

# Microgirds 1

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```
clc
close all % close figure windows
clear
format compact
```

## Run initialization

```
hw_microgrids1_init;
```

Equation solved.

fsolve completed because the vector of function values is near zero as measured by the value of the function tolerance, and the problem appears regular as measured by the gradient.

<stopping criteria details>

Equation solved.

fsolve completed because the vector of function values is near zero as measured by the value of the function tolerance, and the problem appears regular as measured by the gradient.

<stopping criteria details>

Good job! The init file ran successfully, hopefully the simulation does too.

## Question 1

**The starting system is only energy storage and load (the wind turbine is commented out). The system is stable -- meaning  $\Delta\omega_{pu}$  is kept within  $\pm 0.10$  -- but the starting energy storage power and energy capacity are way oversized.**

**Use the smallest  $es.P_{pe\_rated}$  and  $es.E_{rated\_kWh}$  that works well (e.g., keeps  $\Delta\omega_{pu}$  within  $\pm 0.10$ ) plus a 10% margin of safety in the power and energy capacity (i.e., make the power and energy capacity 10% larger than the bare minimum).**

To find the smallest  $es.P_{pe\_rated}$  and  $es.E_{rated\_kWh}$  that works well, I first gradually reduce  $es.E_{rated\_kWh}$  from the original setting 24,000 kWh and rerun the simulation.

For each values, I check the simulation result:

- $\Delta\omega_{pu}$  stay within  $\pm 0.10$
- SOC remain within -0.01 to 1.01 (due to the Relay setting)
- $p_{es}$  has no larger oscillation

The value of 4,145 kWh is the smallest required energy capacity I got to meet my checklist and let the system operate stably, as shown in Figure 1.

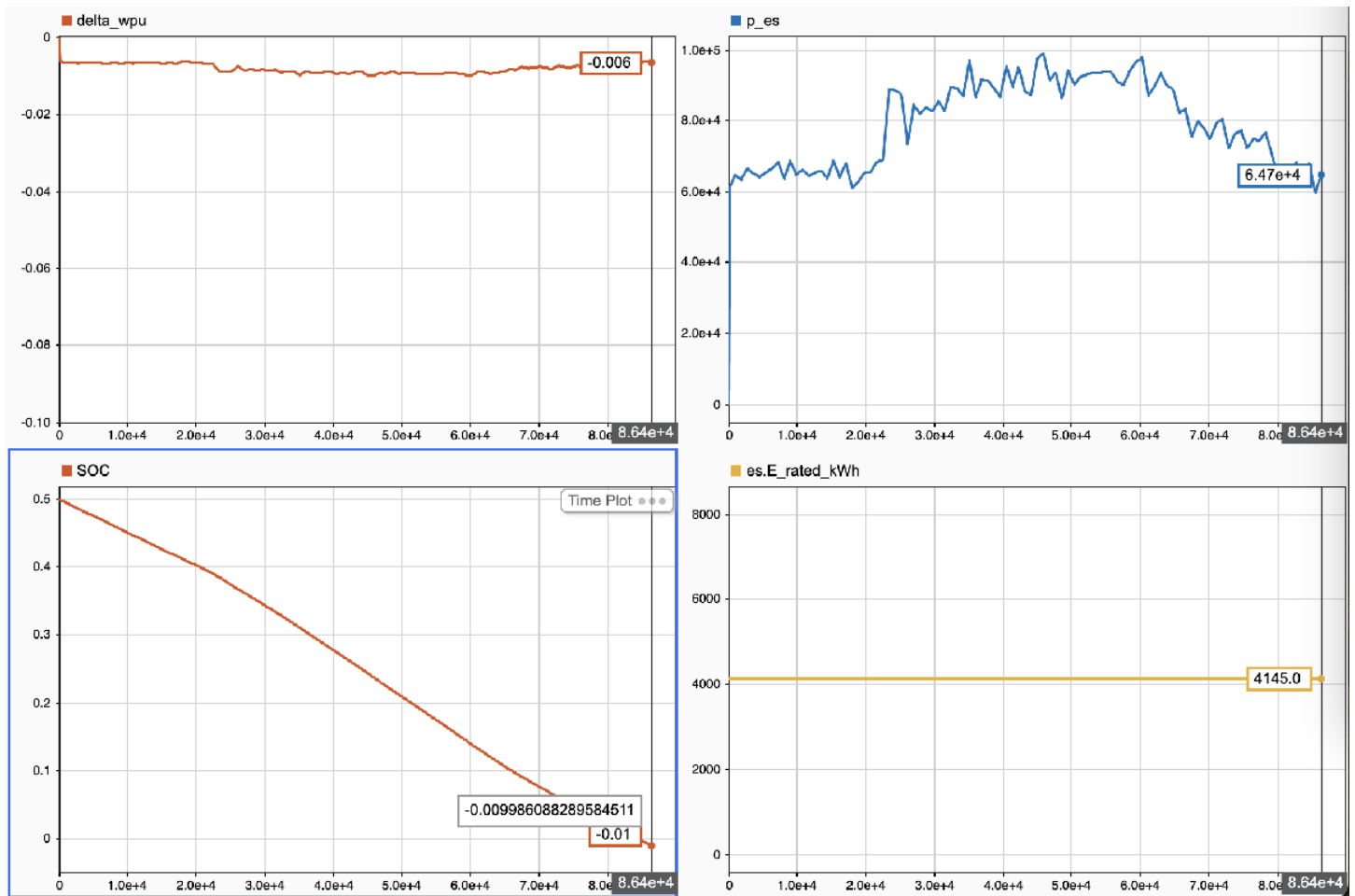


Figure 1. The smallest  $es.E\_rated\_kWh$  is 4,145 kWh when only the Energy Storage system is enable.

