

Module 4:End-to-End Analytical: Pipeline in R

Fundamentals of Genomic Prediction and Data-Drive Crop Breeding

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Contents

| | |
|--|-----------|
| Load the Libraries | 1 |
| Phenotypic Data Analysis in lme4 R Package | 2 |
| Upload the Filtered Phenotypic Data | 2 |
| Quick Visualization of Data | 2 |
| Single Stage/Step Wise Analysis | 4 |
| Subset the Data for One Environment | 5 |
| Run the Mixed model | 5 |
| Results | 5 |
| Extract variance components | 6 |
| Plot the residual vs fitted plot | 6 |
| ANOVA for fixed effects | 8 |
| Extract the Fixed effects | 8 |
| Extract the Random effects | 8 |
| Heritability | 9 |
| Run the Analysis for all Environments | 9 |
| MET Analysis | 10 |
| Combined ANOVA | 10 |
| Check for Homogeneity of Variance | 10 |
| Combined Analysis in lme4 | 11 |
| Summary of MET results | 11 |
| Plot of model | 13 |
| Extract the variance components | 13 |
| Heritability | 13 |
| BLUEs for Random Effects | 14 |
| Accounting Spatial Variability | 14 |
| Additional on MET and Stability Analysis | 16 |
| Additional Literature | 16 |

Load the Libraries

```
> # Load the Required Libraries
> rm(list=ls()) # Remove previous work
> library(rrBLUP)
> library(BGLR)
> library(AGHmatrix)
> library(ggplot2)
> library(DT)
> #library(cuTools)
> library(dplyr)
> library(lme4)
> library(arm)
> library(statgenSTA)
```

This section shows the analysis of filtered phenotypic data in lme4 and other open source R packages. The filtered data set was obtained after pre-processing and Quality check of data

Phenotypic Data Analysis in lme4 R Package

- Here in this section phenotypic data analysis is performed in an open source R package called **lme4**. More on this R package can be found here [lme4 Tutorial 1](#), and [lme4 Tutorial 2](#).
- The purpose of this section is to repeat the phenotypic data analysis in lme4 as ASReml R package is commercial package and may not available for all the users.
- Filtered data set will be used, same one used in ASReml R package to perform the analysis in lme4.
- ANOVA, variance components, BLUPS, BLUES and heritability is extracted for the results part.

Upload the Filtered Phenotypic Data

```
> demo.data.filtered<-read.csv(file="./Data/demo.data.filtered.csv",
+                             header = TRUE)
> # factor conversion if below are not in factors
> columns<-c("Environment", "Genotype", "Rep", "Block", "Row", "Column", "Line.type")
> demo.data.filtered[, columns]<-lapply(columns, function(x) as.factor(demo.data.filtered[[x]]))
> demo.data.filtered$Yield<-as.numeric(demo.data.filtered$Yield)
> demo.data.filtered$HT<-as.numeric(demo.data.filtered$HT)
> demo.data.filtered$DTF<-as.numeric(demo.data.filtered$DTF)
>
> # Subset the required columns
> demo.data.filtered<-demo.data.filtered[, c("Environment", "Genotype", "Rep",
+                                           "Block", "Row", "Column", "Line.type",
+                                           "Yield", "HT", "DTF")]
> # First we will arrange the rows and columns for spatial analysis.
> # Now we will subset the environments and Yields for analysis
> demo.data.filtered<-data.frame(demo.data.filtered%>% group_by(Environment)%>%arrange(Row, Column)) #
> demo.data.filtered<-data.frame(demo.data.filtered%>% arrange(Environment)) # Arrange by environment
>
> #demo.data.filtered<-demo.data.filtered[!demo.data.filtered$Environment %in% c("Env2", "Env5","Env8",
> # View as table in file
> head(demo.data.filtered)
```

| Environment | Genotype | Rep | Block | Row | Column | Line.type | Yield | HT | DTF |
|-------------|----------|-----|-------|-----|--------|-----------|----------|-------|-----|
| Env1 | 44 | 1 | 1 | 1 | 1 | Entry | 4956.395 | 115.6 | 96 |
| Env1 | 131 | 1 | 1 | 1 | 2 | Entry | 5059.207 | 116.0 | 89 |
| Env1 | 17 | 1 | 1 | 1 | 3 | Entry | 4948.038 | 99.0 | 101 |
| Env1 | 146 | 1 | 1 | 1 | 4 | Entry | 6012.658 | 102.8 | 92 |
| Env1 | 123 | 1 | 1 | 1 | 5 | Entry | 4456.759 | 112.2 | 94 |
| Env1 | 116 | 1 | 1 | 1 | 6 | Entry | 4473.946 | 108.0 | 98 |

