```
In [325]: ▶ import pandas as pd
             import numpy as np
             import warnings
             warnings.filterwarnings('ignore')
             data = pd.read csv('Airlines graph.csv')
In [326]: ▶ import matplotlib.pyplot as plt
             import networkx as nx
             data.shape
             data.dtypes
   Out[326]: year
                                 int64
             month
                                 int64
             day
                                 int64
             dep time
                               float64
              sched_dep_time
                                 int64
             dep delay
                               float64
                               float64
             arr time
             sched arr time
                                 int64
             arr_delay
                               float64
             carrier
                                object
                                 int64
             flight
             tailnum
                                object
             origin
                                object
             dest
                                object
             air time
                               float64
             distance
                                 int64
             dtype: object
In [327]:
           ▶ nx.__version__
   Out[327]: '2.5'
```

```
In [328]:
           # converting sched dep time to 'std' - Scheduled time of departure
              data['std'] = data.sched_dep_time.astype(str).str.replace('(\d{2}$)', '') + ':' + data.sched_dep_time.astype(str).str
In [329]:
           # converting sched arr time to 'sta' - Scheduled time of arrival
              data['sta'] = data.sched arr time.astype(str).str.replace('(\d{2}$)', '') + ':' + data.sched arr time.astype(str).str
             # converting dep time to 'atd' - Actual time of departure
             data['atd'] = data.dep time.fillna(0).astype(np.int64).astype(str).str.replace('(\d{2}$)', '') + ':' + data.dep time.
          # converting arr time to 'ata' - Actual time of arrival
In [330]:
              data['ata'] = data.arr time.fillna(0).astype(np.int64).astype(str).str.replace('(\d{2}$)', '') + ':' + data.arr time.
           | data['date'] = pd.to datetime(data[['year', 'month', 'day']])
In [331]:
In [332]: 

# finally we drop the columns we don't need
              data = data.drop(columns = ['year', 'month', 'day'])
In [333]:

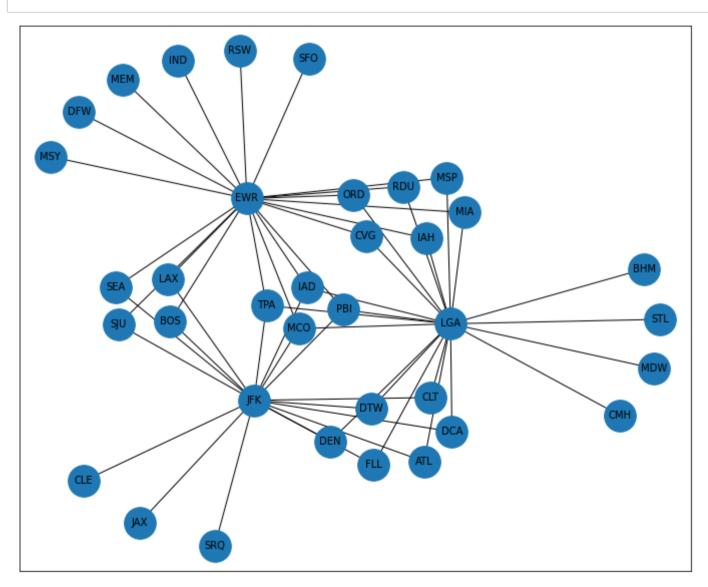
    data["origin"].value counts()

   Out[333]: LGA
                     42
              EWR
                     31
              JFK
                     27
              Name: origin, dtype: int64
          ▶ len(data["dest"].value counts())
In [334]:
   Out[334]: 33
```

```
In [335]:
           FG = nx.from pandas edgelist(data, source='origin', target='dest', edge attr=True,)