```
es.E_rated_kWh = 4145;
fprintf("The smallest required energy capacity: %.2f kWh", es.E_rated_kWh)
```

The smallest required energy capacity: 4145.00 kWh

Finally, apply the safety margin to  $es.E\_rated\_kWh$ . We got the smallest  $es.E\_rated\_kWh = 4,559.5$  kWh.

```
es.E_rated_kWh = es.E_rated_kWh*1.1;
fprintf("The smallest es.E_rated_kWh: %.2f kWh", es.E_rated_kWh)
```

The smallest  $es.E\_rated\_kWh$ : 4559.50 kWh

The peak power of the load demand is 100 kW. Then, the required  $es.P\_pe\_rated$  should be adjusted for efficiency loss.

```
es.P_pe_rated = maxLoadPower/es.eta_pe;
fprintf("The es.P_pe_rated before efficiency loss: %.2d kW", es.P_pe_rated/1000)
```

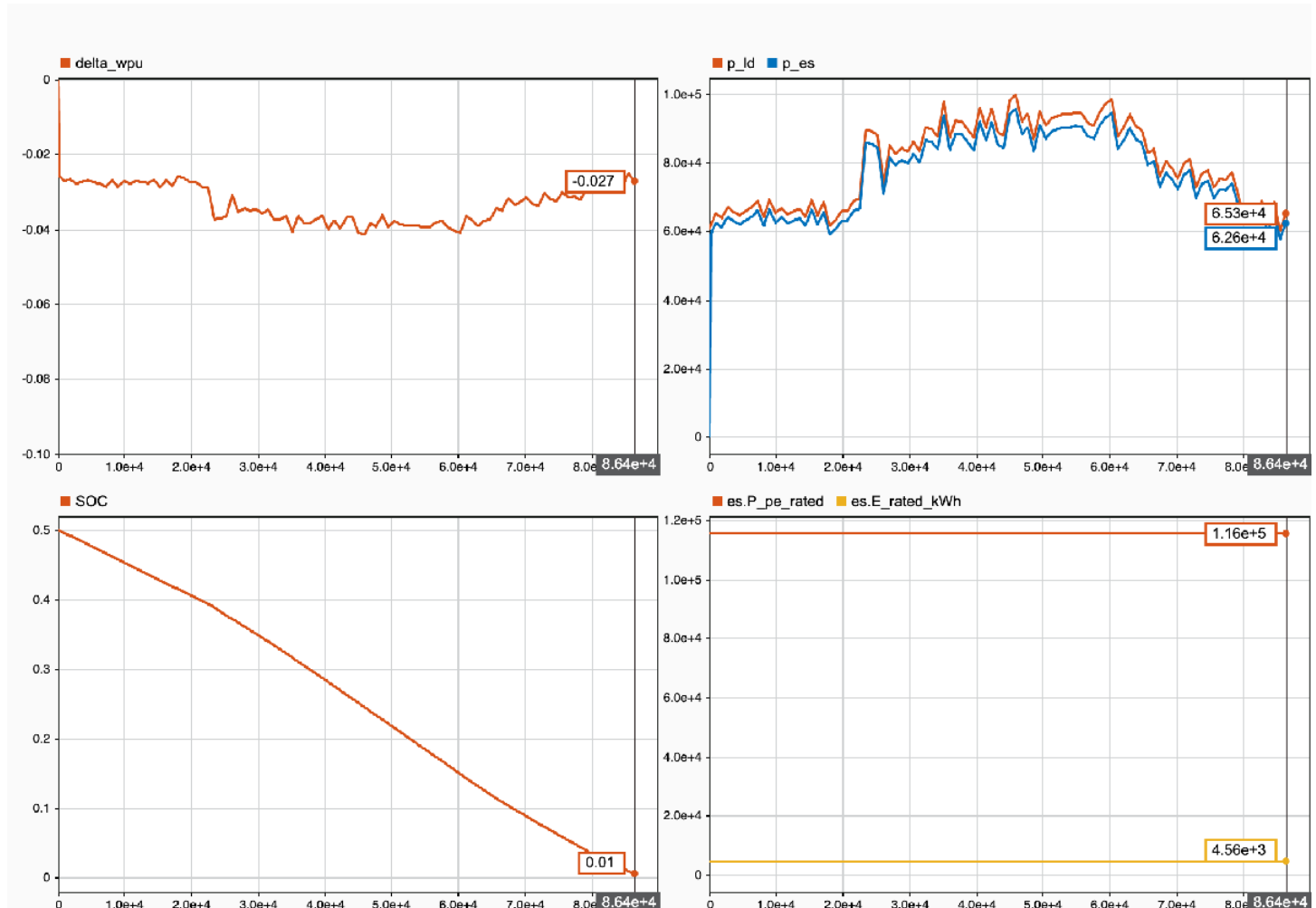
The  $es.P\_pe\_rated$  before efficiency loss: 1.05e+02 kW

Finally, apply the safety margin to  $es.P\_pe\_rated$ . We got the smallest  $es.P\_pe\_rated = 116$  kW.