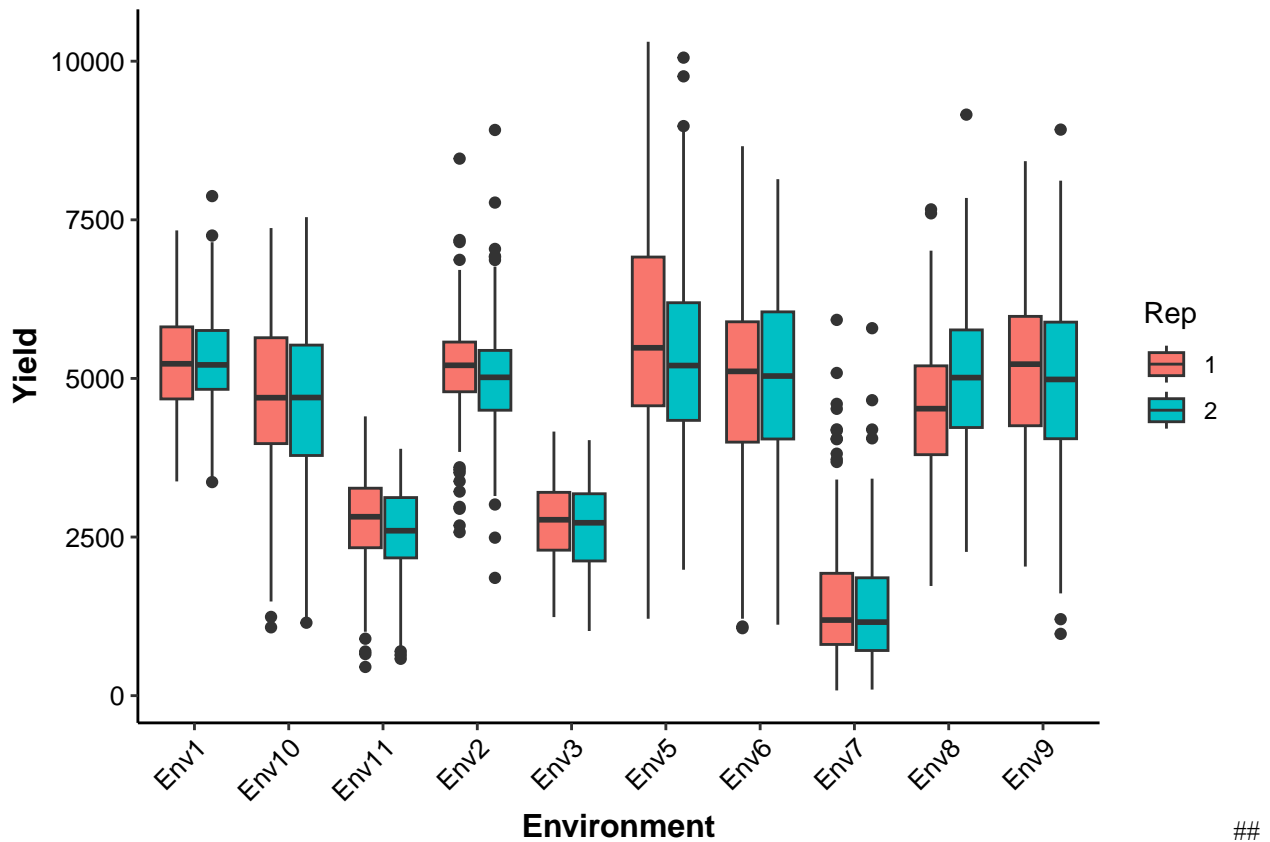
Quick Visualization of Data

```
> ggplot(data = demo.data.filtered, aes(x = Environment, y = Yield, fill = Rep))+
+   geom_boxplot()+
+   theme_classic()+
+   theme(axis.text.x = element_text(angle = 45, hjust = 1)) + # fill by timepoint to give different col
+   #scale_fill_manual(values = c("", ""))+
```

```

+ #scale_color_manual(values = c("", ""))
+ theme (plot.title = element_text(color="black", size=12,hjust=0.5, face = "bold"), # add and modify
+       axis.title.x = element_text(color="black", size=12, face = "bold"), # add and modify title t
+       axis.title.y = element_text(color="black", size=12, face="bold")) + # add and modify title t
+ #scale_y_continuous(limits=c(0,15000), breaks=seq(0,15000,1000), expand = c(0, 0))+
+ theme(axis.text= element_text(color = "black", size = 10)) # modify the axis text

```

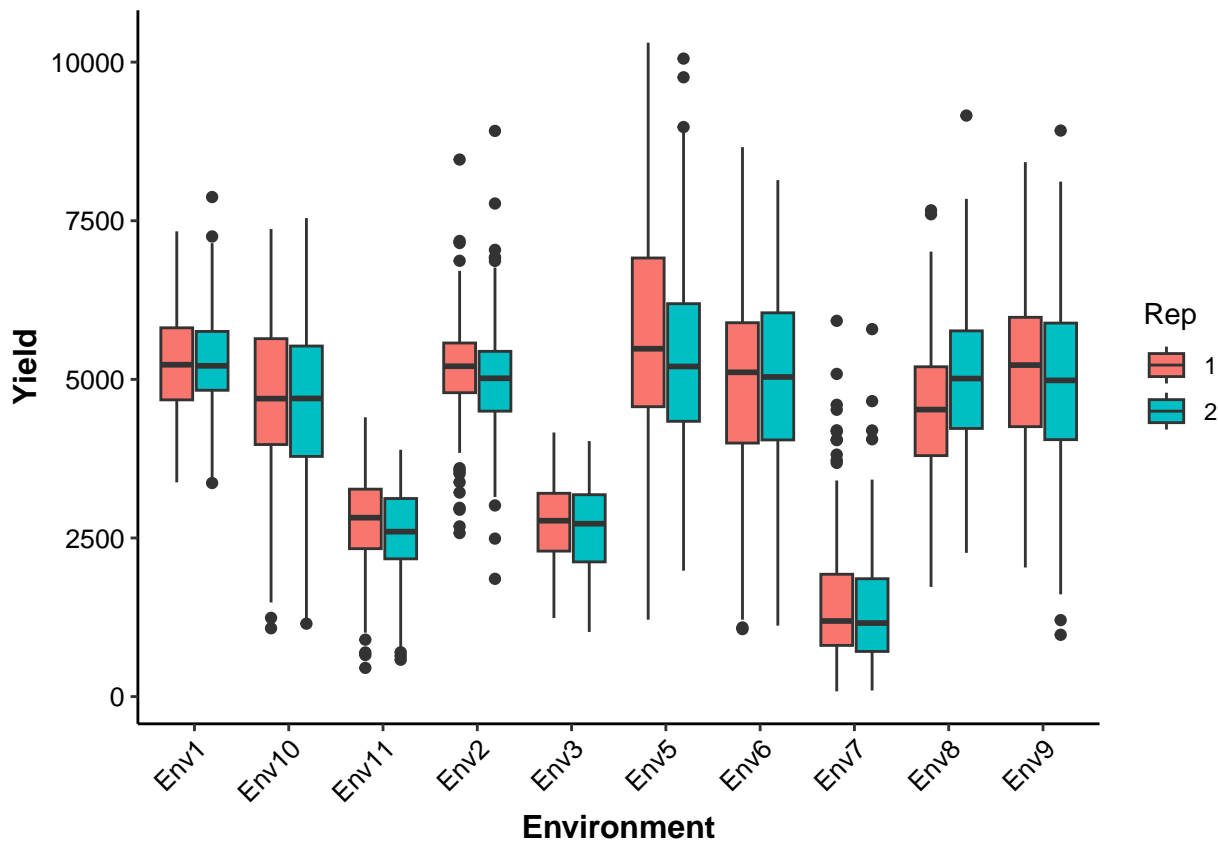


Quick Visualization of Data

```

> ggplot(data = demo.data.filtered, aes(x = Environment, y = Yield, fill = Rep))+
+ geom_boxplot()+
+ theme_classic()+
+ theme(axis.text.x = element_text(angle = 45, hjust = 1)) + # fill by timepoint to give different col
+ #scale_fill_manual(values = c("", ""))+
+ #scale_color_manual(values = c("", ""))
+ theme (plot.title = element_text(color="black", size=12,hjust=0.5, face = "bold"), # add and modify
+       axis.title.x = element_text(color="black", size=12, face = "bold"), # add and modify title to x axi
+       axis.title.y = element_text(color="black", size=12, face="bold")) + # add and modify title to y axi
+ #scale_y_continuous(limits=c(0,15000), breaks=seq(0,15000,1000), expand = c(0, 0))+
+ theme(axis.text= element_text(color = "black", size = 10)) # modify the axis text