In [336]: | len(FG.nodes())
   Out[336]: 36
In [337]: ▶ len(FG.edges())
   Out[337]: 57
In [338]:
           FG.nodes()
   Out[338]: NodeView(('EWR', 'MEM', 'LGA', 'FLL', 'SEA', 'JFK', 'DEN', 'ORD', 'MIA', 'PBI', 'MCO', 'CMH', 'MSP', 'IAD', 'CLT',
              'TPA', 'DCA', 'SJU', 'ATL', 'BHM', 'SRQ', 'MSY', 'DTW', 'LAX', 'JAX', 'RDU', 'MDW', 'DFW', 'IAH', 'SFO', 'STL', 'CV
             G', 'IND', 'RSW', 'BOS', 'CLE'))
In [339]:
           # show how 36 connected by 57 edges
              FG.edges()
   Out[339]: EdgeView([('EWR', 'MEM'), ('EWR', 'SEA'), ('EWR', 'MIA'), ('EWR', 'ORD'), ('EWR', 'MSP'), ('EWR', 'TPA'), ('EWR',
              'MSY'), ('EWR', 'DFW'), ('EWR', 'IAH'), ('EWR', 'SFO'), ('EWR', 'CVG'), ('EWR', 'IND'), ('EWR', 'RDU'), ('EWR', 'IA
              D'), ('EWR', 'RSW'), ('EWR', 'BOS'), ('EWR', 'PBI'), ('EWR', 'LAX'), ('EWR', 'MCO'), ('EWR', 'SJU'), ('LGA', 'FL
              L'), ('LGA', 'ORD'), ('LGA', 'PBI'), ('LGA', 'CMH'), ('LGA', 'IAD'), ('LGA', 'CLT'), ('LGA', 'MIA'), ('LGA', 'DC
              A'), ('LGA', 'BHM'), ('LGA', 'RDU'), ('LGA', 'ATL'), ('LGA', 'TPA'), ('LGA', 'MDW'), ('LGA', 'DEN'), ('LGA', 'MS
              P'), ('LGA', 'DTW'), ('LGA', 'STL'), ('LGA', 'MCO'), ('LGA', 'CVG'), ('LGA', 'IAH'), ('FLL', 'JFK'), ('SEA', 'JF
              K'), ('JFK', 'DEN'), ('JFK', 'MCO'), ('JFK', 'TPA'), ('JFK', 'SJU'), ('JFK', 'ATL'), ('JFK', 'SRQ'), ('JFK', 'DC
             A'), ('JFK', 'DTW'), ('JFK', 'LAX'), ('JFK', 'JAX'), ('JFK', 'CLT'), ('JFK', 'PBI'), ('JFK', 'CLE'), ('JFK', 'IA
              D'), ('JFK', 'BOS')])
```

```
In [340]:  # your code is here (Quick view of the Graph.)
for i in list(FG.edges):
    FG.add_edge(i[0],i[1])

plt.figure(figsize=(12,10))
nx.draw_networkx(FG, node_size = 1000, font_size=10)
plt.show()
```



```
max(dict(nx.eccentricity(FG)).values())
In [341]:
   Out[341]: 4
In [342]: N nx.algorithms.degree centrality(FG) # Notice the 3 airports from which all of our 100 rows of data originates
             # Calculate average edge density of the Graph
             np.mean(list(nx.algorithms.degree centrality(FG).values()))
             # your code is here
   Out[342]: 0.09047619047619045
          nx.average shortest path length(FG) # Average shortest path length for ALL paths in the Graph
In [343]:
   Out[343]: 2.36984126984127
In [344]:
           ▶ nx.average degree connectivity(FG) # For a node of degree k - What is the average of its neighbours' degree?
   Out[344]: {20: 1.95, 1: 19.307692307692307, 2: 19.0625, 17: 2.0588235294117645, 3: 19.0}
           # Let us find the dijkstra path from JAX to DFW.
In [345]:
             # You can read more in-depth on how dijkstra works from this resource - https://courses.csail.mit.edu/6.006/fall11/le
             dijpath = nx.dijkstra path(FG, source='JAX', target='DFW')
             dijpath