```
es.P_pe Rated = es.P_pe Rated*1.1;
fprintf("The smallest es.P_pe Rated: %.2d kW", es.P_pe Rated/1000)
```

The smallest es.P\_pe Rated: 1.16e+02 kW

Plot {p\_ld, p\_es} and SOC and delta\_wpu and show what es.P\_pe Rated, and es.E Rated\_kWh you used.



Using an estimate of \$100 per kW of power capacity, and \$130 per kWh of energy capacity, how much does your energy storage cost? (Start with SOC = 0.5.)

```
energyStorageCost_power = energyStorageCost_dollarsperkW*es.P_pe Rated/1000;
fprintf("The cost of power: $%.3.0f", energyStorageCost_power)
```

The cost of power: \$11579

```
energyStorageCost_energy = energyStorageCost_dollarsperkWh*es.E Rated_kWh;
fprintf("The cost of energy: $%.3.0f", energyStorageCost_energy)
```

The cost of energy: \$592735

```
fprintf("Total cost of energy storage system: $%3.0f",
energyStorageCost_power + energyStorageCost_energy)
```

Total cost of energy storage system: \$604314

## Question 2

**Now add the wind turbine. What is now the smallest energy storage  $es.P_{pe\_rated}$  and  $es.E_{rated}$  you can safely use?**

In theory, if we add the wind turbine power, the  $es.P_{pe\_rated}$  and  $es.E_{rated\_kWh}$  can be smaller than the derivation from Question 1. Therefore, I started the  $es.E_{rated\_kWh}$  from the value of 1500 and gradually reduced it to find the smallest value that still makes the system stable.

