$Males_HW1$

18.6/20

Score: 18.8 / 20

Late submission (1 hour late): -1%

Time stamp: 12/04/24 19:44

1 Homework 1:

1.0.1 Deadline: Thursday 11 April 2024 (by 19h00)

1.0.2 Credits: 20 points

2 Name: Males-Araujo Yorlan

2.0.1 1. (7 points) Orbital dynamics

This problem consists of computing and displaying the orbits of Mars' moons (Phobos and Deimos) around Mars and the Sun:

- Phobos has an orbital period of $T_{phobos} = 7.65$ hours around Mars and is located at a distance of 5.99×10^3 km from Mars.
- Deimos has an orbital period $T_{deimos} = 30.30$ hours around Mars and is located at a distance of 2.35×10^4 km from Mars.

For simplicity, we can assume that all the orbits are circular. Thus, the Mars' orbit around the Sun is described by the following parametric equations:

$$x_{mars} = R \cos(\omega_{mars} t)$$

$$y_{mars} = R \sin(\omega_{mars} t)$$

where $R=2.1\times 10^8\,\mathrm{km}$ is the Sun-Mars distance, $\omega_{mars}=2\pi/T_{mars}$, and $T_{mars}=687\,\mathrm{days}$.

Similarly, the orbits of each moon (i) is the sum of its position relative to Mars and the position of Mars relative to the Sun (which is at the origin), so:

$$x_i = x_{mars} + r_i \cos(\omega_i t)$$

$$y_i = y_{mars} + r_i \sin(\omega_i t)$$

where i refers to either Phobos and Deimos, r_i to their distances from Mars, and $\omega_i = 2\pi/T_i$ refers to their respective angular frequencies.

(a) Create a python function that takes the period (T) as argument and returns the angular frequency (ω) of any body.

```
[1]: # Importing the libraries:
   import numpy as np
   import pandas as pd
   import matplotlib.pyplot as plt
   import scipy.optimize as opt
   from astropy.io import fits
   import skimage
   from skimage.feature import peak_local_max
```

C:\Users\DELL\anaconda3\Lib\site-packages\paramiko\transport.py:219: CryptographyDeprecationWarning: Blowfish has been deprecated and will be removed in a future release

"class": algorithms.Blowfish,

```
[2]: # Function:
    def angular_freq(T):
        """
            Computes the angular frequency of any body.
            Input: T -> Period
            Ouput: omega -> Angular frequency.
            Author: MAY.
            Date: 04/04/2024
            """
            # We simply use the well-known relation.
            # (Specific units depend on the input).
            omega = 2*np.pi/T
            return omega
```

(b) Then, call your function in (a) and assign to three global python variables the angular frequencies of: i) Mars while orbiting around the Sun, (ii) Phobos, and (iii) Deimos orbiting around Mars.

```
[3]: # We will work with the time in days. So,

t_mars = 687*24*60 # minutes
t_phobos = 7.65*60 # minutes
t_deimos = 30.30*60 # minutes

# Now we call our function to get the respective angular frequencies:

ang_mars = angular_freq(t_mars) # minutes^(-1)
ang_phobos = angular_freq(t_phobos) # minutes^(-1)
ang_deimos = angular_freq(t_deimos) # minutes^(-1)

# And put the last two in an array because it might be useful later:
ang_moons = np.array([ang_phobos, ang_deimos])
```

(c) Create a vector for time, t, that spans from 0 to 687 days, and define R and r_i as global variables.

```
[4]: # Creating the time vector:
t = np.arange(0,687*24*60+1,1) # minutes

# Now R and r_i:
R = 2.1e8 #km
r_moons = np.array([5.99e3, 2.35e4]) #km (with [0] being Phobos, and [1] Deimos)
```