```



Single Stage/Step Wise Analysis

- In this section, data analysis will be shown only for grain yield trait using a **Linear Mixed-Model Approach** in lme4 R Package package, and will be useful to the users who do not have access to the commercial **ASReml-R package**.
- In general analysis pipeline is divided in two parts:
 1. **Separate analysis/step-wise**: In this each environment/trial is analyzed separately.
 2. **Combined analysis or Multi-environment trial (MET) analysis**: In this analysis all the environments will be analyzed jointly.
 - Various mixed models from basic to advanced models will be used will for MET analysis.
 - First let us subset the data for on environment to show how to perform the analysis for one trial or environment in lme4 R package
 - We will run models which are feasible in lme4 R package. Note spatial models are not possible to run in lme4 R package.
 - We will use basic models and show how to extract the results

Mixed Effect Model

Single Stage Analysis

Each trial or environment is analyzed separately

Stage-wise analysis is more appropriate.

- Trials with unbalanced data sets,
- Different experimental design factors across trials,
- Avoid the computational challenges of analyzing a huge number of trials.

Two Stage Analysis

All trials combined and analyzed together

Commentary | [Open access](#) | Published: 05 February 2022

Open-source analytical pipeline for robust data analysis, visualizations and sharing in crop breeding

Waseem Hussain , Mahender Anumalla, Margaret Catollos, Apurva Khanna, Ma. Teresa Sta. Cruz, Joie Ramos & Sankalp Bhosale

Plant Methods 18, Article number: 14 (2022) | [Cite this article](#)

8126 Accesses | 2 Citations | 27 Altmetric | [Metrics](#)

Abstract

Subset the Data for One Environment

- Subset the data for one environment first.

```
> # Subset the environment 1
> sub.data<-subset(demo.data.filtered, Environment=="Env1")
> sub.data<-droplevels.data.frame(sub.data)
```

Run the Mixed model

Model 1.lme4

- The model described below is equivalent to *model 1* described in ASReml R package analysis.

$y_{ijk} = \mu + g_i + r_j + b_{jk} + \epsilon_{ijk}$ Where y_{ijk} = is the effect of i th genotype in j th replication and k th block within the j th replication, μ = overall mean, g_i = random effect of the i th genotype, r_j = fixed effect of the j th replication, b_{jk} = random effect of k th block nested within j replication, ϵ_{ijk} = residual error, here we assume errors are independent and identically distributed.

```
> # Now apply model
> model1<-lmer(Yield~Rep+(1|Genotype)+(1|Rep:Block), data =sub.data)
```

Results

- Here we will summarize the results using `summary()` function. The first few lines of output indicate that the model was fitted by REML as well as the value of the REML criterion. The second piece of the summary output provides information regarding the random-effects and residual variation. The third piece of the summary output provides information regarding the fixed-effects and the fourth piece of summary output provides information regarding the correlation of fixed effects.

```
> # Summarise the results
> summary(model1)
```

```
Linear mixed model fit by REML ['lmerMod']
Formula: Yield ~ Rep + (1 | Genotype) + (1 | Rep:Block)
Data: sub.data
```

```
REML criterion at convergence: 6239.3
```

```
Scaled residuals:
```

| Min | 1Q | Median | 3Q | Max |
|----------|----------|---------|---------|---------|
| -1.90048 | -0.59387 | 0.03899 | 0.60311 | 1.71001 |

```
Random effects:
```

| Groups | Name | Variance | Std.Dev. |
|-----------|-------------|----------|----------|
| Genotype | (Intercept) | 431861 | 657.2 |
| Rep:Block | (Intercept) | 28499 | 168.8 |
| Residual | | 193255 | 439.6 |

```
Number of obs: 394, groups: Genotype, 197; Rep:Block, 10
```

```
Fixed effects:
```

| | Estimate | Std. Error | t value |
|-------------|----------|------------|---------|
| (Intercept) | 5233.19 | 94.20 | 55.552 |
| Rep2 | 60.38 | 115.60 | 0.522 |

```
Correlation of Fixed Effects:
```

```
(Intr)
Rep2 -0.614
```

Extract variance components

- Here we will extract variance components

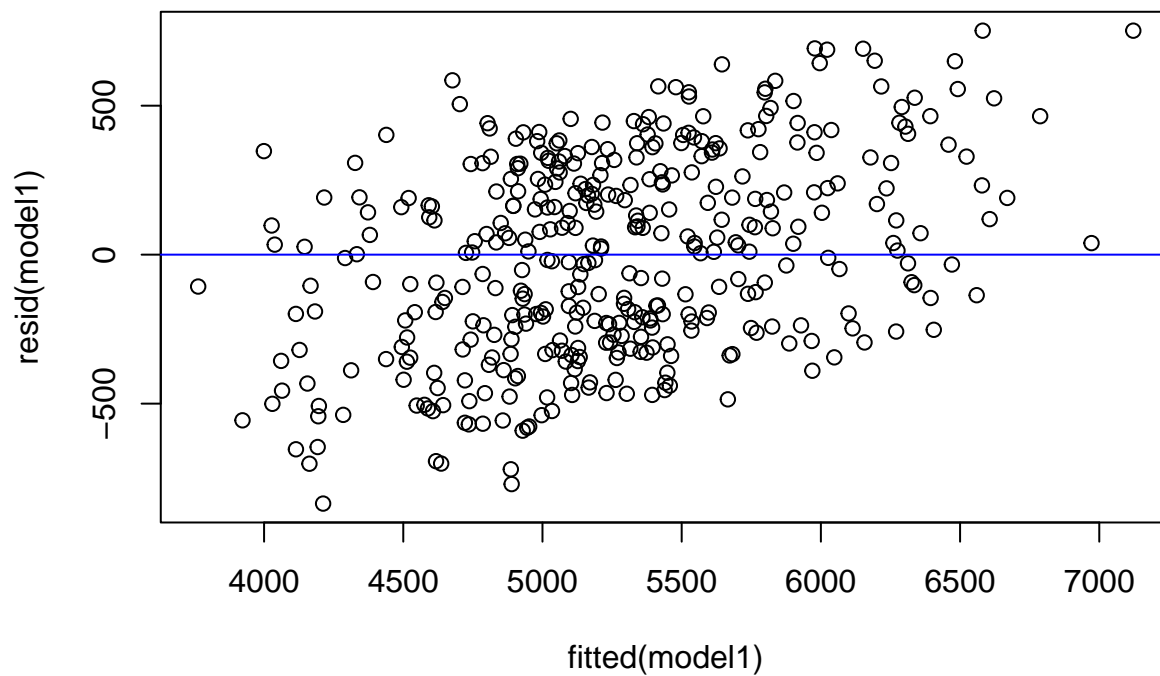
```
> Ve<- VarCorr(model1)
> Ve
```

| Groups | Name | Std.Dev. |
|-----------|-------------|----------|
| Genotype | (Intercept) | 657.16 |
| Rep:Block | (Intercept) | 168.82 |
| Residual | | 439.61 |

