
<= 67.99	F



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Computing

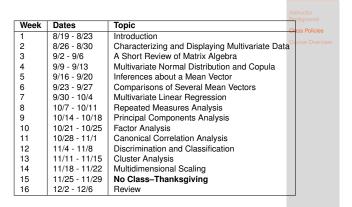
- a free/open-source programming language for statistical analysis
- available at https://www.r-project.org/(R); https://rstudio.com/(Rstudio)
- I strongly encourage you to use R Markdown for homework assignments





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Topics



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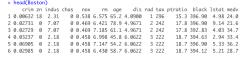
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Course Overview

Introduction

 In many observational or experimental studies, measurements are collected simultaneously on more than one variable on each unit



- Multivariate analysis is the collection of statistical methods that can be used to (jointly) analyze these multiple measurements
 - ⇒ some are extensions of familiar methods (t-test, ANOVA, Linear Regression, ...) while others are unique to multivariate analysis (PCA, CCA, Factor Analysis, ...)
- The idea is to exploit potential "correlations" among the multiple measurements to improve inference



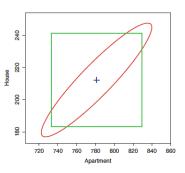
Importance of Multivariate Analysis

- If all the variables are independent, one can't do better than analyze each variable's behavior by using histograms or box plots, looking at the means, medians, variances and other 'one dimensional statistics'
- However if some of the variables are acting together, either that they are positively correlated or that they inhibit each other, one will miss a lot of important information by slicing the data up into those column vectors and studying them separately
- Thus important connections between variables are only available to us if we consider the data as a whole.

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Using Multivariate Methods Could Lead to Sharper Inference



Source: Fig. 1.1 of Applied Multivariate Statistics with R by Zelterman



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Dimensionality Reduction or Structural Simplification

 Goal: to reduce the "dimensionality" by considering a small number of (linear) combinations of a large number of measurements without losing important information

• Examples:

- A single index of patient reaction to radiotherapy can be constructed from measurements on several response variables
- Wildlife ecologists can construct a few indices of habitat preference from measurements of dozens of features of nesting sites selected by a certain bird species

Techniques:

- Principal Component Analysis (Week 9)
- Factor Analysis (Week 10)
- Multidimensional Scaling (Week 14)



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Grouping or Classification

 Goal: to identify groups of "similar" units or to classify units into previously defined groups

• Examples:

- Using the concentration of elements (copper, silver, tin, antimony) in the lead alloy used in bullets, the FBI identifies 'similar' bullets that may be used to infer whether bullets were produced from the same batch of lead
- The US IRS uses data collected from tax returns (income, amount withheld, deductions, ...) to classify taxpayers into two groups: those who will be audited and those who will not

Techniques:

- Classification Analysis (Week 12)
- Cluster Analysis (Week 13)

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Dependence among Variables and Prediction

 Goal: to estimate the relationship among variables and to predict the value of some of them given information on the others

• Examples:

- The associations between measures of risk-taking propensity and measures of socioeconomic characteristics for top-level business executives were used to assess the relation between risk-taking behavior and performance
- The association between test scores, and several college performance variables were used to develop predictors of success in college

Techniques:

- Multivariate Regression (Week 7)
- Repeated Measures Analysis (Week 8)
- Canonical Correlation Analysis (Week 11)

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Hypothesis Testing

 Goal: to test if differences in sets of response mean vectors for two or more groups large enough to be distinguished from sampling variation

• Examples:

- A transportation company wants to know if means for gasoline mileage, repair costs, downtime due to repairs differ for different truck models
- An insurance company wants to know if changing case management practices leads to changes in mean length of hospital stay, mean infection rates, and mean costs

Techniques:

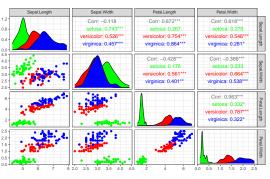
 \bullet Hotelling's T^2 and MAVONA (Week 5 and Week 6)



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Exploratory Data Analysis [EDA, Tukey 1977]

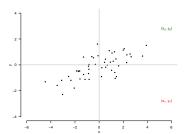


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Statistical Distance

Multivariate methods rely on "distances" between data points: clustering (group units that are "close"); classification (allocate each unit to the "closest" group)



Question: which one $((x_0, y_0) \text{ or } (x_1, y_1))$ is closer the center of the observations? \Rightarrow We will learn **Mahalanobis distance** to formally answer this question



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Matrix Algebra (Week 3)

The study of multivariate methods is greatly facilitated by the use of matrix algebra

- Many operations performed on multivariate data are presented using vector/matrix notation, e.g., $X_{n \times p}$ (Data matrix); $\hat{\mu}_{p \times 1}$ (estimated mean vector); $\hat{\Sigma}_{p \times p}$ (estimated covaraince matrix)
- The computation of eigenvalues and eigenvectors (i.e., the spectral decomposition) plays an important role in multivariate analysis
- We will use R to perform the needed matrix operations



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Multivariate Normal Distribution (Week 4)

• We will often assume the joint distribution of $\boldsymbol{X} = (X_1, X_2, \cdots, X_p)^{\mathrm{T}}$ follows a multivariate normal distribution with the probability density function:

$$f(\boldsymbol{x}|\boldsymbol{\mu},\boldsymbol{\Sigma}) = \frac{1}{(2\pi)^{\frac{d}{2}}\mathrm{det}(\boldsymbol{\Sigma})^{\frac{1}{2}}}\exp\left[-\frac{1}{2}(\boldsymbol{x}-\boldsymbol{\mu})^{\mathrm{T}}\boldsymbol{\Sigma}^{-1}(\boldsymbol{x}-\boldsymbol{\mu})\right]$$

- The multivariate normal assumption is often appropriate:
 - Variables can sometimes be assumed to be multivariate normal (perhaps after transformation)
 - Central limit theorem tells us that distribution of many multivariate sample statistics is approximately normal, regardless of the form of the population distribution

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Data Mining, Machine Learning, and Multivariate Analysis

- Data Mining is the process of extracting and discovering patterns (e.g., unexpected structures or relationships, trends, clusters, and outliers) in massive data sets
- Supervised learning and unsupervised learning are two most common problems in machine learning
- Data mining/machine learning applications usually involve many variables, often related in complex ways, hence techniques from multivariate analysis play an important role

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