(d) Create a python function that takes R, r_i , t as arguments and returns x_i and y_i for either Phobos or Deimos.

```
[5]: # Function:
     def parametric_eqs(R, r_moons, t):
         n n n
         Gets the parametric values for circular orbits
         of a planet and two of its moons. All around the sun.
         Inputs: R -> radius of the planet's orbit
                 r_moons -> radii of the two moons around the planet
                 t -> time vector
         Outputs: All the 6 orbits around the sun.
         Author: MAY.
         Date: 04/04/2024
         # We define the parametrizations for Mars:
         x_mars = R*np.cos(ang_mars*t)
         y_mars = R*np.sin(ang_mars*t)
         # And then we do it for each moon:
         x_phobos = x_mars + r_moons[0]*np.cos(ang_moons[0]*t)
         y_phobos = y_mars + r_moons[0]*np.sin(ang_moons[0]*t)
         x_deimos = x_mars + r_moons[1]*np.cos(ang_moons[1]*t)
         y_deimos = y_mars + r_moons[1]*np.sin(ang_moons[1]*t)
         return x_mars, y_mars, x_phobos, y_phobos, x_deimos, y_deimos
```

(e) Then, call your function in (d), retrieve x_i and y_i , and save them into a CSV file with 7 columns: t, x_{mars} , y_{mars} , x_{phobos} , y_{phobos} , x_{deimos} , y_{deimos} .

```
"x_deimos [km]": x_deimos, "y_deimos [km]": y_deimos},

index=None)

# And , second, a csv file:

df_orbits.to_csv("orbits.csv", ",", float_format = "{:.4e}".format)
```

I'm aware there might be better ways of doing it without having to call each one, but it works.

(f) Make a 2D Cartesian plot, with the Sun in the origin, showing the orbits of Mars, Phobos, and Deimos around the Sun for a full Martian year. Which orbit is more intricate?

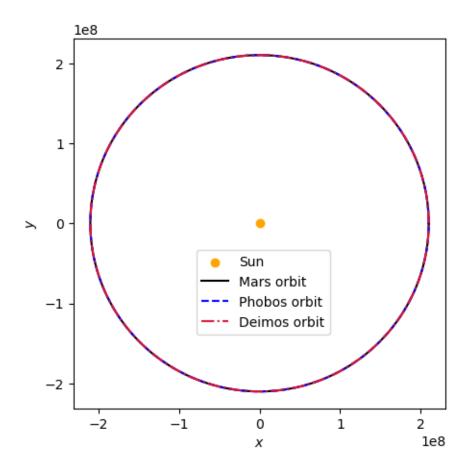
```
[7]: # Plotting:
    plt.figure(figsize=(5,5))

    plt.scatter(0, 0, marker = "o", color="orange", label="Sun")

plt.plot(x_mars, y_mars, color="k" , label="Mars orbit")
    plt.plot(x_phobos, y_phobos, linestyle="--", color="b", label = "Phobos orbit")
    plt.plot(x_deimos, y_deimos, linestyle="--", color="crimson", label = "Deimos_u")
    orbit")

plt.xlabel(r"$x$")
    plt.ylabel(r"$y$")

plt.legend(loc=(0.33,0.20))
    plt.show()
    plt.close()
```



The Sun and Mars orbit are as expected, and I think the problem with the other two orbits is that the radius of the Mars orbit is very large in comparison with the other two.