Similarly, the value of 1,365 kWh is the smallest required energy capacity I got to meet my checklist and let the system operate stably, as shown in Figure 2.

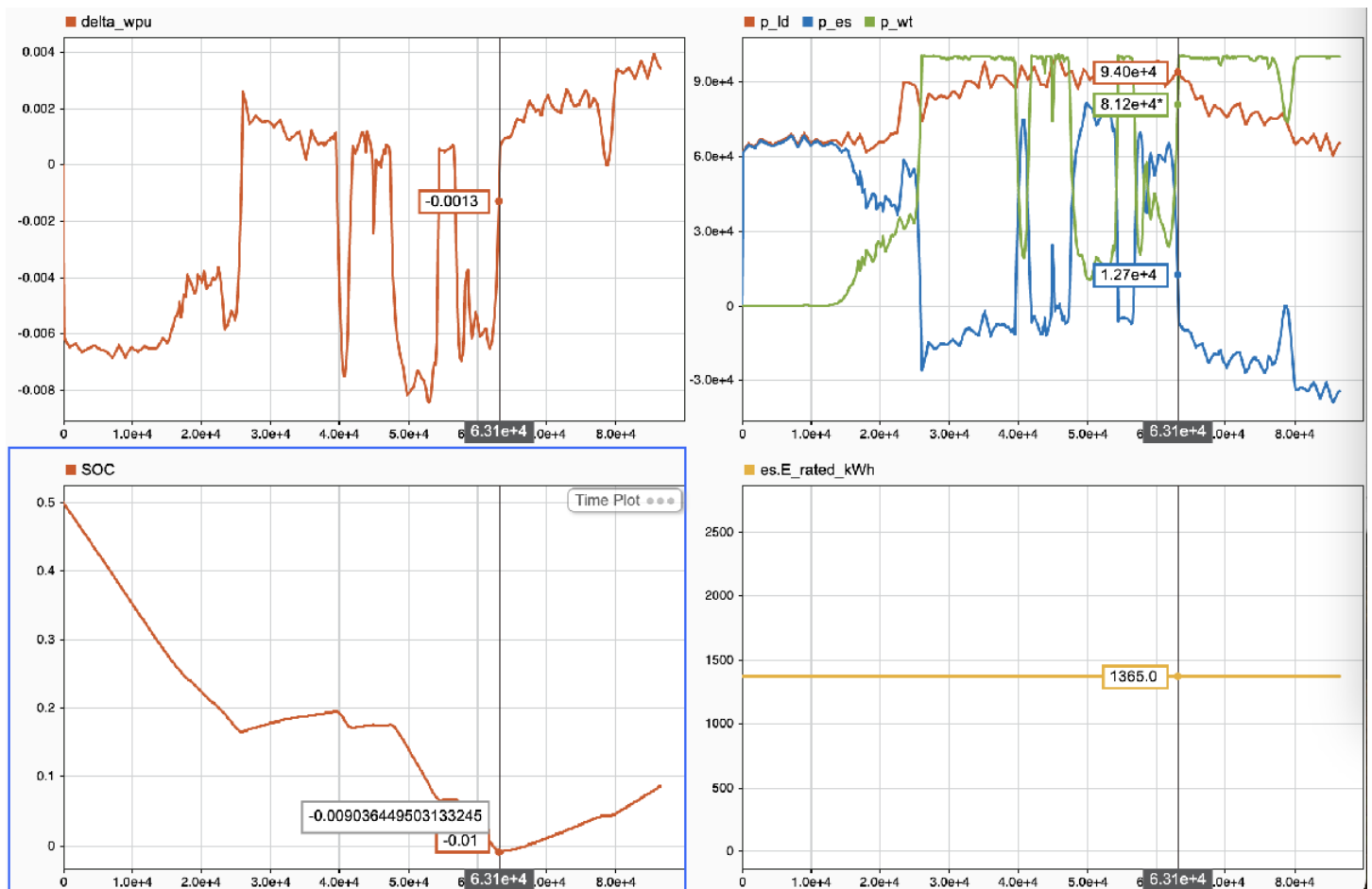


Figure 2. The smallest  $es.E_{rated\_kWh}$  is 1,365 kWh when both Energy Storage and Wind Turbine are enable.

```
es.E_rated_kWh = 1365;
```

```
fprintf("The smallest required storage energy: %.2f kWh", es.E Rated_kWh)
```

The smallest required storage energy: 1365.00 kWh

Finally, apply the safety margin to es.E Rated\_kWh. We got the smallest es.E Rated\_kWh = 1,501.5 kWh.

```
es.E Rated_kWh = es.E Rated_kWh*1.1;  
fprintf("The smallest es.E Rated_kWh: %.2f kWh", es.E Rated_kWh)
```

The smallest es.E Rated\_kWh: 1501.50 kWh

The peak power of the load demand is not 100 kW due to the wind turbine system.

```
log = sim("hw_microgrids1_both").logout;  
p_es = log.getElement("p_es").Values.Data;  
maxLoadPower_with_tb = max(p_es);  
fprintf("The max required with turbine power: %.2d kW",  
maxLoadPower_with_tb/1000) % 8.19e+01 kW
```

The max required with turbine power: 8.19e+01 kW

Then, the required es.P\_pe Rated should be adjusted for efficiency loss.