Plot the residual vs fitted plot

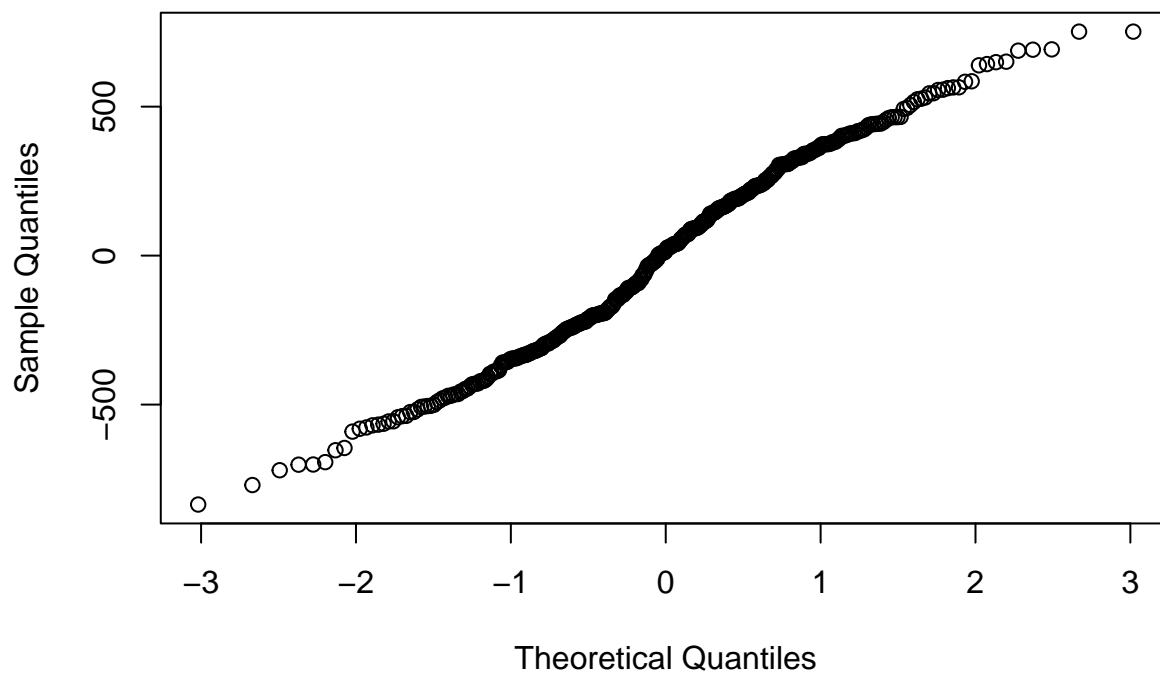
- Here will show how to check for homoscedasticity

```
> # Plot the residual plot
> plot(fitted(model1), resid(model1), type="pearson")
> abline(0,0, col="blue")
```

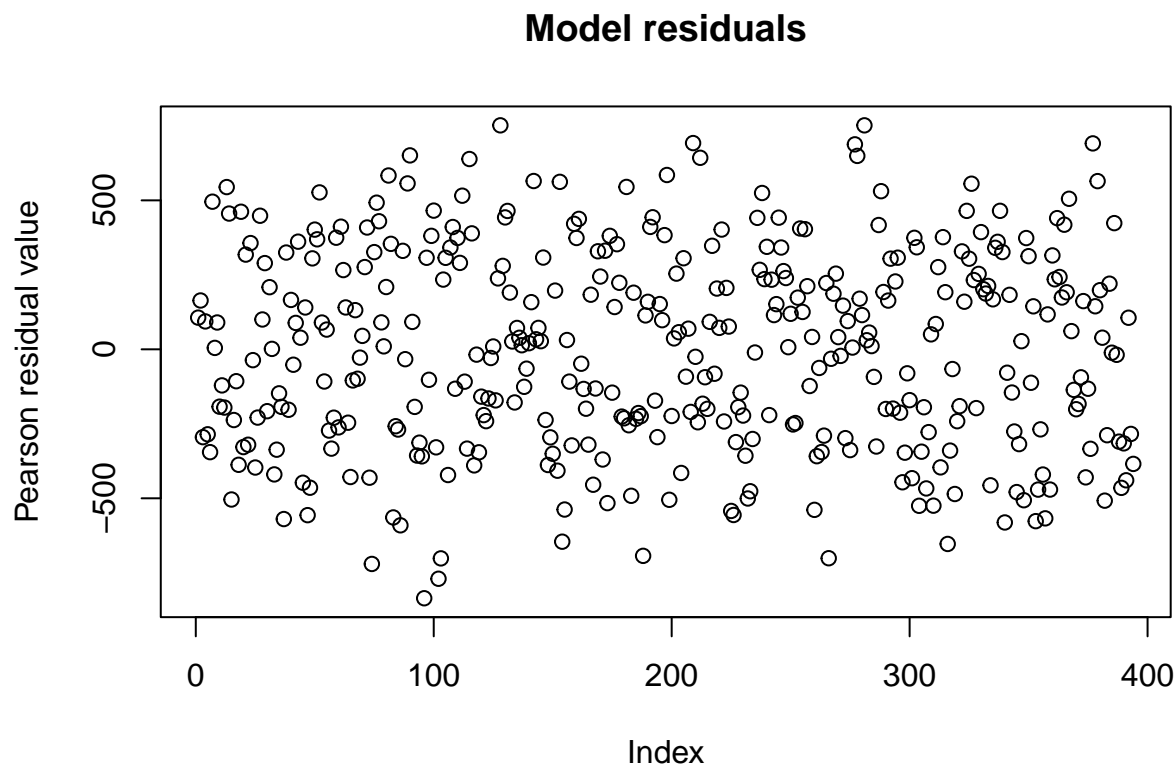


```
> # Plot QQ plot
> qqnorm(resid(model1))
```

Normal Q-Q Plot



```
> # Residual plot
> plot(residuals(model1,type="pearson"), main='Model residuals',
+       ylab='Pearson residual value')
```