Zooming in might let us see.

```
[8]: # Plotting: Zoomed image.
plt.figure(figsize=(6,6))

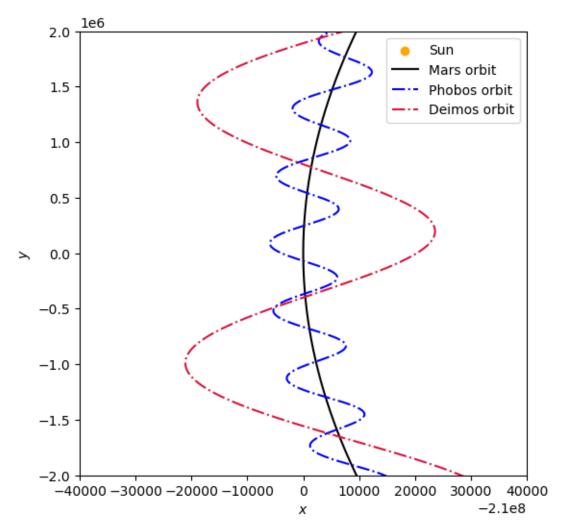
plt.scatter(0, 0, marker = "o", color="orange", label="Sun")

plt.plot(x_mars, y_mars, color="k" , label="Mars orbit")
plt.plot(x_phobos, y_phobos, linestyle="-.", color="b", label = "Phobos orbit")
plt.plot(x_deimos, y_deimos, linestyle="-.", color="crimson", label = "Deimos_\_\text{\text{\text{orbit}"}})

plt.xlabel(r"$x$")
plt.xlabel(r"$y$")

plt.ylabel(r"$y$")
```

```
plt.legend(loc="best")
plt.show()
plt.close()
```

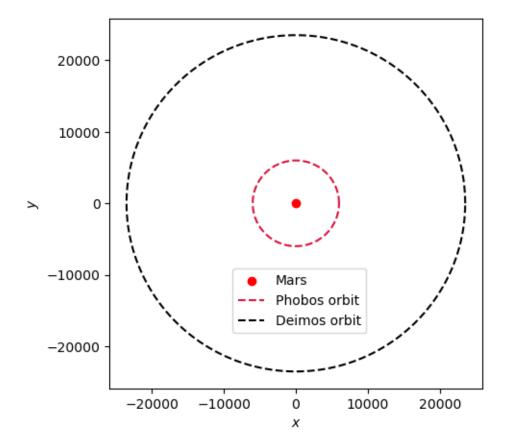


That allowed us to see the orbits of the moons. With this, we can conclude that it is the Phobos orbit the one that is more intricate since it varies more than the other two.

(g) Make a 2D Cartesian plot, with Mars in the origin, showing the orbits of Phobos and Deimos around it for a full Deimos period. We only need to plot the parametrizations of both moons subtracting the Mars' orbit values from them.

```
[9]: # It's done as follows:
    x_phobos_mars = x_phobos - x_mars
    y_phobos_mars = y_phobos - y_mars
```

```
x_deimos_mars = x_deimos - x_mars
y_deimos_mars = y_deimos - y_mars
```



/ Seems good, but it didn't, at first, because I was making the mistake of overlapping many orbits. That's why I sliced the elements of the arrays to get only one complete orbit for each.

2.0.2 2. (7 points) Spectral fitting

This problem consists of fitting spectral lines and finding the relative velocities between multiple Gaussian components (interstellar gas clouds).

The supplied data file:

 $https://github.com/wbandabarragan/computational-physics-1/tree/main/sample-data/j074814-7435 \ gass \ spectra.dat$

contains observational data from the Parkes radio telescope (see https://en.wikipedia.org/wiki/Parkes Observatory).

The data corresponds to HI clouds in the Chamaeleon molecular cloud complex (see https://en.wikipedia.org/wiki/Chamaeleon_complex).

This data file contains emission line features from neutral hydrogen (HI, i.e., $\lambda = 21\,\mathrm{cm}$) in the Milky Way. The second column has gas velocities (in km s⁻¹) and the third column emission intensity (called brightness temperature in K). We can assume that each gas cloud in our line of sight produces a Gaussian emission feature that is only dependent on the column density if the gas is optically thin.

