(a) Original Objective max 4x1+572-3x3

=> min -4x1-5x2+3x3

S.t.
$$\gamma_1+2\gamma_2+3\gamma_3$$
 = 10

$$x_1 - x_2 = 6$$

$$x_1 + 3x_2 + x_3 + x_5 = 14$$

71,---7530

Gincl constrain 1. already meet the standard formation I, we don't need to introduce a macessary slack varaible into the system, because the coefficients of the slack varriable are not a identical matrix, it's necessary to introduce artifical variables in to the system, which are Xt, X7, X8.

PHASE I min -4x1-5x2+3x3 =>min x6+x7+x5-

Si 71+272+73+ +76 =10

 $\chi_1 - \chi_2 - \chi_4 + \chi_7 = 6$

X	1 +	3X2-)		+ X	5			=	14
×0		x1	x2	жЗ	×4	ж5	×6	×7	RHS	
	1		0	0					0	
	0	1	- 2	1				0	10	
	0	1	2	1 0	-1	0	0	1	6	
	0	1			0	1	0	0	14	
			_	_		_	_	_		
×0		×1	×2	ж3	×4	x5	ж6	я7	RHS	
	1	3				_	_		30	
	0	1	2	1		_	1	_	10	
	0	1				_			6	
-	0	1	3	1	0	1	0	0	14	
×0		×1	x2	x 3	×4	×5	×6	×7	RHS	
	1	1.6667			-1		0			
	0	0.3333			0		1			
	0	1.3333		0.3333			0	1		
	0	0.3333		<mark>1</mark> 0.3333						
_			_							
×0		x1	×2	×3	×4	x5	×6	×7	RHS	
	1	0				2	-5 3 -4 -1	0	8	
	0	1		•			3	0	2	
	0	0		•		3	-4	1		
-	0	0		1 0	0	1	-1	0	4	
×0		×1	x2	×3	×4	ж5	×6	87	RHS	
-	1	0		-0.333	-0.333	0	-2.333		2.6667	
	0	1		0.3333		_			7.3333	
_	0	ó	-							
	0	0		0.3333					1.3333	

be have the BFS, (X1, X2, X5

PHASE LI

min - 4x1 - 5x2 +3x3

×0		×1		×2	я3	×4	×5	RHS		
	1		4	5	-3	0	0	0		
	0		1	0	0.3333	-0.667	0	7.3333		
	0		0	0	-0.333	-0.333	1	2.6667		
-	0		0	1	0.3333	0.3333	0	1.3333		
×0		×1		×2	x3	×4	x5	RHS		
	1		0	0	-6	1	0	-36		
	0		1	0	0.3333	-0.667	0	7.3333		
	0		0	0	-0.333	-0.333	1	2.6667		
	0		0	1	0.3333	0.3333	0	1.3333		
×0		×1		×2	×3	×4	x5	RHS		
	1		0	-3	-7	0	0	-40		
	0		1	2	1	0	0	10		
	0		0	1	0	0	1	4		
	0		0	3	1	1	0	4		

Since all the coefficences of Ro are ≤ 0 , which indicates that with the variable increase the objective value will increase, 80 the original objective will drop, 50 we got the optional solution where $(\chi_1, \chi_2, \chi_3) = (10, 0, 0)$, 80 the max value of objective function is 40

(b) Big-M simply method.