ANOVA for fixed effects

```
> # ANOVA
> anova(model1)
```

| | npair | Sum Sq | Mean Sq | F value |
|-----|-------|----------|----------|-----------|
| Rep | 1 | 52724.26 | 52724.26 | 0.2728223 |

Extract the Fixed effects

- Here will show how to extract the BLUEs.

```
> BLUEs<-fixef(model1)
> BLUEs
```

```
(Intercept)      Rep2
  5233.1856      60.3794
```

Extract the Random effects

- Here will show how to extract the BLUPs.

```
> # Extract the Random effects
> BLUPs<-data.frame(Blups.yield=raneff(model1)$Genotype)
> GV<-data.frame(BLUPs.GY=coef(model1)$Genotype[,1]) #Genotype values (Blups +Intercept)
```

Heritability

- Here will show how to calculate the heritability. Two approaches will be show how to estimate heritability: 1) Based on Variance components and 2) Based on Cullis et al. 2006 is also $1 - \frac{\bar{V}_{BLUP}}{2\sigma^2_g}$. Where \bar{V}_{BLUP} is mean variance difference of two genotypes based on BLUPs and σ^2_g is variance of genotypes.

```
> # Extract the variance components
> Ve<- data.frame (VarCorr(model1))
> Ve
```

| grp | var1 | var2 | vcov | sdcor |
|-----------|-------------|------|-----------|----------|
| Genotype | (Intercept) | NA | 431860.94 | 657.1613 |
| Rep:Block | (Intercept) | NA | 28498.55 | 168.8151 |
| Residual | NA | NA | 193254.94 | 439.6077 |

```
> # Now calculate heritability using variance components
> genotype.var=Ve[1,4]
> error.var=Ve[2,4]
> # Now heritability
> h2=genotype.var/(genotype.var+error.var)*100
> h2
```

```
[1] 93.8095
```

```
> # Reliability
> std.err<-se.ranef(model1)$Genotype
> v_BLUP<- mean(std.err)
> # Heritability/Reliability
> h2<- (1-((v_BLUP)^2/(Ve[1,4]*2)))*100
> h2
```

```
[1] 90.55036
```

Run the Analysis for all Environments

```
> # Run the analysis and check reliability
> # For Non-Stress Data using DTF as co-variate
> demo.data.filtered$Environment<- as.character(demo.data.filtered$Environment)
> un.exp<- unique(demo.data.filtered$Environment)
> for(i in 1:length(un.exp)){
+   sub<- droplevels.data.frame(demo.data.filtered[which(demo.data.filtered$Environment==un.exp[i]),])
+
+   model<-lmer(Yield~Rep+(1|Genotype)+ (1|Rep:Block), data =sub)
+   #BLUPs<-data.frame(Blups.yield=ranef(model)$Genotype, Environment=un.exp[i])
+   BLUPs<-data.frame(BLUPs.GY=coef(model)$Genotype[,1], Environment=un.exp[i])
+   if(i>1){
+     BLUPs.all<-rbind(BLUPs.all, BLUPs)
+   }
+   else{
+     BLUPs.all<- BLUPs
+   }
+ }
> # Save the BLUES out put file for Genomic Predictions
> #estimates.all$Genotype<-gsub("^.{8}", "", estimates.all$Genotype)
```

MET Analysis

Model 2.lme4

- Here we will analyze all the environments jointly and extract the single BLUE for each genotype. We will use mixed model analysis in lme4 r package model. We will treat genotypes as fixed and environment as random effect.

Combined ANOVA

- Here ANOVA will be generated for all the factor levels.
- Replications are nested with environments and Blocks are within Replications which are nested within environment.

```
> # Linear model to get ANOVA
> demo.data.filtered$Environment<-as.factor(demo.data.filtered$Environment)
> model.anova<-lm(formula = Yield~Genotype+Environment+Genotype*Environment+Environment:Rep+ Environment:Block,
+ data=demo.data.filtered)
> # Get ANOVA
> anova(model.anova)
```

| | Df | Sum Sq | Mean Sq | F value | Pr(>F) |
|-----------------------|------|------------|-------------|-------------|----------|
| Genotype | 199 | 1185402954 | 5956798.8 | 14.585107 | 0.00e+00 |
| Environment | 9 | 7105461322 | 789495702.4 | 1933.065053 | 0.00e+00 |
| Genotype:Environment | 1779 | 3073244084 | 1727512.1 | 4.229780 | 0.00e+00 |
| Environment:Rep | 10 | 57746059 | 5774605.9 | 14.139012 | 0.00e+00 |
| Environment:Rep:Block | 76 | 57387089 | 755093.3 | 1.848831 | 1.72e-05 |
| Residuals | 1890 | 771907223 | 408416.5 | NA | NA |

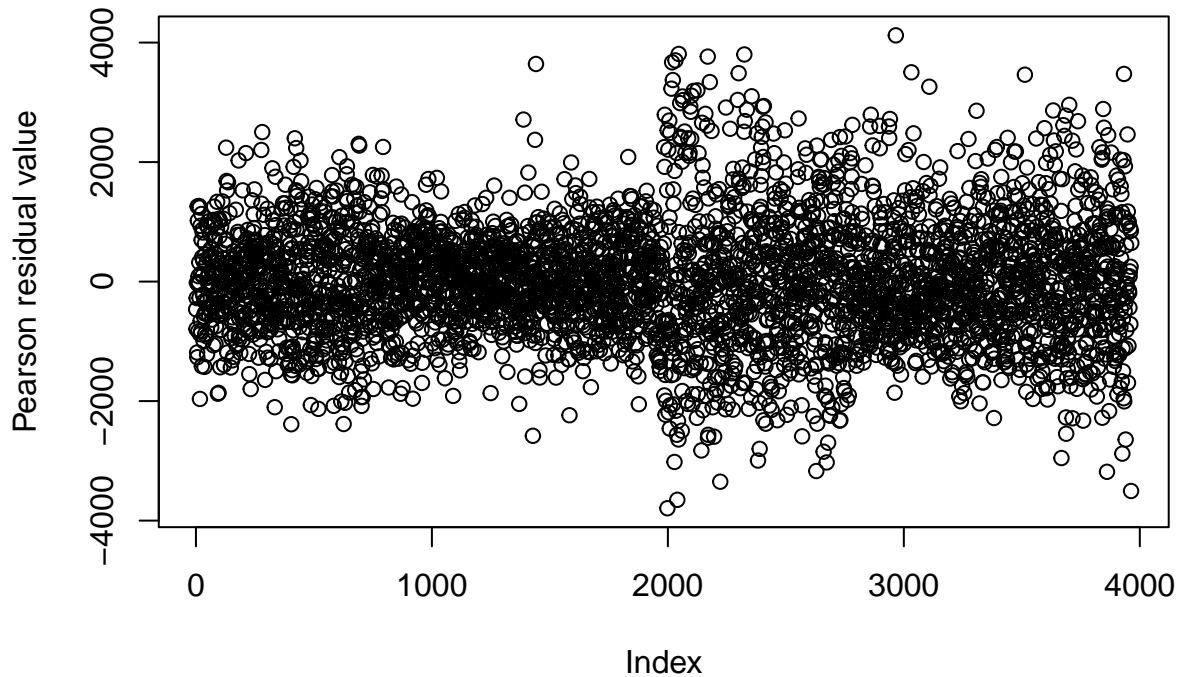
Significant differences are observed for all factors and genotype by environment interactions are significant

