

# Linear Programming

Harder AMPL example  
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# Harder example: bits and bobs

- A company produces two products, bits and bobs.
- Bits take 7 hours to make and bobs take 16.25 hours to make.
- Monthly demand:

Demand	June	July
Bits	40	20
Bobs	24	56



# Harder example: bits and bobs

- A company produces two products, bits and bobs.
- Bits take 7 hours to make and bobs take 16.25 hours to make.
- Monthly demand:
- Products can be stored from month to month at a cost of \$20/bit, \$24/bob
- There are two different work-modes available: normal and overtime.
- Hours available and wage rate for the workmodes:

Demand	June	July
Bits	40	20
Bobs	24	56

Work-mode	Hours available	Wage rate ( \$ per hour)
Normal	1400	8
Overtime	440	12

# AMPL implementation

## Sets

$P$  PRODS

$T$  TIME

$W$  MODES

## Parameters

$d_{p,t}$  demand

$a_m$  hrs\_avail

$r_p$  hrs\_req

$c_p$  store\_cost

$k_m$  hrly\_pay

## Variables

$x_{p,t}$  produce

$s_{p,t}$  store

$h_{m,t}$  hrs\_paid

# AMPL implementation

## Declaring 2-dimensional parameters and variables

```
param demand{PRODS, TIME};
```

## Writing the objective function

```
minimize TotalCost:  sum{p in PRODS, t in TIME} store_cost[p] * store[p, t]  
                    + sum{m in MODES, t in TIME} hrly_pay[m] * hrs_paid[m, t];
```

# AMPL implementation

## Writing the constraints

```
SatisfyDemand {t in TIME diff {1}, p in PRODS}:  
produce [p, t] + store [p, t-1] - store [p, t] >= demand [p, t];
```

or...

```
SatisfyDemand: {t in TIME: t > 1, p in PROD}  
produce [p, t] + store [p, t-1] - store [p, t] >= demand [p, t];
```

# AMPL implementation

## Set operations in AMPL

Union:

Intersection:

Complement:

Symmetric difference:

```
A union B
```

```
A inter B
```

```
A diff B
```

```
A symdiff B
```

# AMPL implementation

Entering data for 2-dimensional parameters

```
param demand:          1    2 :=  
                        bits 40  20  
                        bobs 24  56;
```