

#### **Proportion of Varainces**

$$Phenotype(P) = Genotype(G) + Environment(E) + Residual(e)$$

$$V_P = V_g + V_e + V_{ge}$$

$$V_a + V_d + V_i$$

- Heritability is used to measure the proportion of variance
- The proportion of variation that is due to genetics is heritability

Broad Sense heritability 
$$(H^2) = \frac{V_g}{V_p}$$

Proportion of total genetic variance Measures the role of the environment Highly unpredictive-includes  $V_d + V_i$ 

Narrow Sense heritability 
$$(h^2) = \frac{V_a}{V_p}$$

Proportion of additive genetic variance Responds to selection Predictive-includes  $V_a$  Measures breeding Value

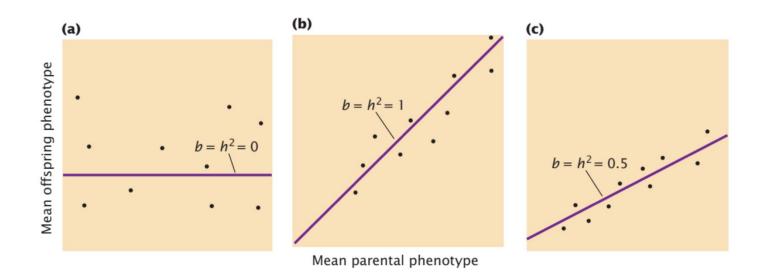
#### **Misconceptions**

- Heritability do not determine genetics
- Individuals do not have heritability.
- Heritability effected by genes and environment.

### **Narrow Sense Heritability**

#### Heritability by parent-offspring regression

 $h^2 = b_{(regression mean offspring again mean if parents)}$ 



The  $h^2$  is equal to the regression coefficient b.

- a) There is no relationship between parental phenotype and offspring
- b) Offspring phenotype is same as parental phenotype
- c) Besides genes some other factors contribute to difference between parent and offspring

#### **Narrow Sense Heritability**

#### **Regression Coefficient of Breeding Values**

$$P_i = A_i + \varepsilon_i$$

where P is phenotype value and A is breeding value and  $\varepsilon$  is residual

$$b_{PA} = \frac{cov(A, P)}{var(P)} = \frac{\sigma_A^2}{\sigma_P^2} = h^2$$

**Accuracy**, which is  $\sqrt{h}$  i as correlation between phenotype (P) and Breeding Value (A)

Correlation coefficient 
$$(r_{AP}) = \frac{Cov(A, P)}{\sqrt{\sigma_A^2 \sigma_P^2}} == b_{AP} \frac{\sqrt{\sigma_P^2}}{\sigma_A^2} = b_{AP} \frac{1}{\sqrt{h^2}} = \frac{h^2}{h} = h$$

### **Narrow Sense Heritability**

Breeding Value is product of Phenotypic Value and heritability

$$A_{expected} = h^2 x P$$

Phenotypic value 
$$(P) = \frac{A \text{ (breeding value)}}{h^2}$$

If heritability is 1, the breeding value equals the Phenotypic value!! Lower the heritability; poor is to indicate the breeding value from phenotypic value

## Measuring Heritability in Plant Breeding

# For Balanced Data (MET data across locations)

$$H^2 = \frac{\sigma_g^2}{\sigma_p^2}$$

Phenotype is mean of genotypes across l locations and r replication per trial, and this has variance (Entry mean based Heritability)

$$H^{2} = \frac{\sigma_{g}^{2}}{\sigma_{g}^{2} + \frac{\sigma_{ge}^{2}}{l} + \frac{\sigma^{2}}{lr}}$$

where,  $\sigma_{ge}^2$  is variance due to genotype x environment,  $\sigma^2$  is residual error variance

## Under balanced Data, $H^2$ has simple and direct interpretations

- a) H<sup>2</sup> is the fraction of phenotypic variation that can be explained by the genotype, where the phenotype is taken to be the arithmetic entry mean.
- b)  $H^2$  is equivalent to the coefficient of determination of a linear regression of the (latent) genotype on the observed phenotype
- c) H<sup>2</sup> is also the squared correla the tion between predicted (phenotypic) value and actual genetic or genotypic value
- d)  $H^2$  can be used to predict the response to selection  $R = h^2S$ , where S

## Measuring Heritability in Plant Breeding

# What if we have these scenarios

- Data is Unbalanced (For example, missing or p rep-design
- Genetic (Random) Effects are correlated, not independent
- Heteroscedastic (heterogeneity of variances)
- Complex variance-covariance structures (spatial variations)

#### Reliability (An Alternative Approach)

$$H_p^2 = rac{\sigma_g^2}{\sigma_g^2 + rac{ar{V}_{BLUE}}{2}}$$
 (Pheipho and Mohrang, 2007)

where, mean variance of difference of BLUEs and  $\sigma_g^2$  is variance of genotypes

$$H_c^2 = 1 - rac{ar{V}_{BLUP}}{2\sigma_g^2}$$
 (Cullis et al. 2006)

where,  $\bar{V}_{BLUP}$  is mean difference of BLUPs and  $\sigma_g^2$  is variance of genotypes