```
es.P_pe Rated = maxLoadPower_with_tb/es.eta_pe;  
fprintf("The es.P_pe Rated before efficiency loss: %.2d kW", es.P_pe Rated/  
1000) % 8.63e+01 kW
```

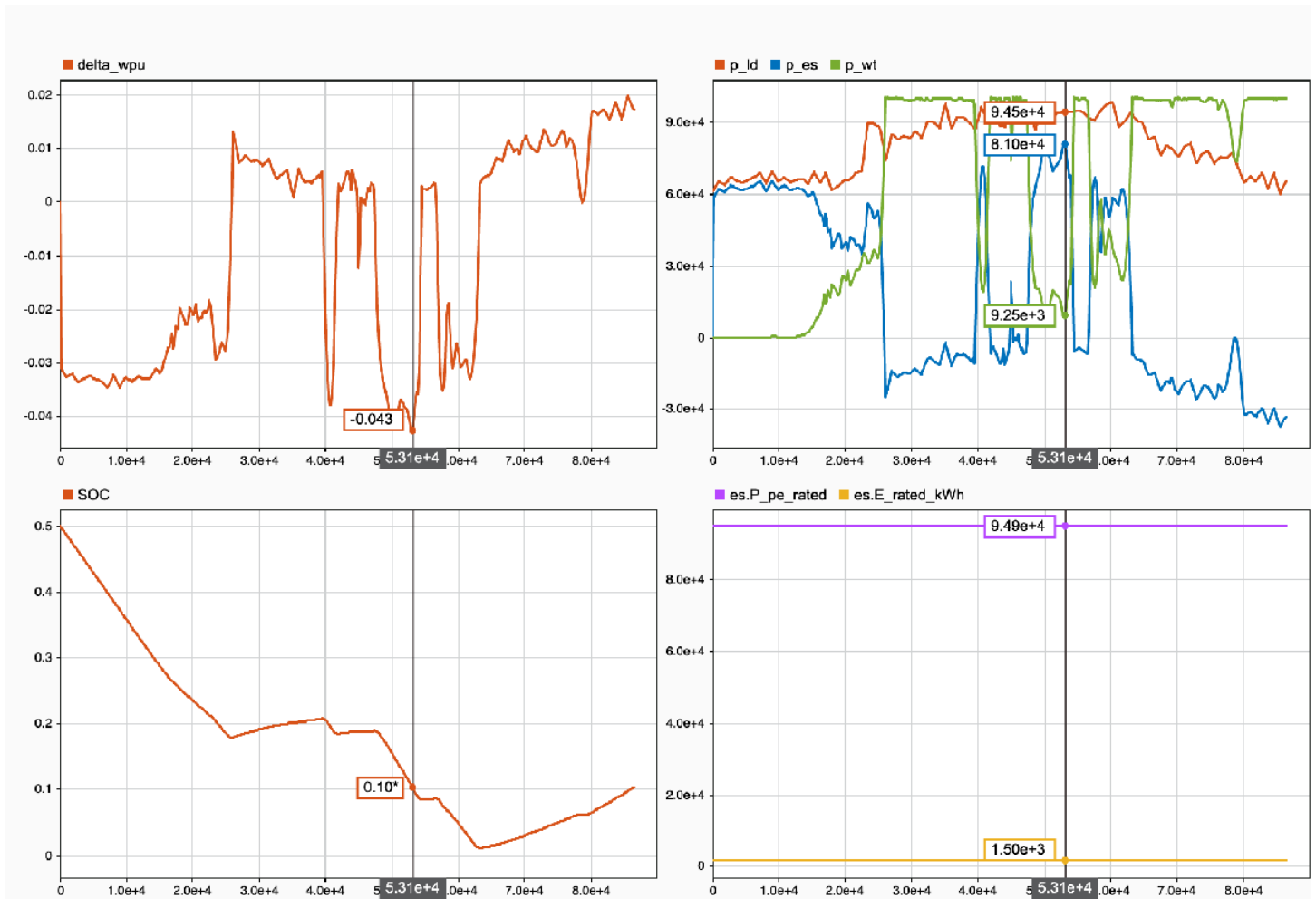
The es.P\_pe Rated before efficiency loss: 8.63e+01 kW

Finally, apply the safety margin to es.P\_pe Rated. We got the smallest es.P\_pe Rated = 94.9 kW.

```
es.P_pe Rated = es.P_pe Rated*1.1;  
fprintf("The smallest es.P_pe Rated: %.2d kW", es.P_pe Rated/1000) %  
9.49e+01 kW
```

The smallest es.P\_pe Rated: 9.49e+01 kW

**Plot {p\_ld, p\_es, p\_wt} and SOC and delta\_wpu and show what es.P\_pe Rated, and es.E Rated\_kWh you used.**



### Why is the energy storage smaller than what you found initially?

First of all, the initial energy storage power and energy capacity are way oversized. Secondly, the simulation revealed the actual energy we need. In addition, the renewable energy source (wind turbine power) is involved in reducing the reliance on energy storage. Thus, it makes sense that the energy storage is smaller than what I found initially.

### How much does it cost now? (Start with SOC=0.5)

