

(a)code

```
import cv2
import numpy as np
from PIL import Image
import matplotlib.pyplot as plt
from operator import itemgetter

if __name__ == "__main__":

    img = cv2.imread('kid.tif', 0)

    # generate 2d fourier type
    f_img = np.fft.fft2(img)
    # shift picture
    img_shift = np.fft.fftshift(f_img)

    # (b)
    # turn into magnitude spectrum
    magnitude_spectrum = 20*np.log(np.abs(img_shift))
    PILimage = Image.fromarray(magnitude_spectrum)
    PILimage = PILimage.convert('RGB')
    PILimage.save("img/(b)kid_magnitude_spectrum.png", dpi=(150, 150))

    # padding to 1200*1200
    img_padding = cv2.copyMakeBorder(
        img, 0, 600, 0, 600, cv2.BORDER_CONSTANT)
    # generate 2d fourier type
    f_img_padding = np.fft.fft2(img_padding)
    # shift picture
    img_fshift_padding = np.fft.fftshift(f_img_padding)
    # turn into magnitude spectrum
    magnitude_spectrum_padding = 20*np.log(np.abs(img_fshift_padding))

    # producing HPF, LPF
    M, N = img_padding.shape
    H_LP = np.zeros((M, N), dtype=np.float32)
    #  $( (100 ** 2) * \pi ) / 600 ** 2 = ( (D0 ** 2) * \pi ) / 1200 * 2, D0 = 200$ 
    D0 = 200
    for u in range(M):
        for v in range(N):
            D = np.sqrt((u - M/2)**2 + (v - N/2)**2)
            H_LP[u, v] = np.exp(-(D**2) / (2 * (D0**2)))
```

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Gshift_LP = img_fshift_padding * H_LP
G_LP = np.fft.ifftshift(Gshift_LP)
g_LP = np.abs(np.fft.ifft2(G_LP))
# PILimage = Image.fromarray(np.abs(Gshift_LP).astype(np.uint8))
# PILimage.save("img/kid_Gshift_LP.png", dpi=(150, 150))

# produce HPF
H_HP = 1 - H_LP
Gshift_HP = img_fshift_padding * H_HP
G_HP = np.fft.ifftshift(Gshift_HP)
g_HP = np.abs(np.fft.ifft2(G_HP))
# PILimage = Image.fromarray(np.abs(Gshift_HP).astype(np.uint8))
# PILimage.save("img/kid_Gshift_HP.png", dpi=(150, 150))

PILimage = Image.fromarray((H_LP*255).astype(np.uint8))
PILimage.save("img/kid_LPF.png", dpi=(150, 150))
PILimage = Image.fromarray((H_HP*255).astype(np.uint8))
PILimage.save("img/kid_HPF.png", dpi=(150, 150))
PILimage = Image.fromarray(g_LP[0:600, 0:600].astype(np.uint8))
PILimage.save("img/kid_output_LPF.png", dpi=(150, 150))
PILimage = Image.fromarray(g_HP[0:600, 0:600].astype(np.uint8))
PILimage.save("img/kid_output_HPF.png", dpi=(150, 150))

# (e)
r = 600
c = 300
e_list = np.zeros((r*c, 3))
k = 0
for i in range(r):
    for j in range(c):
        e_list[k] = [j, i, magnitude_spectrum[j, i]]
        k = k+1
sorted_list = sorted(e_list, key=itemgetter(2), reverse=True)
print("(e) tables of top 25 DFT")
for i in range(25):
    print(sorted_list[i][0:2])

plt.subplot(211)
plt.imshow(H_LP, cmap='gray')
plt.title('LPF'), plt.xticks([]), plt.yticks([])
plt.subplot(212)
plt.imshow(H_HP, cmap='gray')
plt.title('HPF'), plt.xticks([]), plt.yticks([])
plt.show()

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plt.subplot(321)
plt.imshow(img, cmap='gray')
plt.title('Original img')
plt.subplot(322)
plt.imshow(magnitude_spectrum, cmap='gray')
plt.title('(b)magnitude_spectrum')
plt.subplot(323)
plt.imshow(np.abs(Gshift_LP), cmap='gray')
plt.title('output specturm of Gaussian LPF')
plt.subplot(324)
plt.imshow(np.abs(Gshift_HP), cmap='gray')
plt.title('output specturm of Gaussian HPF')
plt.subplot(325)
plt.imshow(g_LP[0:600, 0:600], cmap='gray')
plt.title('output of Gaussian LPF')
plt.subplot(326)
plt.imshow(g_HP[0:600, 0:600], cmap='gray')
plt.title('output of Gaussian HPF')
plt.axis('off')
plt.show()

```

#####