Check for Homogeneity of Variance

- Some test can be used to check variance between pair of environments as given below:
- More on this can be found on this: Source 1, Source 2
- Here we will check the distribution of residuals and see how they vary as we have more than two environments. For that we will run the mixed model in lme4 and then plot the residuals

```
> #
> model2<- lmer(Yield~Rep+(1|Genotype)+(1|Environment)+
+ (1|Environment:Rep)+(1|Environment:Rep:Block),
+ data=demo.data.filtered)
>
> #plot residuals
> plot(residuals(model2,type="pearson"), main='Model residuals',
+ ylab='Pearson residual value')
```

Model residuals



```
> #var.test(Yield~Environment,data=demo.data.filtered)
```

From the plot it is clear that residuals are not same and highly different

Combined Analysis in lme4

- The model we will use is give below:

$$y_{ijkl} = \mu + g_i + e_j + (ge)_{ij} + r_{jk} + b_{jkl} + \epsilon_{ijklm}$$

Where, μ = overall mean, g_i = random effect of the i th genotype, e_j = random effect of the j th environment, $(ge)_{ij}$ = is the interaction effect of i th genotypes with the j th environment, r_{jk} = fixed effect of the k th replication nested within j th environment, b_{jkl} = random effect of l th block nested with j environment and k th replication, ϵ_{ijkl} = residual error, here we assume residuals are independent.

- Mixed models are powerful tools to handle assumptions of linear model Read this one
- We will extract variance components and also calculate heritability.

```
> demo.data.filtered$Environment<-as.factor(demo.data.filtered$Environment)
> Model3.lme4<-lmer(Yield~Genotype+(1|Rep)+(1|Environment:Genotype)+
+ (1|Environment:Rep:Block), data=demo.data.filtered)
```

Summary of MET results

- In summary we will get following summarized results: 1) Description of model we used, 2) Random effects and variances, 3) Fixed effects, 4) Correlation of fixed effects

```
> summary(Model3.lme4)
```

Linear mixed model fit by REML ['lmerMod']
Formula: Yield ~ Genotype + (1 | Rep) + (1 | Environment:Genotype) + +(1 |
Environment:Rep:Block)
Data: demo.data.filtered

REML criterion at convergence: 62923.7

Scaled residuals:

| Min | 1Q | Median | 3Q | Max |
|---------|---------|---------|--------|--------|
| -3.5042 | -0.4373 | -0.0158 | 0.4092 | 4.1520 |

Random effects:

| Groups | Name | Variance | Std.Dev. |
|-----------------------|-------------|-----------|-----------|
| Environment:Genotype | (Intercept) | 6.559e+05 | 8.099e+02 |
| Environment:Rep:Block | (Intercept) | 1.859e+06 | 1.363e+03 |
| Rep | (Intercept) | 5.465e-03 | 7.393e-02 |
| Residual | | 4.086e+05 | 6.393e+02 |

Number of obs: 3964, groups:

Environment:Genotype, 1988; Environment:Rep:Block, 96; Rep, 2

Fixed effects:

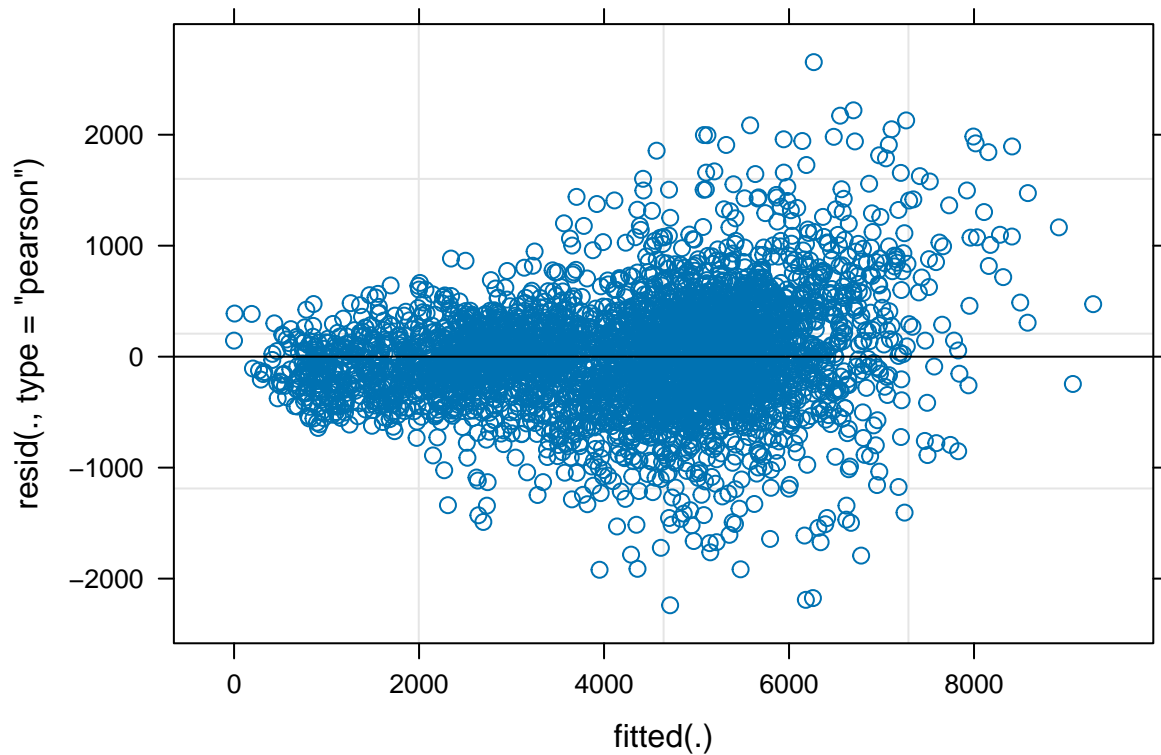
| | Estimate | Std. Error | t value |
|-------------|-----------|------------|---------|
| (Intercept) | 4006.5428 | 325.7186 | 12.301 |
| Genotype2 | -158.3061 | 418.7820 | -0.378 |
| Genotype3 | -100.7883 | 416.7684 | -0.242 |
| Genotype4 | 685.7349 | 416.6863 | 1.646 |
| Genotype5 | 395.5221 | 416.9535 | 0.949 |
| Genotype6 | 409.2635 | 415.8521 | 0.984 |
| Genotype7 | -355.5394 | 416.8936 | -0.853 |
| Genotype8 | 546.5261 | 416.4542 | 1.312 |
| Genotype9 | -480.3568 | 416.5919 | -1.153 |
| Genotype10 | -474.1254 | 418.4225 | -1.133 |
| Genotype11 | 589.1146 | 416.2162 | 1.415 |
| Genotype12 | 215.6045 | 416.2547 | 0.518 |
| Genotype13 | 49.1649 | 416.0796 | 0.118 |
| Genotype14 | 477.5898 | 416.8830 | 1.146 |
| Genotype15 | -260.8794 | 416.2345 | -0.627 |
| Genotype16 | -223.6248 | 428.3856 | -0.522 |
| Genotype17 | 241.2194 | 416.6967 | 0.579 |
| Genotype18 | 197.2838 | 416.2462 | 0.474 |
| Genotype19 | -411.0785 | 416.8845 | -0.986 |
| Genotype20 | 377.8620 | 416.5646 | 0.907 |
| Genotype21 | -26.2123 | 415.8055 | -0.063 |
| Genotype22 | 489.4758 | 416.5019 | 1.175 |
| Genotype23 | 0.6426 | 416.7124 | 0.002 |
| Genotype24 | 642.2857 | 419.0594 | 1.533 |
| Genotype25 | 304.2129 | 416.6928 | 0.730 |
| Genotype26 | -2.0851 | 416.2181 | -0.005 |
| Genotype27 | -309.2393 | 416.5684 | -0.742 |
| Genotype28 | -258.6101 | 416.7560 | -0.621 |
| Genotype29 | 165.2624 | 417.9146 | 0.395 |
| Genotype30 | 104.9037 | 415.9059 | 0.252 |
| Genotype31 | -670.4483 | 416.7135 | -1.609 |
| Genotype32 | 583.0878 | 416.5086 | 1.400 |

```
Genotype33      -14.6119    416.2335   -0.035
[ reached getOption("max.print") -- omitted 167 rows ]
```