Carry out the following calculations using python:

(a) Create a python function that reads in the spectral data (velocity and intensity) from the file, and returns them as arrays. Hint: You need to jump over the header of the data file.

```
[11]: # Having inspecting the data, we define the function:

def spectral_data(filename):
    """
    Reads in a file with information on spectral fitting
    and gets two arrays: one for velocities and the other
    with intensity. It skips the header.
    Input: filename -> variable storing the file
    Outputs: velocity -> np.array with the velocities
        intensity -> np.arrat with the intensities
    Author: MAY
    Date: 05/04/2024
    """

# We read in the file (skipping the header).

file = pd.read_csv(filename, sep = "\s+", comment ="#", header = None)

# Then we get the corresponding arrays via indexing:
```

```
velocity = np.array(file[1])
intensity = np.array(file[2])
return velocity, intensity
```

```
[12]: # We call and use the function:
    spectra = "data/j074814-7435_gass_spectra.dat"

velocity, intensity = spectral_data(spectra)
```

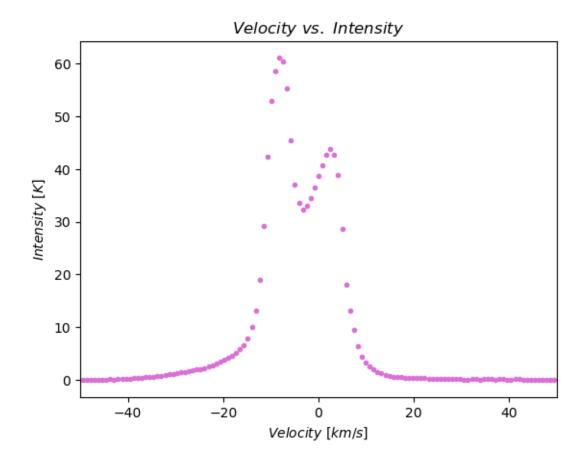
(b) Make a high-quality, labeled plot of the spectrum (velocity on the x-axis and intensity on the y-axis). How many "HI clouds" do you see? Note that each Gaussian-like feature represents a separate HI cloud.

```
[13]: # We simply plot:
    plt.figure()

    plt.scatter(velocity, intensity, marker = ".", color="orchid")

/ plt.title(r"$Velocity\ vs.\ Intensity$")
    plt.xlabel(r"$Velocity\ [km/s]$")
    plt.ylabel(r"$Intensity\ [K]$")

plt.xlim(-50,50)
    plt.show()
    plt.close()
```



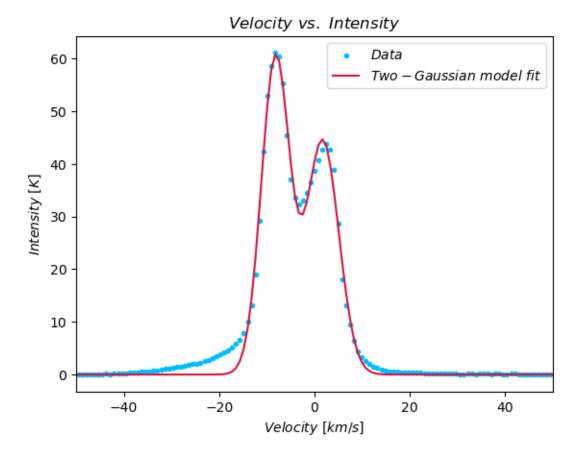
✓ Evidently, there are two Gaussian-like features, that is, two HI clouds.

(c) Define an appropriate multi-Gaussian model for the spectrum and create a python function for it. The model we'll use is a two-Gaussian one given by

