

# Week 2

Tuesday, 8 January 2019

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- **Likelihoods**

- Observe phenomenon then compute likelihood of observation given hypothesis
- Ratios
  - $H_0/H_1$  or  $H_1/H_0$
  - Ratio > 8 moderately strong evidence
  - Ratio > 32 strong evidence
  - $H_0$  and  $H_1$  can be not useful hence care need to be taken with ratios
- We can also use  $H_0$  with  $\alpha=0.05$  and  $H_1$  with  $\alpha=0.8$ (power) to compare the likelihood of both. E.g. 2 out 3 study are significant gives ratio of 54
- Mixed results is very likely for example with 3 studies, even with  $H_1$  true likeliness to not find 3 significant result is 49%!

- **Bayesian**

- Use prior belief to infer likeliness of result
- P-value was  $P(\text{data} | H_0)$ , but what you want to know is  $P(H_0 | \text{data})$  and  $P(H_1 | \text{data})$ , for this we update odds from prior to posterior

Posterior odds:

$$\frac{P(H_1 | D)}{P(H_0 | D)} = \frac{P(D | H_1)}{P(D | H_0)} \times \frac{P(H_1)}{P(H_0)}$$

*Posterior = Likelihood Ratio  $\times$  Prior*

- We need to start with initial distribution, called beta distribution of parameters  $\alpha$  and  $\beta$ , for example [50,50] gives a normal around 0.5 i.e. fair coin and [1,1] is uniform distribution

The posterior is a



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Beta( $\alpha^*$ ,  $\beta^*$ ) distribution:

$$\alpha^* = \alpha_{\text{prior}} + \alpha_{\text{likelihood}} - 1$$

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- Bayes factor is relative evidence and enable us to only quantify the relative prob hypothesis being true compared to another hypothesis
- If prior == uniform ==> posterior == likelihood
- Bayesian estimation: only use posterior to estimate plausible values instead of u models
- After prior and data we have a new model and can iterate as many times as wan refine the estimation of the phenomenon observed.
- The Bayes factor represents how much we have updated our beliefs, based on ob data.

- **Practice**

- B C B A A 0.9999131 undetermined answer
- Bayes: compare different posterior given different priors and same  $\Theta$ , Likelihood different  $\Theta$  values
- ??? For Bayes does the posterior and prior not depends on size of study i.e. N?
- Rule of thumb is Bayes factor 1-3 v. small, 3-10 substantial, >10 strong, only des difference in belief. So if starting really small even BF14 will not change our belie
- Credible interval is equivalent to confidence interval for uniform prior only

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