```
energyStorageCost_power = energyStorageCost_dollarsperkW*es.P_pe_rated/1000;
fprintf("The cost of power: %.0f", energyStorageCost_power)
```

The cost of power: \$9488

```
energyStorageCost_energy = energyStorageCost_dollarsperkWh*es.E_rated_kWh;
fprintf("The cost of energy: %.0f", energyStorageCost_energy)
```

The cost of energy: \$195195

```
fprintf("Total cost of energy storage system: $%.0f",
energyStorageCost_power + energyStorageCost_energy)
```

Total cost of energy storage system: \$204683

## Question 3

**Add secondary control to the energy storage control.**

Plot `delta_wpu` with and without secondary control in place to show the difference. (Hint: a K of around  $20/(60 \times 10)$  should work OK. That's the same gain of the initial primary loop design, acting over 10 minutes. Don't make the secondary gain too aggressive. You don't want it to over-react. A gentle response is desirable. One test you could do is to step the change the load at some point and see how long it takes for `delta_wpu` to be driven back to zero by the secondary power signal. You want that to take a few minutes.)

### - Without Secondary Control

```
log = sim("hw_microgrids1_both").logout;
x = log.getElement("delta_wpu").Values.Time;
delta_wpu_non_sctrl = log.getElement("delta_wpu").Values.Data;
fprintf("delta_wpu maximum: %f pu, minimum: %f pu",
max(delta_wpu_non_sctrl), min(delta_wpu_non_sctrl))
```

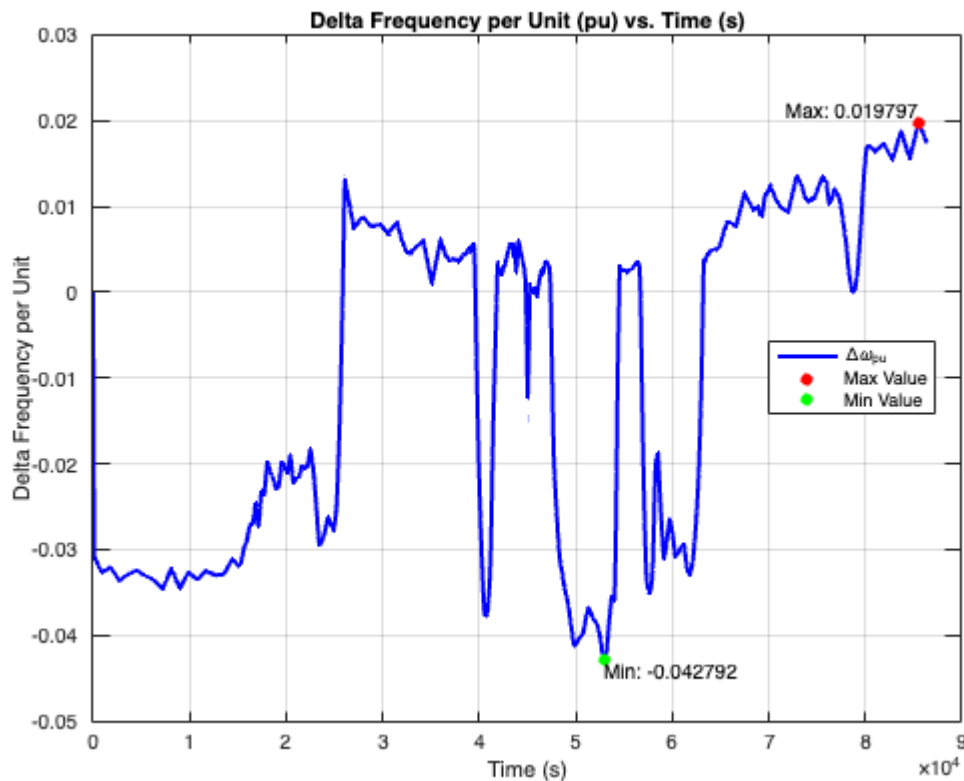
delta\_wpu maximum: 0.019797 pu, minimum: -0.042792 pu

```
fprintf("Frequency range: %f Hz to %f Hz", 60+max(delta_wpu_non_sctrl)*60,
60+min(delta_wpu_non_sctrl)*60)
```

Frequency range: 61.187811 Hz to 57.432506 Hz