$$\phi(x) = a e^{-b(x+c)^2} + d e^{-f(x+g)^2}$$

where a, b, c, d, f and g are constants to be determined.

```
# We get the equation:
          phi = a*np.exp(-b*(x + c)**2) + d*np.exp(-f*(x + g)**2)
          return phi
     (d) Fit your model to the spectrum, and report the best-fit values for the free param-
     eters with their respective uncertainties.
[15]: # We'll use curve_fit() function as we need to report uncertainties.
      coef, cova = opt.curve_fit(two_gauss, velocity, intensity)
     C:\Users\DELL\AppData\Local\Temp\ipykernel_8724\411450246.py:14: RuntimeWarning:
     overflow encountered in exp
       phi = a*np.exp(-b*(x + c)**2) + d*np.exp(-f*(x + g)**2)
     C:\Users\DELL\AppData\Local\Temp\ipykernel_8724\411450246.py:14: RuntimeWarning:
     overflow encountered in multiply
       phi = a*np.exp(-b*(x + c)**2) + d*np.exp(-f*(x + g)**2)
[16]: # Fittings
      two_gaussian_fit = two_gauss(velocity, *coef)
[17]: # Reporting the uncertainties of the coefficients (1-sigma).
      two_gauss_unc = np.sqrt(np.diag(cova))
      print("Parameters estimates with uncertainties:")
      print("\n")
      print("a =", coef[0], "±", two_gauss_unc[0])
      print("b =", coef[1], "±", two_gauss_unc[1])
      print("c =", coef[2], "±", two_gauss_unc[2])
      print("d =", coef[3], "±", two_gauss_unc[3])
      print("f =", coef[4], "±", two_gauss_unc[4])
      print("g =", coef[5], "±", two_gauss_unc[5])
     Parameters estimates with uncertainties:
     a = 60.2276464222906 \pm 0.2524921395168533
     b = 0.05628464743562763 \pm 0.0007756801031673931
     c = 8.173393127001168 \pm 0.020972903285341293
     d = 44.427479083888876 \pm 0.23836504397539193
     f = 0.043754005317697416 \pm 0.0008012427860561296
     g = -1.7039854945794364 \pm 0.030209809971325146
[18]: # Plotting everything together.
      plt.figure()
      plt.scatter(velocity, intensity, marker =".", color="deepskyblue", __
       →label=r"$Data$")
```



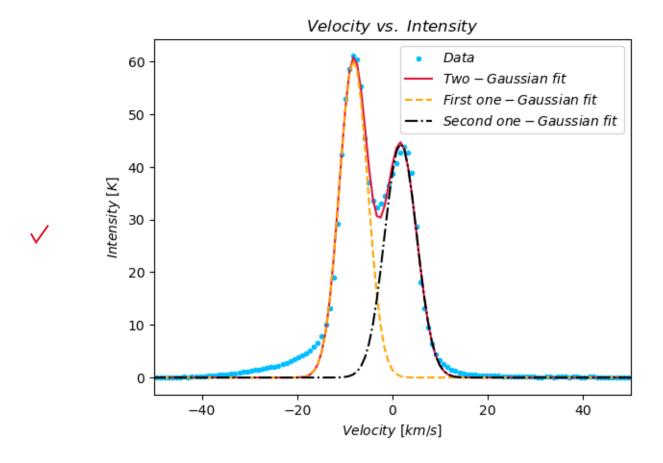
It looks fine.

(e) Make a high-quality, labeled plot that shows the original spectrum, the overall multi-Gaussian fit, and also each individual Gaussian component. We need a one-Gaussian model where we use the parameters obtained just now. Its expression is

```
\phi(x) = a e^{-b(x+c)^2}.
```

```
[19]: # Function for the one-Gaussian model:
      def one_gaussian(x, a, b, c):
          Defines a one-Gaussian model for the regression.
          Inputs: x -> velocity vector,
                  a -> the height of the Gaussian
                  b -> the width ""
                  c -> displacement ""
          Output: y \rightarrow 1D one-Gaussian model
          # The expression
          phi = a*np.exp(-b*(x + c)**2)
          return phi
[20]: # Now we get the two individual Gaussians:
      one_gaussian_1 = one_gaussian(velocity, coef[0], coef[1], coef[2])
      one_gaussian_2 = one_gaussian(velocity, coef[3], coef[4], coef[5])
[21]: # And plot:
      plt.figure()
      plt.scatter(velocity, intensity, marker =".", color="deepskyblue", __
      →label=r"$Data$")
      plt.plot(velocity, two_gaussian_fit, color="crimson", label=r"$Two-Gaussian\⊔
      ⇔fit$")
      plt.plot(velocity, one_gaussian_1, linestyle = "--", color ="orange",
               label=r"$First\ one-Gaussian\ fit$")
      plt.plot(velocity, one_gaussian_2, linestyle = "-.", color ="k",
              label=r"$Second\ one-Gaussian\ fit$")
      plt.title(r"$Velocity\ vs.\ Intensity$")
      plt.xlabel(r"$Velocity\ [km/s]$")
      plt.ylabel(r"$Intensity\ [K]$")
      plt.xlim(-50,50)
      plt.legend(loc="best")
      plt.show()
```