Plot of model

- With the plot function model we will get the residuals vs fitted values

```
> plot(Model3.lme4)
```



```
> Ve<- data.frame (VarCorr(Model3.lme4))
> Ve
```

Extract the variance components

| grp | var1 | var2 | vcov | sdcor |
|-----------------------|-------------|------|--------------|--------------|
| Environment:Genotype | (Intercept) | NA | 6.559377e+05 | 809.8998098 |
| Environment:Rep:Block | (Intercept) | NA | 1.858562e+06 | 1363.2908155 |
| Rep | (Intercept) | NA | 5.465100e-03 | 0.0739264 |
| Residual | NA | NA | 4.086498e+05 | 639.2572114 |

Heritability

- Here will estimate the combined heritability based on **Cullis et al.2006**

```
> #std.err<-se.ranef(Model3.lme4)$Genotype
> #v_BLUP<- mean(std.err)
> # Heritability/Reliability
> #h2<- (1-((v_BLUP)^2/(Ve[2,4]*2)))*100
> #h2
```

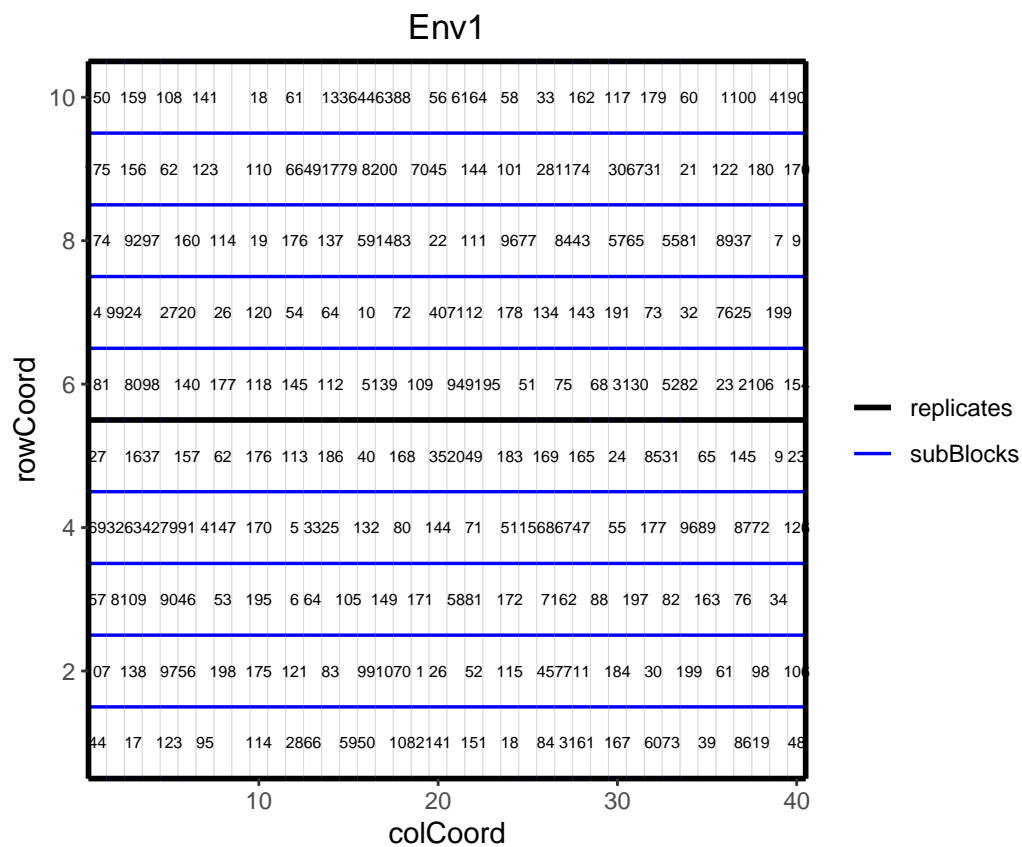
BLUEs for Random Effects

```
> # BLUEs
> BLUEs.all<-data.frame(BLUEs.Yield=fixef(Model3.lme4))
> #BLUPs<-data.frame(BLUPs.GY=coef(Model3.lme4)$Genotype[,1])
> head(BLUEs.all)
```