   Out[345]: ['JAX', 'JFK', 'SEA', 'EWR', 'DFW']
```

```
In [348]:
                 print(path)
              ['JAX', 'JFK', 'DEN', 'LGA', 'ORD', 'EWR', 'DFW']
              ['JAX', 'JFK', 'DEN', 'LGA', 'PBI', 'EWR', 'DFW']
              ['JAX', 'JFK', 'DEN', 'LGA', 'IAD', 'EWR', 'DFW']
              ['JAX', 'JFK', 'DEN', 'LGA', 'MIA', 'EWR', 'DFW']
              ['JAX', 'JFK', 'DEN', 'LGA', 'RDU', 'EWR', 'DFW']
              ['JAX', 'JFK', 'DEN', 'LGA', 'TPA', 'EWR', 'DFW']
              ['JAX', 'JFK', 'DEN', 'LGA', 'MSP', 'EWR', 'DFW']
              ['JAX', 'JFK', 'DEN', 'LGA', 'MCO', 'EWR', 'DFW']
              ['JAX', 'JFK', 'DEN', 'LGA', 'CVG', 'EWR', 'DFW']
              ['JAX', 'JFK', 'DEN', 'LGA', 'IAH', 'EWR', 'DFW']
              ['JAX', 'JFK', 'SEA', 'EWR', 'DFW']
              ['JAX', 'JFK', 'MCO', 'LGA', 'ORD', 'EWR', 'DFW']
              ['JAX', 'JFK', 'MCO', 'LGA', 'PBI', 'EWR', 'DFW']
              ['JAX', 'JFK', 'MCO', 'LGA', 'IAD', 'EWR', 'DFW']
              ['JAX', 'JFK', 'MCO', 'LGA', 'MIA', 'EWR', 'DFW']
              ['JAX', 'JFK', 'MCO', 'LGA', 'RDU', 'EWR', 'DFW']
              ['JAX', 'JFK', 'MCO', 'LGA', 'TPA', 'EWR', 'DFW']
              ['JAX', 'JFK', 'MCO', 'LGA', 'MSP', 'EWR', 'DFW']
              ['JAX', 'JFK', 'MCO', 'LGA', 'CVG', 'EWR', 'DFW']
              ['JAX', 'JFK', 'MCO', 'LGA', 'IAH', 'EWR', 'DFW']
              ['JAX', 'JFK', 'MCO', 'EWR', 'DFW']
              ['JAX', 'JFK', 'TPA', 'EWR', 'DFW']
              ['JAX', 'JFK', 'TPA', 'LGA', 'ORD', 'EWR', 'DFW']
              ['JAX', 'JFK', 'TPA', 'LGA', 'PBI', 'EWR', 'DFW']
              ['JAX', 'JFK', 'TPA', 'LGA', 'IAD', 'EWR', 'DFW']
              ['JAX', 'JFK', 'TPA', 'LGA', 'MIA', 'EWR', 'DFW']
              ['JAX', 'JFK', 'TPA', 'LGA', 'RDU', 'EWR', 'DFW']
              ['JAX', 'JFK', 'TPA', 'LGA', 'MSP', 'EWR', 'DFW']
              ['JAX', 'JFK', 'TPA', 'LGA', 'MCO', 'EWR', 'DFW']
              ['JAX', 'JFK', 'TPA', 'LGA', 'CVG', 'EWR', 'DFW']
              ['JAX', 'JFK', 'TPA', 'LGA', 'IAH', 'EWR', 'DFW']
              ['JAX', 'JFK', 'SJU', 'EWR', 'DFW']
              ['JAX', 'JFK', 'ATL', 'LGA', 'ORD', 'EWR', 'DFW']
              ['JAX', 'JFK', 'ATL', 'LGA', 'PBI', 'EWR', 'DFW']
              ['JAX', 'JFK', 'ATL', 'LGA', 'IAD', 'EWR', 'DFW']
              ['JAX', 'JFK', 'ATL', 'LGA', 'MIA', 'EWR', 'DFW']
             ['JAX', 'JFK', 'ATL', 'LGA', 'RDU', 'EWR', 'DFW']
```

```
['JAX', 'JFK', 'ATL', 'LGA', 'TPA', 'EWR', 'DFW']
['JAX', 'JFK', 'ATL', 'LGA', 'MSP', 'EWR', 'DFW']
['JAX', 'JFK', 'ATL', 'LGA', 'MCO', 'EWR', 'DFW']
['JAX', 'JFK', 'ATL', 'LGA', 'CVG', 'EWR', 'DFW']
['JAX', 'JFK', 'ATL', 'LGA', 'IAH', 'EWR', 'DFW']
['JAX', 'JFK', 'DCA', 'LGA', 'ORD', 'EWR', 'DFW']
['JAX', 'JFK', 'DCA', 'LGA', 'PBI', 'EWR', 'DFW']
['JAX', 'JFK', 'DCA', 'LGA', 'IAD', 'EWR', 'DFW']
['JAX', 'JFK', 'DCA', 'LGA', 'MIA', 'EWR', 'DFW']
