

Question 1

The C program *paretodnes.c* is attached in the Appendix. We use the following code to compile it.

```
gcc paratodnes.c -o paratodnes -lm -Wall -pedantic
```

In this way we have generated an executable file called *paretodnes*. Run this program, the following window will pop up. Users will enter the values of x , α and β for pareto distribution one by one.



Three sets of values are used to test it.

1. $x = 4$, $\alpha = 2$, $\beta = 3$



2. $x = 4$, $\alpha = 5$, $\beta = 3$



```
/mnt/nfs/netapp2/grad/yliu255/s7400/STAT7400/HW1/pareto
Input x:
4
Input alpha:
5
Input beta:
3
The density is 0.000000.
Process returned 0 (0x0)   execution time : 4.251 s
Press ENTER to continue.
█
```

3. $x = 4$, $\alpha = 2$, $\beta = -3$



```
/mnt/nfs/netapp2/grad/yliu255/s7400/STAT7400/HW1/pareto
Input x:
4
Input alpha:
2
Input beta:
-3
Warning message: The parameters are not meaningful! NaN produced!
The density is nan.
Process returned 0 (0x0)   execution time : 3.717 s
Press ENTER to continue.
█
```

Question 2

The R program *dpareto.r* is as follows.

```
dpareto <- function(x,alpha,beta){  
  
  #Calculate the maximum length of inputs  
  L <- max(length(x), length(alpha), length(beta))  
  
  #Align all the inputs  
  x <- rep(x,length.out = L)  
  alpha <- rep(alpha,length.out = L)  
  beta <- rep(beta,length.out = L)  
  
  #Initialize the densities with NaN  
  dens <- rep(NaN, length.out = L)  
  
  for (i in 1:L){  
    if (alpha[i] <= 0 || beta[i] <= 0){  
      warning("NaNs produced")  
      next  
    } else if (x[i] < alpha[i]){  
      dens[i] <- 0  
    } else{  
      dens[i] <- beta[i]*alpha[i]^beta[i]/x[i]^(beta[i]+1)  
    }  
  }  
  return(dens)  
}
```

I use the following set of values to test it.

- $x = c(4,4,4)$
- $\alpha = c(2,5,2)$
- $\beta = c(3,3,-3)$

The results are as follows.

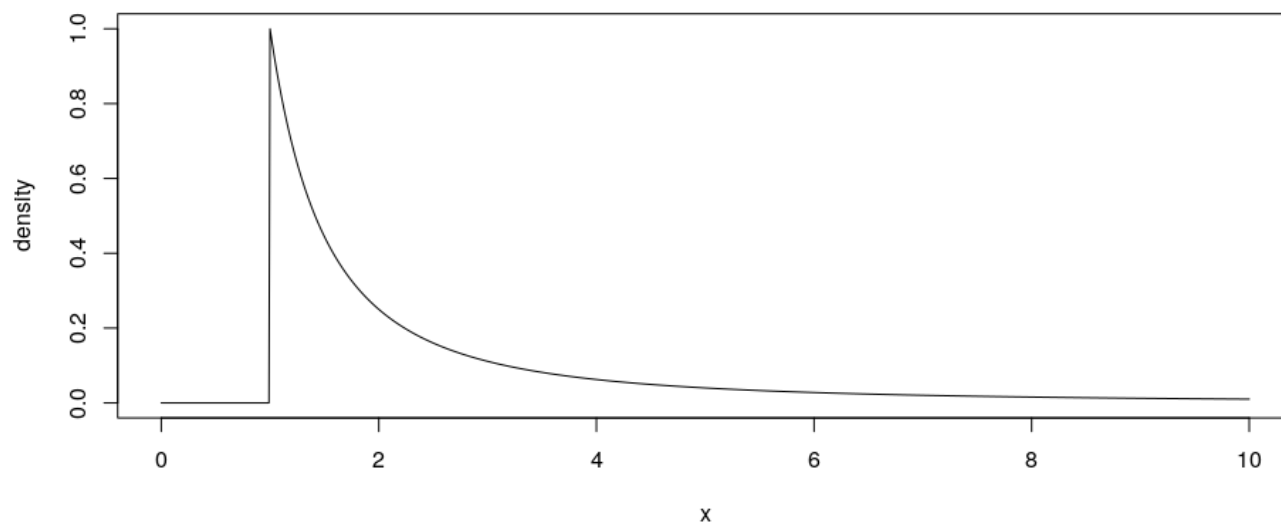
```
> dpareto(c(4,4,4),c(2,5,2),c(3,3,-3))  
[1] 0.09375 0.00000      NaN
```