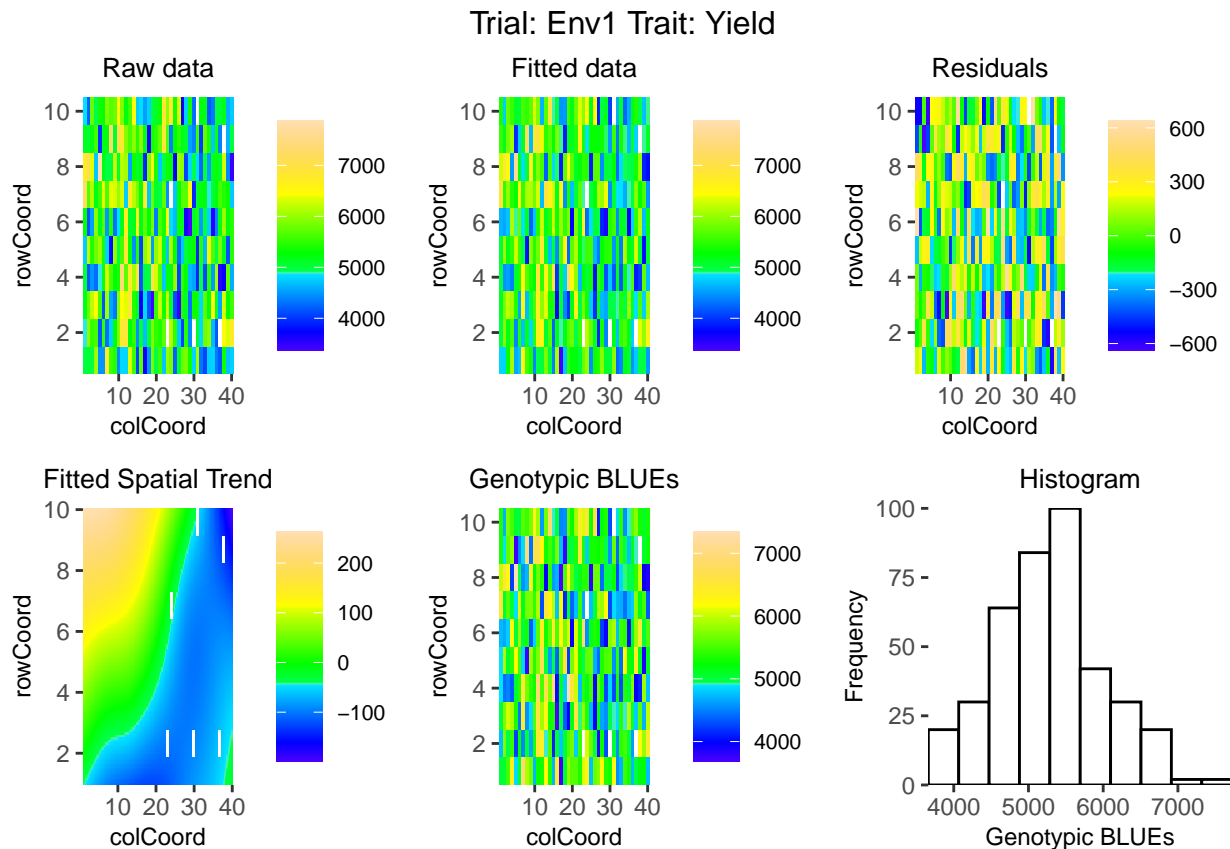
| | BLUEs.Yield |
|-------------|-------------|
| (Intercept) | 4006.5428 |
| Genotype2 | -158.3061 |
| Genotype3 | -100.7883 |
| Genotype4 | 685.7349 |
| Genotype5 | 395.5221 |
| Genotype6 | 409.2635 |

Accounting Spatial Variability

```
> library(statgenSTA)
> TD_STA <- createTD(sub.data,
+                   trial = "Environment",
+                   genotype = "Genotype",
+                   rowCoord = "Row",
+                   colCoord = "Column",
+                   repId = "Rep",
+                   subBlock = "Block",
+                   trDesign = "res.ibd")
>
> ## Create layout plot with variety labels
> plot(TD_STA,
+      plotType = "layout",
+      showGeno = TRUE)
```



```
> ## Model specification (using engine = "SpATS")
> sta_model_SpATS <- fitTD(TD = TD_STA,
+                           traits = "Yield",
+                           design = "res.ibd",
+                           what = "fixed",
+                           spatial = TRUE,
+                           engine = "SpATS")
>
> plot(sta_model_SpATS,
+       plotType = "spatial",
+       traits = 'Yield')
```

```
> ## Extract all available statistics from the fitted model.
> extr <- extractSTA(sta_model_SpATS)
> ## Extract only the BLUES from the fitted model.
> BLUES <- extractSTA(sta_model_SpATS,
+                      what = "BLUES")
```

Additional on MET and Stability Analysis

- Here in this section we are giving some useful *R* resources that can be used for stability and MET analysis.
1. metan-R: Multi-environment Trial Analysis
 2. gge-R: Functions for GGE and GGB

Additional Literature

- Screening experimental designs
- Analysis and Handling of $G \times E$ in a Practical Breeding Program
- A stage-wise approach for the analysis of multi-environment trials
- Analysis of series of variety trials with perennial crops
- A tutorial on the statistical analysis of factorial experiments with qualitative and quantitative treatment factor levels

- Experimental design matters for statistical analysis: how to handle blocking
- Random effects structure for confirmatory hypothesis testing: Keep it maximal
- Generalized linear mixed models: a practical guide for ecology and evolution
- Mixed Models Offer No Freedom from Degrees of Freedom
- Perils and pitfalls of mixed-effects regression models in biology
- A brief introduction to mixed effects modelling and multi-model inference in ecology
- Modeling Spatially Correlated and Heteroscedastic Errors in Ethiopian Maize Trials
- More, Larger, Simpler: How Comparable Are On-Farm and On-Station Trials for Cultivar Evaluation
- Rethinking the Analysis of Non-Normal Data in Plant and Soil Science
- The Design and Analysis of Long-Term Rotation Experiments
- Analysis of Combined Experiments Revisited
- Fundamentals of Experimental Design: Guidelines for Designing Successful Experiments

Note: For questions specific to data analysis shown here contact waseem.hussain@irri.org

If your experiment needs a statistician, you need a better experiment - Ernest Rutherford