It seems to fit.

(f) Find the (velocity, intensity) coordinates of the maximum of each Gaussian component. Note: the velocity coordinates of the maxima are called central velocities. Both points are given by the coefficients found. Velocities are given by the displacements and intensities by the heights.

The coordinates of the maximum in the first Gaussian component is (8.173393127001168, 60.2276464222906).

The coordinates of the maximum in the second Gaussian component is (-1.7039854945794364, 44.427479083888876).

They seem to strongly agree with the plot.

-0.5 The sign of the velocities is swapped.

(g) Use the coordinates of the maxima computed in (f) to compare the central velocities of the clouds, and calculate the relative velocity between the clouds. We just use the classical addition of velocities. The difference in their velocities tells us which one has a higher kinetic energy and temperature.

```
[23]: print(f"The relative velocity between the HI clouds is {abs(coef[5]-coef[2])} km/

→s.")
```

 \checkmark

The relative velocity between the HI clouds is 9.877378621580604 km/s.

2.0.3 3. (6 points) Distance between galaxies

The purpose of this exercise is to isolate features (galaxies) in an image by analysing the pixel information. The sample data correspond to NGC 1512 and its companion the dwarf galaxy NGC 1510 (see https://en.wikipedia.org/wiki/NGC 1512).

The provided data file:

https://github.com/wbandabarragan/computational-physics-1/tree/main/sample-data/skvNGC~1512.fits

contains optical images of the two galaxies from NASA's HEARSARC website (https://skyview.gsfc.nasa.gov/current/cgi/titlepage.pl). The FITS file contains an image in blue colour taken from the 2nd Digitized Sky Survey (DSS2 Blue).

Carry out the following analysis:

(a) Create a python function that reads in the data from the FITS file, and returns two objects: the image itself as a 2D array, and the value of the header key called "CDELT2", which reports the size of a pixel in degrees. Let's first take a look at the data:

[False True]

```
[25]: # Cheking the header to see the value of "CDELT2": # print(galaxies_header)
```

```
[26]: # Now we are ready to define the asked function:

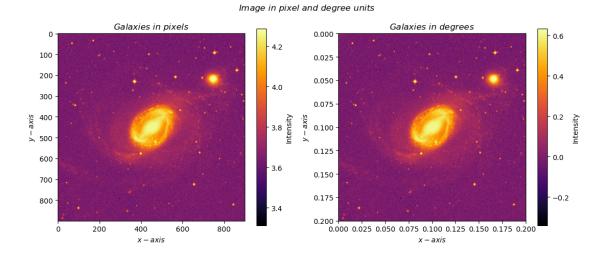
def data_fits(filename):
    """

    Given a .fits file, returns two variables
    with the data without the head, and the pixel size.
    Input: filename -> variable storing the fits image
```

