

Note: how to build an AVL tree

1. Insert():

use `AvlNode<AnyTpye> insert(val)` instead of return void, because if root = null, need to return new root. For the same reason, when recursively call insert(), don't forget: `t.left = insert(val, t.left)`.

if(t == null) return new AvlNode<>(x, null, null); to create new node.

don't forget to `return balance(t)` instead of t at last, reason see `Balance()`

2. Remove():

As well `AvlNode<AnyTpye> remove(val)` is necessary, because the root could be removed, need to return new root. For the same reason, when search node, don't forget `t.left = remove(val, t.left)`.

When find the node, there are two condition: (1) both `t.left & t.right != null` (2) at least one of them is null.

don't forget to `return balance(t)` instead of t at last, reason see `Balance()`

3. Balance():

if (right side higher), use `height(t.right.right) >= height(t.right.left)` will NOT cause `OUTBOUNDEXCEPTION`, because right side higher, `t.right != null`.

if not balanced, call `t = rotate/doubleWithLeft/RightChild(t)` to update t.

don't forget to add: `t.height = Math.max(height(t.left), height(t.right)) + 1;`

How do we know every node's height? Because every time call `insert(t)`, `insert(t)` will call `insert(t.left/right)`, and `insert(t.left/right)` will call `balance(t.left/right)`, and `balance` will set the height from the bottom to top, update all the ancient nodes.

`null node's height = -1`

4. Contains():

simple one, use a `while(t != null)` to check.

5. printTree():

simple one, if (t != null){ use any of pre/in/post order}.

6. rotateWithLeftChild():

when it is called, it is like: `t = rotate/doubleWithLeft/RightChild(t)`. So don't have to use the pre.t to point t, because, just return new t is fine.

don't forget to update two nodes: (other node below t and t.left will not be changed, node above will be updated in outer balance())

```
t.height = Math.max( height( k1.left ), height( k1.right ) ) + 1;
```

```
t.left.height = Math.max( height( k2.right ), k1.height ) + 1;
```

7. doubleWithLeftChild():

A little tricky that call rotateWithLeftChild() twice, remember rotate left child first, then parent node. It is like:

```
t.left = rotateWithRightChild( t.left );
```

```
return rotateWithLeftChild( t );
```