```
[max_val, max_idx] = max(delta_wpu_non_sctrl);
[min_val, min_idx] = min(delta_wpu_non_sctrl);
figure;
plot(x, delta_wpu_non_sctrl, '-b', 'LineWidth', 2);
hold on;
scatter(x(max_idx), max_val, 'ro', 'filled', 'DisplayName', 'Maximum');
scatter(x(min_idx), min_val, 'go', 'filled', 'DisplayName', 'Minimum');
text(x(max_idx), max_val, sprintf('Max: %f', max_val), 'VerticalAlignment',
'bottom', 'HorizontalAlignment', 'right');
text(x(min_idx), min_val, sprintf('Min: %f', min_val), 'VerticalAlignment',
'top', 'HorizontalAlignment', 'left');
ylabel("Delta Frequency per Unit");
ylim([-0.05 0.03]);
xlabel("Time (s)");
title('Delta Frequency per Unit (pu) vs. Time (s)');
legend({'\Delta\omega_{pu}', 'Max Value', 'Min Value'}, 'Location', 'best');
grid on;
```

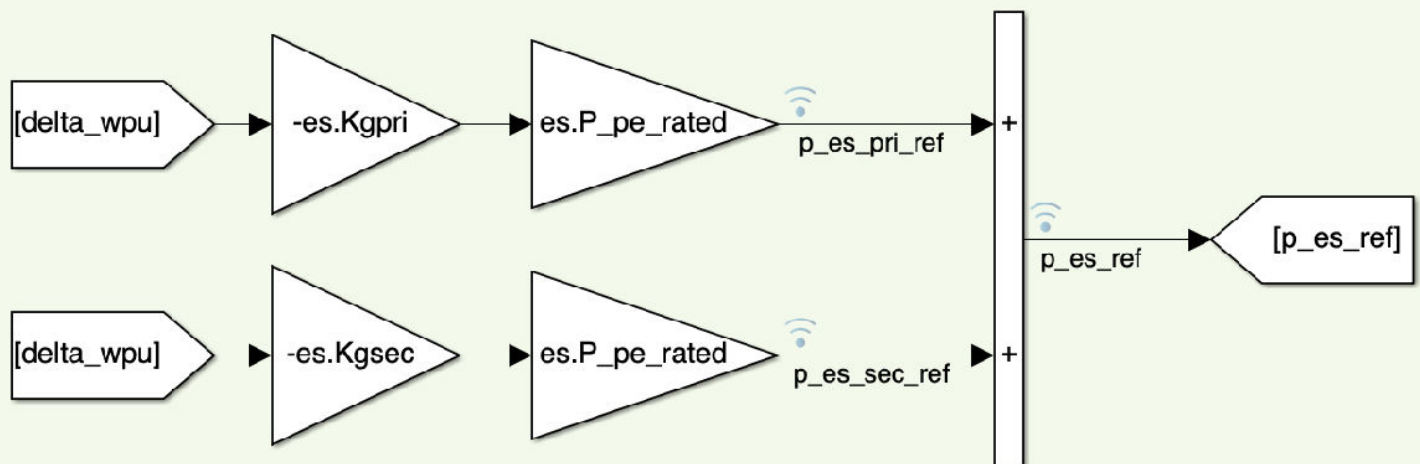
```
hold off;
```



### - With Secondary Control

The most simple implementation would be  $p_{es\_sec\_ref} = -K \cdot \text{integral}(\text{delta\_wpu}) \cdot \text{es.P\_pe\_rated}$  where a large K results in a fast acting secondary loop, and a small K results in a slow loop. Remember that we want the secondary loop to stabilize the frequency to 60 Hz ( $\text{delta\_wpu} = 0$ ) over several minutes.

### Energy Storage Control





Surprisingly, when the K of secondary control is set to  $20/(60 \times 10)$ , it barely affects the delta\_wpu, Frequency range is still 61.187757 Hz to 57.432623 Hz. However, when the K is set to 100, the Frequency range is 60.206588 Hz to 59.553478 Hz.