Warning message:

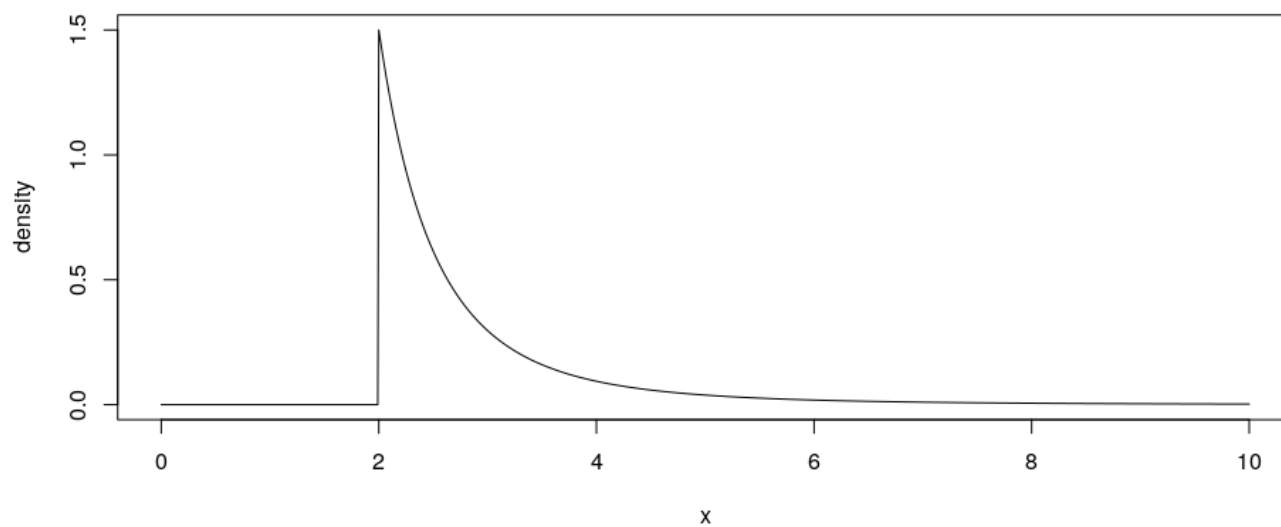
```
In dpareto(c(4, 4, 4), c(2, 5, 2), c(3, 3, -3)) : NaNs produced
```

Then I use this function to plot the density in R. Two sets of parameters are used.

1. $\alpha = 1$, $\beta = 1$



2. $\alpha = 2$, $\beta = 3$



Appendix

paretodens.c

```
#include <stdio.h>
#include <math.h>

/*Define parto density function*/
double paratodens(double x, double alpha, double beta) {
    /*Check whether alpha and beta are positive*/
    if (alpha <= 0 || beta <= 0){
        printf("Warning message: The parameters are not meaningful! NaN
produced!\n");
        return NAN;
    }
    /*Check whether x is greater than alpha*/
    else if (x < alpha){
        return 0;
    }
    else {
        return beta*pow(alpha,beta)/pow(x,beta+1);
    }
}

int main() {
    double x,alpha,beta;

    printf("Input x:\n");
    scanf("%lf",&x);

    printf("Input alpha:\n");
    scanf("%lf",&alpha);

    printf("Input beta:\n");
    scanf("%lf",&beta);

    printf("The density is %lf.\n", paratodens(x,alpha,beta));
    return 0;
}
```