```

img = cv2.imread('fruit.tif', 0)

# generate 2d fourier type
f_img = np.fft.fft2(img)
# shift picture
img_shift = np.fft.fftshift(f_img)

# (b)
# turn into magnitude specturm
magnitude_spectrum = 20*np.log(np.abs(img_shift))
PILimage = Image.fromarray(magnitude_spectrum)
PILimage = PILimage.convert('RGB')
PILimage.save("img/(b)fruit_magnitude_spectrum.png", dpi=(150, 150))

# padding to 1200*1200
img_padding = cv2.copyMakeBorder(
    img, 0, 600, 0, 600, cv2.BORDER_CONSTANT)
# generate 2d fourier type
f_img_padding = np.fft.fft2(img_padding)
# shift picture
img_fshift_padding = np.fft.fftshift(f_img_padding)
# turn into magnitude specturm
magnitude_spectrum_padding = 20*np.log(np.abs(img_fshift_padding))

```

```

# producing HPF, LPF
M, N = img_padding.shape
H_LP = np.zeros((M, N), dtype=np.float32)
#  $((100 ** 2) * \pi) / 600 ** 2 = ((D0 ** 2) * \pi) / 1200 ** 2$ ,  $D0 = 200$ 
D0 = 200
for u in range(M):
    for v in range(N):
        D = np.sqrt((u - M/2)**2 + (v - N/2)**2)
        H_LP[u, v] = np.exp(-(D**2) / (2 * (D0**2)))

Gshift_LP = img_fshift_padding * H_LP
G_LP = np.fft.ifftshift(Gshift_LP)
g_LP = np.abs(np.fft.ifft2(G_LP))
# PILimage = Image.fromarray(np.abs(Gshift_LP).astype(np.uint8))
# PILimage.save("img/kid_Gshift_LP.png", dpi=(150, 150))

# produce HPF
H_HP = 1 - H_LP
Gshift_HP = img_fshift_padding * H_HP
G_HP = np.fft.ifftshift(Gshift_HP)
g_HP = np.abs(np.fft.ifft2(G_HP))
# PILimage = Image.fromarray(np.abs(Gshift_HP).astype(np.uint8))
# PILimage.save("img/kid_Gshift_HP.png", dpi=(150, 150))

PILimage = Image.fromarray((H_LP*255).astype(np.uint8))
PILimage.save("img/fruit_LPF.png", dpi=(150, 150))
PILimage = Image.fromarray((H_HP*255).astype(np.uint8))
PILimage.save("img/fruit_HPF.png", dpi=(150, 150))
PILimage = Image.fromarray(g_LP[0:600, 0:600].astype(np.uint8))
PILimage.save("img/fruit_output_LPF.png", dpi=(150, 150))
PILimage = Image.fromarray(g_HP[0:600, 0:600].astype(np.uint8))
PILimage.save("img/fruit_output_HPF.png", dpi=(150, 150))

# (e)
r = 600
c = 300
e_list = np.zeros((r*c, 3))
k = 0
for i in range(r):
    for j in range(c):
        e_list[k] = [j, i, magnitude_spectrum[j, i]]
        k = k+1
sorted_list = sorted(e_list, key=itemgetter(2), reverse=True)
print("(e) tables of top 25 DFT")