max 4x1+5x2-3x3

- =) min -4x,-5x2+3x3
- => min -4x,-5x,+3x3 MX6 Mx7

 $5.t. \quad \gamma_1 + 2\gamma_2 + \gamma_3 \qquad + M\gamma_6 \qquad = 10$

 $\gamma_1 - \gamma_2 - \gamma_4 + M_{\gamma_7} = 6$

 $\chi_1 + 3\chi_2 + \chi_3 + \chi_5 = 14$

×0							×7		
		5		0				0	
0		_		_	_	-			
0			_		_	_		_	
0	1	3	1	0	1	0	0	14	
×0	x1			×4			×7		
	204			-100				1600	
	1			0				10	
0					_	_		_	
0	1	3	1	0	1	0	0	14	
×0	x1			×4					
	169		62		-35			1110	
1	0.3333			0				0.6667	
	1.3333		0.3333		0.3333			10.667	
0	0.3333	1	0.3333	0	0.3333	0	0	4.6667	
				×4					
			-107					772	
0				0	-2	3		2	
0	_	_	-		_		-	8	
0	0	1	0	0	1	-1	0	4	
×0	x1	x2		×4					
				1				-36	
0	1			-0.667					
0	_	0	-0.333	-0.333	1	-1.333	0.3333	2.6667	
0	0	1	0.3333	0.3333	0	0.3333	-0.333	1.3333	
×0	x1	x2	ж3	×4	ж5	×6	×7	RHS	
	_	-3	-7			-104	-100	-40	
0	1	2	1	0	0	1	0	10	
0	0	1		_	1	-1	0	4	
0	0	3	1	1	0	1	-1	4	

Since ···· C Same as two-phase) -----

SD the last tableau give the optional solution, $(X_1, X_2, X_3) = (10, 0, 0)$, and the max value of the objective function is (40.)

Question II

(a)	0	1	1	2	2		4		e	7	DNG	
V = V	ж0	X1		x2	хЗ	44	x4	x5	ж6	×7	RHS	
	-	0	0	53		41						0
		0	_ '	-11		-5	18					0
		0	0	4		2	-8				<u>'</u>	0
	-	0	0	11		5	-18	-2	0		l .	1
				_	_			_	_			
	×0	×1		ж2	хЗ		×4	x5	×6	×7	RHS	
		1	0			14.5	-98					0
		0	1	0		0.5						0
		0	0	1		0.5	-2					0
		0	0	0		-0.5	4	0.75	-2.75		1	1
	ж0	×1		ж2	хЗ		×4	х5	x6	87	RHS	
		1	-29	0		0)	0
		0	2	0		1	-8		5.5	()	0
		0	-1	1		0	2	0.5	-2.5	0)	0
		0	1	0		0	0	0	0		1	1
	ж0	×1	1	x2	хЗ		×4	ж5	x6	×7	RHS	
		1	-20	-9		0	0	10.5	-70.5	0)	0
		0	-2	4		1	0	0.5	-4.5	- 0)	0
		0	-0.5	0.5		0	1	0.25	-1.25	()	0
		0	1	0		0	0	0			1	1
	_											
	ж0	×1	1	x2	x3		×4	ж5	×6	×7	RHS	
	_	1	22	-93		-21	0					0
		0	-4	8		2	0		-9			0
		0	0.5			-0.5				ı d		0
		0	1	0		0.0			Name and the same		1	1
		-				Ŭ	J					
	×0	×1	1	×2	κЗ		×4	×5	ж6	×7	RHS	
	100	1	7.5			-6.5						0
	_	0	0.5			-2.5		1	0			0
		0	0.5			-0.5	1	o				0
		0	0.0	0		0.0		ő			<u>. </u>	1
		•									•	1
	×0	×1	1	×2	x3		×4	ж5	×6	×7	RHS	
	70	1	0			31						0
		0	- 1	-11		-5	18	-13	-3 0	· (0
		0	ď			-0	-8		1			0
		0	0			2 5	-o -18	-1	o		<mark></mark>	1
	_	U	U	- 11		Э	-10	-2	U		<u>'</u>	
	0			2	2		4		0	7	DNG	
	×0	X1 		x2	хЗ		×4	x5	x6	×7	RHS	
		0	0			14.5						0
		0		0	<u> </u>	0.5	-4	-0.75				0
		0	0	1		0.5		-0.25		C		0
	-	0	0	0		-0.5	4	0.75	-2.75		1	1 we can see that
		1			_			_		_	E1.15	the matrix is
	×0	×1		x2	хЗ			x5	×6	×7	RHS	the same when
		1	-29	0		0		15		0	J	ue do ord pivot
		0	-29 2 -1	0		1	-8 ><2	-1.5	5.5	0)	the nation is the same when we do ord pivot to their pivot rule nould cause cyding
		0	-1	1 0		Q			-2.5	C)	1 would cause cyding
		0	1	0		0	0	0	0		1	1