(b) Call your function in (a), and make a two-panel figure with high-quality, labeled plots of the image in pixel units and in degree units. Hint: Use the value of "CDELT2" for unit conversion.

```
[27]: # Calling the function:
        image_file = "/Users/DELL/Documents/Physics/CompPhysI/data/skvNGC_1512.fits"
        galaxies_data, pixel_in_degrees = data_fits(image_file)
  [28]: # We multiply it to get it in degrees:
                                                               This is not needed.
        galaxies_degrees = galaxies_data*pixel_in_degrees
  [29]: # And we plot the two-panel image:
        fig, (ax1, ax2) = plt.subplots(1, 2, figsize=(13,5))
        fig.suptitle(r"$Image\ in\ pixel\ and\ degree\ units$")
        ax1.imshow(np.log10(galaxies_data), cmap = "inferno")
        ax1.set_title(r"$Galaxies\ in\ pixels$")
        ax1.set_xlabel(r"$x-axis$")
        ax1.set_ylabel(r"$y-axis$")
        cb1 = plt.colorbar(ax1.imshow(np.log10(galaxies_data), cmap = "inferno"))
        cb1.set_label("Intensity")
        ax2.imshow(np.log10(galaxies_degrees), cmap = "inferno",
-0.5
                    extent=[0, 900*pixel_in_degrees, 900*pixel_in_degrees, 0]) \(\square\)
        ax2.set_title(r"$Galaxies\ in\ degrees$")
        ax2.set_xlabel(r"$x-axis$")
        ax2.set_ylabel(r"$y-axis$")
        cb1 = plt.colorbar(ax2.imshow(np.log10(galaxies_degrees), cmap = "inferno",
                                       extent=[0, 900*pixel_in_degrees,_
         →900*pixel_in_degrees, 0]))
        cb1.set_label("Intensity")
```

plt.show()



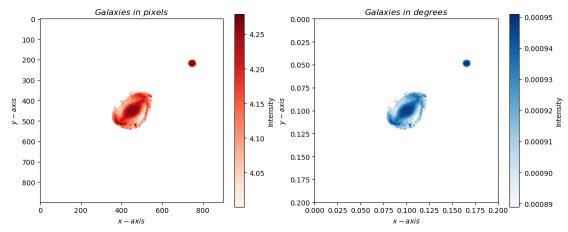
(c) Create a python funtion that receives the image as an argument and returns a masked image. The function should mask the background and any foreground stars, leaving only the regions containing the two galaxies in the image (i.e. the two largest regions in the image). Hint: Use thresholding, subsetting, and/or any other masking technique to select the areas of interest of the image.

```
[30]: # Defining the function:
      def masking_galaxies(galaxies_data):
          Given the data from a .fits file with galaxies and stars, removes
          the background and stars and leaves the regions with only the two
          galaxies in the image.
          Input: qalaxies_data -> variable containing the unmasked image
          Outputs: galaxies_pix -> the masked image in pixel units
                   qalaxies_def -> the masked image in degree units
          Date: 12/04/2024
          Author: MAY
          11 11 11
          # Here we isolate the sections that surpass the threshold:
          threshold = 4.0
          galaxies_stars_pix = np.where(np.log10(galaxies_data) > threshold,
                                         np.log10(galaxies_data), np.nan)
          # And here only the galaxies:
          # In pixels first. We cut them,
```

(d) Call your function in (c), and make a two-panel figure with high-quality, labeled plots of the resulting masked image in pixel units and in degree units.

```
galaxies_pix, galaxies_deg = masking_galaxies(galaxies_data)
[32]: # Plotting
      fig, (ax1, ax2) = plt.subplots(1, 2, figsize=(13,5))
      fig.suptitle(r"$Image\ in\ pixel\ and\ degree\ units$")
      ax1.imshow(galaxies_pix, cmap = "Reds")
      ax1.set_title(r"$Galaxies\ in\ pixels$")
      ax1.set_xlabel(r"$x-axis$")
      ax1.set_ylabel(r"$y-axis$")
      cb1 = plt.colorbar(ax1.imshow(galaxies_pix, cmap = "Reds"))
      cb1.set_label("Intensity")
      #ax1.grid()
      ax2.imshow(galaxies_deg, cmap = "Blues",
                extent=[0, 900*pixel_in_degrees, 900*pixel_in_degrees, 0])
      ax2.set_title(r"$Galaxies\ in\ degrees$")
      ax2.set_xlabel(r"$x-axis$")
      ax2.set_ylabel(r"$y-axis$")
      cb2 = plt.colorbar(ax2.imshow(galaxies_deg, cmap = "Blues",
                                    extent=[0, 900*pixel_in_degrees,_
       →900*pixel_in_degrees, 0]))
      cb2.set_label("Intensity")
      #ax2.grid()
      plt.show()
```