['JAX', 'JFK', 'DCA', 'LGA', 'RDU', 'EWR', 'DFW']
['JAX', 'JFK', 'DCA', 'LGA', 'TPA', 'EWR', 'DFW']
['JAX', 'JFK', 'DCA', 'LGA', 'MSP', 'EWR', 'DFW']
['JAX', 'JFK', 'DCA', 'LGA', 'MCO', 'EWR', 'DFW']
['JAX', 'JFK', 'DCA', 'LGA', 'CVG', 'EWR', 'DFW']
['JAX', 'JFK', 'DCA', 'LGA', 'IAH', 'EWR', 'DFW']
['JAX', 'JFK', 'DTW', 'LGA', 'ORD', 'EWR', 'DFW']
['JAX', 'JFK', 'DTW', 'LGA', 'PBI', 'EWR', 'DFW']
['JAX', 'JFK', 'DTW', 'LGA', 'IAD', 'EWR', 'DFW']
['JAX', 'JFK', 'DTW', 'LGA', 'MIA', 'EWR', 'DFW']
['JAX', 'JFK', 'DTW', 'LGA', 'RDU', 'EWR', 'DFW']
['JAX', 'JFK', 'DTW', 'LGA', 'TPA', 'EWR', 'DFW']
['JAX', 'JFK', 'DTW', 'LGA', 'MSP', 'EWR', 'DFW']
['JAX', 'JFK', 'DTW', 'LGA', 'MCO', 'EWR', 'DFW']
['JAX', 'JFK', 'DTW', 'LGA', 'CVG', 'EWR', 'DFW']
['JAX', 'JFK', 'DTW', 'LGA', 'IAH', 'EWR', 'DFW']
['JAX', 'JFK', 'LAX', 'EWR', 'DFW']
['JAX', 'JFK', 'FLL', 'LGA', 'ORD', 'EWR', 'DFW']
['JAX', 'JFK', 'FLL', 'LGA', 'PBI', 'EWR', 'DFW']
['JAX', 'JFK', 'FLL', 'LGA', 'IAD', 'EWR', 'DFW']
['JAX', 'JFK', 'FLL', 'LGA', 'MIA', 'EWR', 'DFW']
['JAX', 'JFK', 'FLL', 'LGA', 'RDU', 'EWR', 'DFW']
['JAX', 'JFK', 'FLL', 'LGA', 'TPA', 'EWR', 'DFW']
['JAX', 'JFK', 'FLL', 'LGA', 'MSP', 'EWR', 'DFW']
['JAX', 'JFK', 'FLL', 'LGA', 'MCO', 'EWR', 'DFW']
['JAX', 'JFK', 'FLL', 'LGA', 'CVG', 'EWR', 'DFW']
['JAX', 'JFK', 'FLL', 'LGA', 'IAH', 'EWR', 'DFW']
['JAX', 'JFK', 'CLT', 'LGA', 'ORD', 'EWR', 'DFW']
['JAX', 'JFK', 'CLT', 'LGA', 'PBI', 'EWR', 'DFW']
['JAX', 'JFK', 'CLT', 'LGA', 'IAD', 'EWR', 'DFW']
['JAX', 'JFK', 'CLT', 'LGA', 'MIA', 'EWR', 'DFW']
['JAX', 'JFK', 'CLT', 'LGA', 'RDU', 'EWR', 'DFW']
['JAX', 'JFK', 'CLT', 'LGA', 'TPA', 'EWR', 'DFW']
```

```
['JAX', 'JFK', 'CLT', 'LGA', 'MSP', 'EWR', 'DFW']
['JAX', 'JFK', 'CLT', 'LGA', 'MCO', 'EWR',
['JAX', 'JFK', 'CLT', 'LGA', 'CVG', 'EWR', 'DFW']
['JAX', 'JFK', 'CLT', 'LGA', 'IAH', 'EWR', 'DFW']
       'JFK', 'PBI', 'LGA', 'ORD', 'EWR',
['JAX',
['JAX', 'JFK', 'PBI', 'LGA', 'IAD', 'EWR', 'DFW']
['JAX', 'JFK', 'PBI', 'LGA', 'MIA', 'EWR',
['JAX', 'JFK', 'PBI', 'LGA', 'RDU', 'EWR',
['JAX', 'JFK', 'PBI', 'LGA', 'TPA', 'EWR', 'DFW']
['JAX', 'JFK', 'PBI', 'LGA', 'MSP', 'EWR',
['JAX', 'JFK', 'PBI', 'LGA', 'MCO', 'EWR', 'DFW']
['JAX', 'JFK', 'PBI', 'LGA', 'CVG', 'EWR', 'DFW']
['JAX', 'JFK', 'PBI', 'LGA', 'IAH', 'EWR', 'DFW']
['JAX', 'JFK', 'PBI', 'EWR', 'DFW']
['JAX', 'JFK', 'IAD', 'LGA', 'ORD', 'EWR',
['JAX', 'JFK', 'IAD', 'LGA', 'PBI', 'EWR', 'DFW']
['JAX', 'JFK', 'IAD', 'LGA', 'MIA', 'EWR',
['JAX', 'JFK', 'IAD', 'LGA', 'RDU', 'EWR',
['JAX', 'JFK', 'IAD', 'LGA', 'TPA', 'EWR', 'DFW']
['JAX', 'JFK', 'IAD', 'LGA', 'MSP', 'EWR',
['JAX', 'JFK', 'IAD', 'LGA', 'MCO', 'EWR', 'DFW']
['JAX', 'JFK', 'IAD', 'LGA', 'CVG', 'EWR', 'DFW']
['JAX', 'JFK', 'IAD', 'LGA', 'IAH', 'EWR', 'DFW']
['JAX', 'JFK', 'IAD', 'EWR', 'DFW']
['JAX', 'JFK', 'BOS', 'EWR', 'DFW']
```

ASSIGNMENT-4 (100 Points)

Please use the Airlines graph.csv for the following questions.

