STAT7400 HW10, 2017

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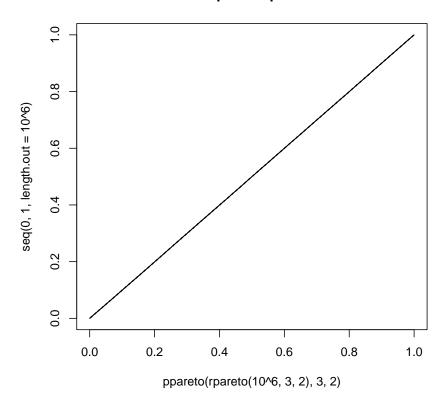
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Problem 1

(a) With runif, uniform random numbers can be generated. Then I can use qpareto to generate pareto random numbers by Inverse CDF method. Some examples of rpareto are shown below.

```
> library(pareto)
> rpareto(1, 3, -2)
[1] NaN
> rpareto(1,3,2)
[1] 71.59332
> rpareto(4,c(100,1),2)
[1] 338.870932
                 1.413489 121.032345 1.942355
> #Check reproducability
> set.seed(100)
> a <- rpareto(c(NA,1,99), 3, 2)
> set.seed(100)
> b <- rpareto(3, 3, 2)
> all.equal(a,b)
[1] TRUE
> #Check qq-plot
> qqplot(ppareto(rpareto(10^6,3,2),3,2), seq(0,1, length.out = 10^6),
         type = "1", main = "QQ plot of rpareto")
```

QQ plot of rpareto



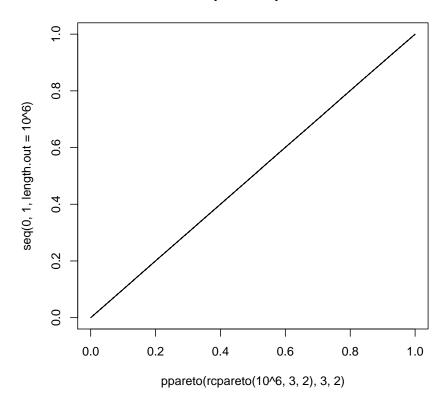
(b) With unif_rand, uniform random numbers can be generated in C. Then I can use Inverse CDF method to generate pareto random numbers. R function rcpareto is defined to call my C code through .C interface. Some examples of rcpareto are shown below.

```
> rcpareto(1,3,-2)
[1] NaN
> rcpareto(1,3,2)
[1] 4.986479
> rcpareto(4,c(100,1),2)
[1] 137.136972  1.043180 264.620436  1.031287
> #Check reproducability
> set.seed(100)
> a <- rcpareto(c(NA,1,99), 3, 2)
> set.seed(100)
```

```
> b <- rcpareto(3, 3, 2)
> all.equal(a,b)

[1] TRUE
> #Check qq-plot
> qqplot(ppareto(rcpareto(10^6,3,2),3,2), seq(0,1, length.out = 10^6),
+ type = "1", main = "QQ plot of rcpareto")
```

QQ plot of rcpareto



It is expected that C should be more efficient than R. The comparison of two functions are as follows.

```
> #Compare efficiency of two functions
> system.time(rpareto(10^6, 3, 2))

  user system elapsed
  0.125   0.004   0.131
> system.time(rcpareto(10^6, 3, 2))
  user system elapsed
  0.092   0.000   0.093
```