(e) Create a python funtion that identifies the centre of each galaxy, calculates the distance between the centres of the two galaxies, and returns such distance in pixels, degrees, and kiloparsecs. Hint: To convert the pixel units into degrees, use "CDELT2". To convert to physical distance units (kpc), define an appropriate trigonometrical model and use the knowledge that these galaxies are at a distance of 12.5 Mpc from us. The model used to get the distance in kiloparsecs assumed that both galaxies were at 12.5 Mpc from us, and we added two right triangles from where we used the said distance as the hypotenuse of both triangles. An option to get the distance in kiloparsecs between them is given by

$$\frac{\ell}{2} = 12500 \cdot \sin(\theta/2).$$

```
[33]: def distances(galaxies_pix):
          Identifies points close to the center of each galaxy,
          calculates the distance between them, and returns them
          in pixels, degrees asn kiloparsecs.
          Inputs: galaxies_pix -> file with the masked image
          Outputs: pixels -> distance in pixels
                   degrees -> distance in degrees
                   kiloparsecs -> distance in kiloparsecs
                   coor_max -> variable containing the peaks
          Date: 12/04/2024
          Author: MAY
          11 11 11
          # We transform the elements:
          np.nan_to_num(galaxies_pix, copy=False, nan = 0.)
          # We get the coordinates of the local maxima:
          coor_max = peak_local_max(galaxies_pix, min_distance = 50, num_peaks = 4)
```

```
[34]: # Here we check that everything is alright while also asigning the variables to ⊔

⇒be used later.

pixels, degrees, kiloparsecs, coor_max = distances(galaxies_pix)

print(pixels, degrees, kiloparsecs)
```

383.20751558391964 0.08515722568531547 18.578422915910892

(f) Make a high-quality, labeled plot of the masked image in physical units, showing the line connecting the centres of the galaxies and the physical distance value between them. We are going to use the image in degree units and multiply everything by the number of kiloparsecs that are in a degree. This number, 213, was found using the line of $18.5 \ Kpc$ as a ruler.

```
[35]: # Here we transform the coordinates of the points to degrees, and then to⊔

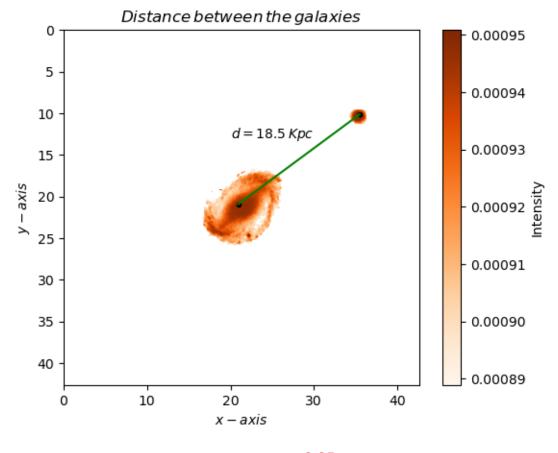
⇒kiloparsecs.

coor_deg = coor_max*pixel_in_degrees*213 This is not needed.
```

```
plt.text(20, 13, r"$d=18.5\,Kpc$")

plt.title(r"$Distance\, between\, the\, galaxies$")
plt.xlabel(r"$x-axis$")
plt.ylabel(r"$y-axis$")

plt.show()
plt.close()
```



The axes should be in degrees or kpc. -0.25

It seems to have given good results; however, I am aware I should be more technical in that regard.