```
es.Kgsec = es.Kgpri*5;  
es.Kgsec
```

```
ans =  
100
```

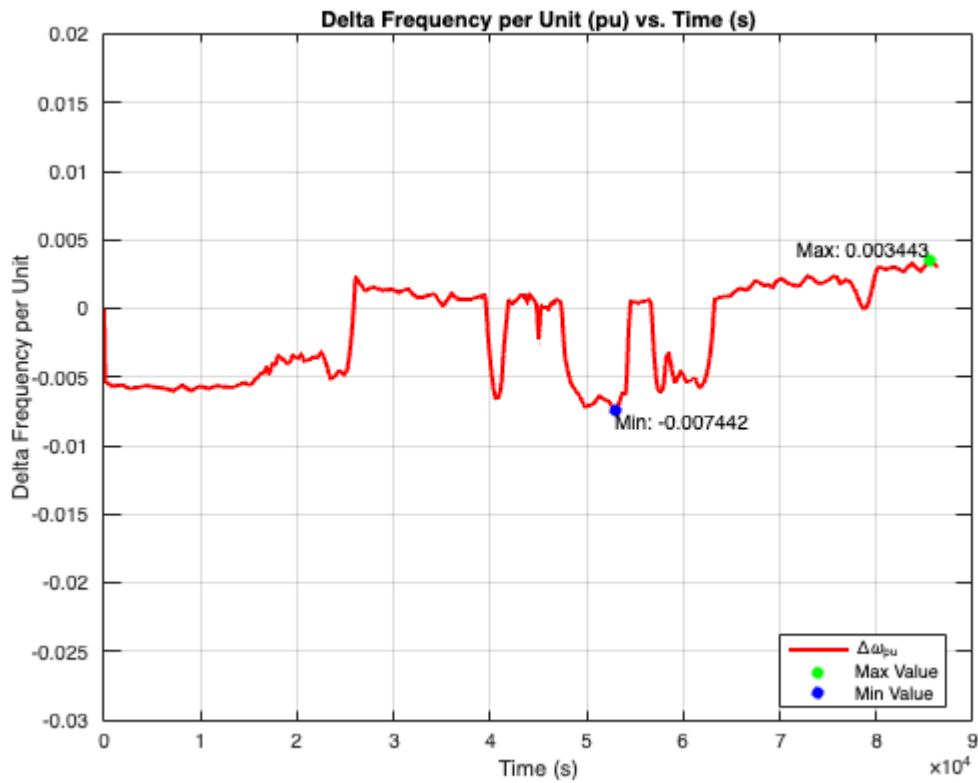
```
log_with_sctrl = sim("hw_microgrids1_with_sctrl").logouts;  
delta_wpu_with_sctrl = log_with_sctrl.getElement("delta_wpu").Values.Data;  
x = log_with_sctrl.getElement("delta_wpu").Values.Time;  
fprintf("delta_wpu maximum: %f pu, minimum: %f pu",  
max(delta_wpu_with_sctrl), min(delta_wpu_with_sctrl))
```

```
delta_wpu maximum: 0.003443 pu, minimum: -0.007442 pu
```

```
fprintf("Frequency range: %f Hz to %f Hz", 60+max(delta_wpu_with_sctrl*60),  
60+min(delta_wpu_with_sctrl*60))
```

```
Frequency range: 60.206598 Hz to 59.553457 Hz
```

```
[max_val, max_idx] = max(delta_wpu_with_sctrl);  
[min_val, min_idx] = min(delta_wpu_with_sctrl);  
figure;  
plot(x, delta_wpu_with_sctrl, '-r', 'LineWidth', 2);  
hold on;  
scatter(x(max_idx), max_val, 'go', 'filled', 'DisplayName', 'Maximum');  
scatter(x(min_idx), min_val, 'bo', 'filled', 'DisplayName', 'Minimum');  
text(x(max_idx), max_val, sprintf('Max: %f', max_val), 'VerticalAlignment',  
'bottom', 'HorizontalAlignment', 'right');  
text(x(min_idx), min_val, sprintf('Min: %f', min_val), 'VerticalAlignment',  
'top', 'HorizontalAlignment', 'left');  
ylabel("Delta Frequency per Unit");  
ylim([-0.03 0.02]);  
xlabel("Time (s)");  
title('Delta Frequency per Unit (pu) vs. Time (s)');  
legend({'\Delta\omega_{pu}', 'Max Value', 'Min Value'}, 'Location', 'best');  
grid on;  
hold off;
```



## Question 4

Calculate the Mean Absolute Error in frequency between the two cases (with and without secondary control).

$$\text{MAE} = \frac{1}{T} \int_0^T |\Delta\omega_{pu}| dt$$

### - Without Secodary Control

```
delta_wpu_non_sctrl_abs = abs(delta_wpu_non_sctrl);
MAE_non_sctrl = trapz(delta_wpu_non_sctrl_abs)*simu.maxStepSize/
simu.endTime;
fprintf("MAE without secondary control: %f", MAE_non_sctrl)
```

MAE without secondary control: 0.018448

### - With Secodary Control

```
delta_wpu_with_sctrl_abs = abs(delta_wpu_with_sctrl);
MAE_with_sctrl = trapz(delta_wpu_with_sctrl_abs)*simu.maxStepSize/
simu.endTime;
fprintf("MAE with secondary control: %f", MAE_with_sctrl)
```

MAE with secondary control: 0.003209