- 1. Please fill "your code here" sections on above cells (10 Points).
- 2. How many maximal cliques we can spot in this airline network? (20 Points)
- 3. List the most busiest/popular airport. (20 Points)
- 4. As a thought leader, identify 6 new routes to recommend. Hint: Think if the pairs are symmetric or not and make your assumption/observation accordingly i.e. whether ORD-LAX and LAX-ORD two separate routes? (50 Points)

```
for i in range(10,0,-1):
In [363]:
                  if list(maximal_cliques(FG,i)) != []:
                      print("max_cliques:",len(list(maximal_cliques(FG,2))))
              list(maximal cliques(FG,2))
              max cliques: 57
   Out[363]: [['SFO', 'EWR'],
               ['LGA', 'MIA'],
               ['LGA', 'ORD'],
               ['LGA', 'DCA'],
               ['LGA', 'DTW'],
               ['LGA', 'IAH'],
               ['LGA', 'CVG'],
               ['LGA', 'CLT'],
               ['LGA', 'DEN'],
               ['LGA', 'STL'],
               ['LGA', 'PBI'],
               ['LGA', 'BHM'],
               ['LGA', 'ATL'],
               ['LGA', 'MCO'],
               ['LGA', 'FLL'],
               ['LGA', 'MSP'],
               ['LGA', 'IAD'],
               ['LGA', 'TPA'],
               ['LGA', 'MDW'],
               ['LGA', 'RDU'],
               ['LGA', 'CMH'],
               ['JAX', 'JFK'],
               ['LAX', 'JFK'],
               ['LAX', 'EWR'],
               ['BOS', 'JFK'],
               ['BOS', 'EWR'],
               ['SEA', 'JFK'],
               ['SEA', 'EWR'],
               ['MEM', 'EWR'],
               ['MSY', 'EWR'],
               ['SRQ', 'JFK'],
               ['DFW', 'EWR'],
```

['RSW', 'EWR'],

```
['CLE', 'JFK'],
['IND', 'EWR'],
['JFK', 'CLT'],
['JFK', 'DEN'],
['JFK', 'DCA'],
['JFK', 'DTW'],
['JFK', 'ATL'],
['JFK', 'FLL'],
['JFK', 'SJU'],
['JFK', 'MCO'],
['JFK', 'IAD'],
['JFK', 'TPA'],
['JFK', 'PBI'],
['SJU', 'EWR'],
['EWR', 'MIA'],
['EWR', 'ORD'],
['EWR', 'MSP'],
['EWR', 'IAH'],
['EWR', 'CVG'],
['EWR', 'MCO'],
['EWR', 'IAD'],
['EWR', 'TPA'],
['EWR', 'RDU'],
['EWR', 'PBI']]
```

3. List the most busiest/popular airport. (20 Points)

```
In [352]:
           # EWR and LGA are two busiest/popular airport due to the most air route.
              degree_dict = dict(nx.degree(FG))
              dict(sorted(degree_dict.items(), key=lambda item: item[1],reverse=True))
   Out[352]: {'EWR': 20,
                'LGA': 20,
                'JFK': 17,
                'PBI': 3,
                'MCO': 3,
                'IAD': 3,
                'TPA': 3,
                'FLL': 2,
               'SEA': 2,
                'DEN': 2,
                'ORD': 2,
                'MIA': 2,
                'MSP': 2,
                'CLT': 2,
               'DCA': 2,
               'SJU': 2,
                'ATL': 2,
                'DTW': 2,
                'LAX': 2,
               'RDU': 2,
                'IAH': 2,
                'CVG': 2,
                'BOS': 2,
                'MEM': 1,
                'CMH': 1,
                'BHM': 1,
                'SRQ': 1,
                'MSY': 1,
                'JAX': 1,
               'MDW': 1,
                'DFW': 1,
                'SFO': 1,
                'STL': 1,
                'IND': 1,
                'RSW': 1,
                'CLE': 1}
```

```
# EWR and LGA are two busiest/popular airport as they are most important node.
In [353]:
              degree cent dict = nx.degree centrality(FG)
              most popular airport = dict(sorted(degree cent dict.items(),
                                          key=lambda item: item[1],reverse=True))
              most popular airport
   Out[353]: {'EWR': 0.5714285714285714,
               'LGA': 0.5714285714285714,
               'JFK': 0.4857142857142857,
               'PBI': 0.08571428571428572,
               'MCO': 0.08571428571428572,
               'IAD': 0.08571428571428572,
               'TPA': 0.08571428571428572,
               'FLL': 0.05714285714285714,
               'SEA': 0.05714285714285714,
               'DEN': 0.05714285714285714,
               'ORD': 0.05714285714285714,
               'MIA': 0.05714285714285714,
               'MSP': 0.05714285714285714,
               'CLT': 0.05714285714285714,
               'DCA': 0.05714285714285714,
               'SJU': 0.05714285714285714,
               'ATL': 0.05714285714285714,
               'DTW': 0.05714285714285714,
               'LAX': 0.05714285714285714,
```

4.As a thought leader, identify 6 new routes to recommend. Hint: Think if the pairs are symmetric or not and make your assumption/observation accordingly i.e. whether ORD-LAX and LAX-ORD two separate routes? (50 Points)

```
In [355]: # find any undeveloped routes
undeveloped_route = list(set(comb) - set(FG.edges()))
```

```
In [357]:
                                         --strategy-
              # recommend the highest 6th degree centrality undeveloped routes.
              # since developing these routes will help others most.
              most popular airport
    Out[357]: {'EWR': 0.5714285714285714,
                'LGA': 0.5714285714285714,
                'JFK': 0.4857142857142857,
                'PBI': 0.08571428571428572,
                'MCO': 0.08571428571428572,
                'IAD': 0.08571428571428572,
                'TPA': 0.08571428571428572,
                'FLL': 0.05714285714285714,
                'SEA': 0.05714285714285714,
                'DEN': 0.05714285714285714,
                'ORD': 0.05714285714285714,
                'MIA': 0.05714285714285714,
                'MSP': 0.05714285714285714,
                'CLT': 0.05714285714285714,
                'DCA': 0.05714285714285714,
                'SJU': 0.05714285714285714,
                'ATL': 0.05714285714285714,
                'DTW': 0.05714285714285714,
                'LAX': 0.05714285714285714,
                'RDU': 0.05714285714285714,
                'IAH': 0.05714285714285714,
                'CVG': 0.05714285714285714,
                'BOS': 0.05714285714285714,
                'MEM': 0.02857142857142857,
                'CMH': 0.02857142857142857,
                'BHM': 0.02857142857142857,
                'SRQ': 0.02857142857142857,
                'MSY': 0.02857142857142857,
                'JAX': 0.02857142857142857,
                'MDW': 0.02857142857142857,
                'DFW': 0.02857142857142857,
                'SFO': 0.02857142857142857,
                'STL': 0.02857142857142857,
                'IND': 0.02857142857142857,
```

```
'RSW': 0.02857142857142857,

'CLE': 0.02857142857142857}

In [358]: 

# convert to list types of for easier handling
most_popular_airport = [list(x) for x in list(most_popular_airport.items())]
undeveloped_route = [list(x) for x in undeveloped_route]

In [359]: 
# a = pd.DataFrame(undeveloped_route)

In [360]: 
# calculate sum of degree centrality of each pair

for i in undeveloped_route:
    for j in most_popular_airport:
        if i[0] == j[0]:
              i[0] = j[1]
        if i[1] == j[0]:
              i[1] = j[0]:
              i[1] = j[1]

undeveloped_degree_centrality = [i[0]+i[1] for i in undeveloped_route]
```

Out[361]:

	airporti	airport2	degree_centrality
159	EWR	LGA	1.142857
320	EWR	JFK	1.057143
27	LGA	JFK	1.057143
240	EWR	DCA	0.628571
252	EWR	DTW	0.628571
462	LGA	SJU	0.628571