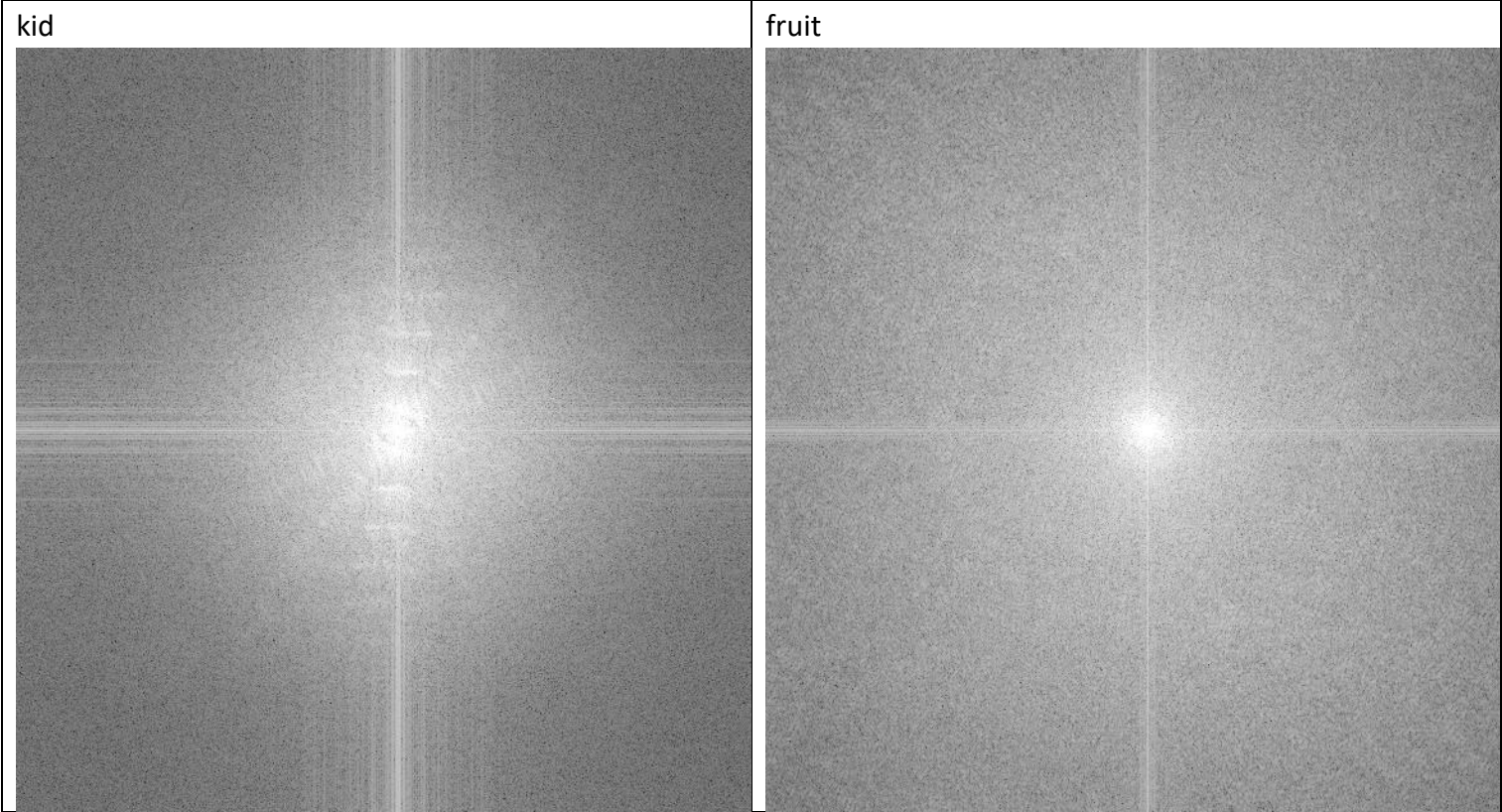
```

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for i in range(25):
    print(sorted_list[i][0:2])

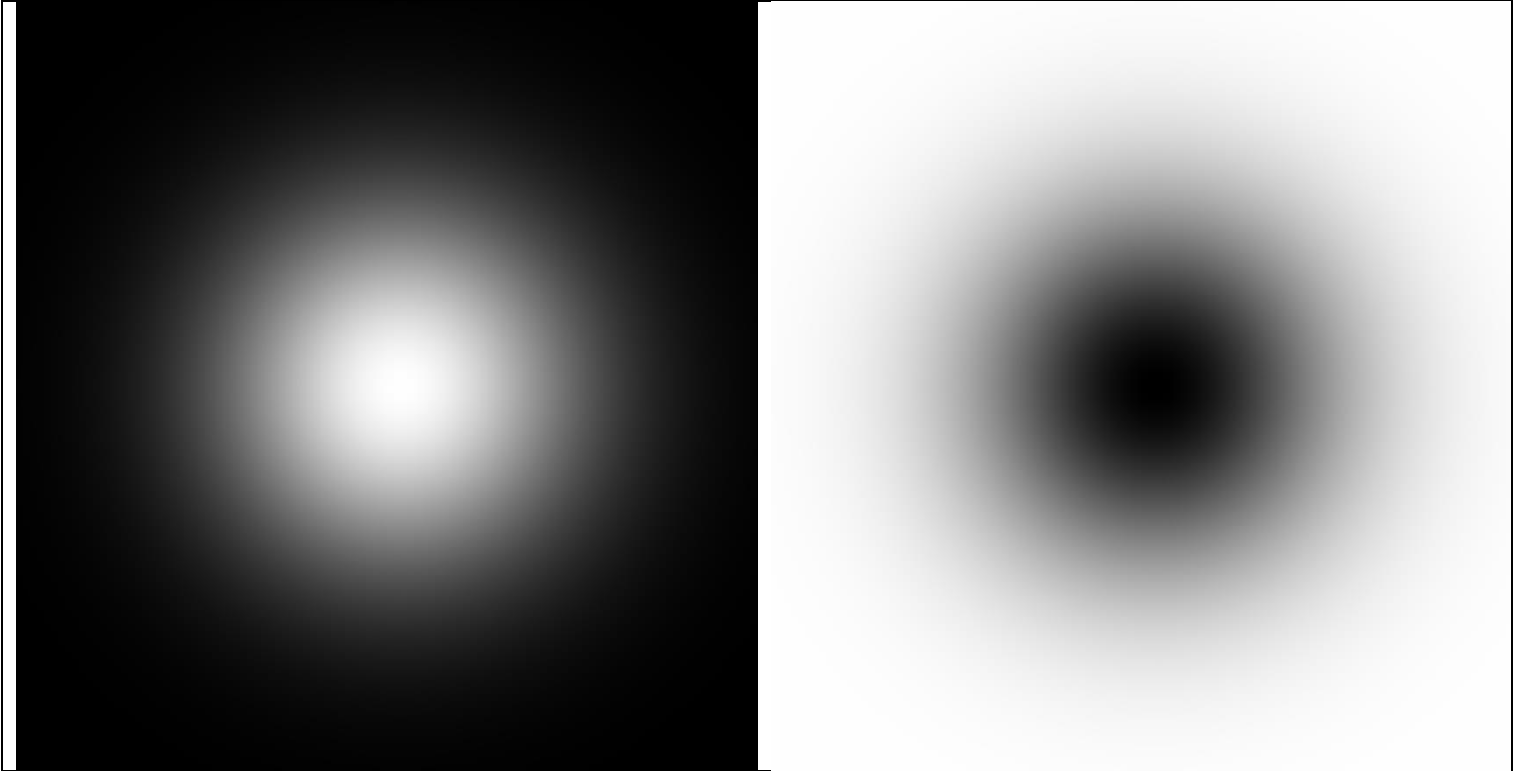
plt.subplot(211)
plt.imshow(H_LP, cmap='gray')
plt.title('LPF'), plt.xticks([]), plt.yticks([])
plt.subplot(212)
plt.imshow(H_HP, cmap='gray')
plt.title('HPF'), plt.xticks([]), plt.yticks([])
plt.show()

plt.subplot(321)
plt.imshow(img, cmap='gray')
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plt.imshow(magnitude_spectrum, cmap='gray')
plt.title('(b)magnitude_spectrum')
plt.subplot(323)
plt.imshow(np.abs(Gshift_LP), cmap='gray')
plt.title('output specturm of Gaussian LPF')
plt.subplot(324)
plt.imshow(np.abs(Gshift_LP), cmap='gray')
plt.title('output specturm of Gaussian HPF')
plt.subplot(325)
plt.imshow(g_LP[0:600, 0:600], cmap='gray')
plt.title('output of Gaussian LPF')
plt.subplot(326)
plt.imshow(g_HP[0:600, 0:600], cmap='gray')
plt.title('output of Gaussian HPF')
plt.axis('off')
plt.show()
```

(b) Fourier magnitude spectra (in Log scale) of kid and fruit



c) Magnitude responses of Gaussian LPF and HPF

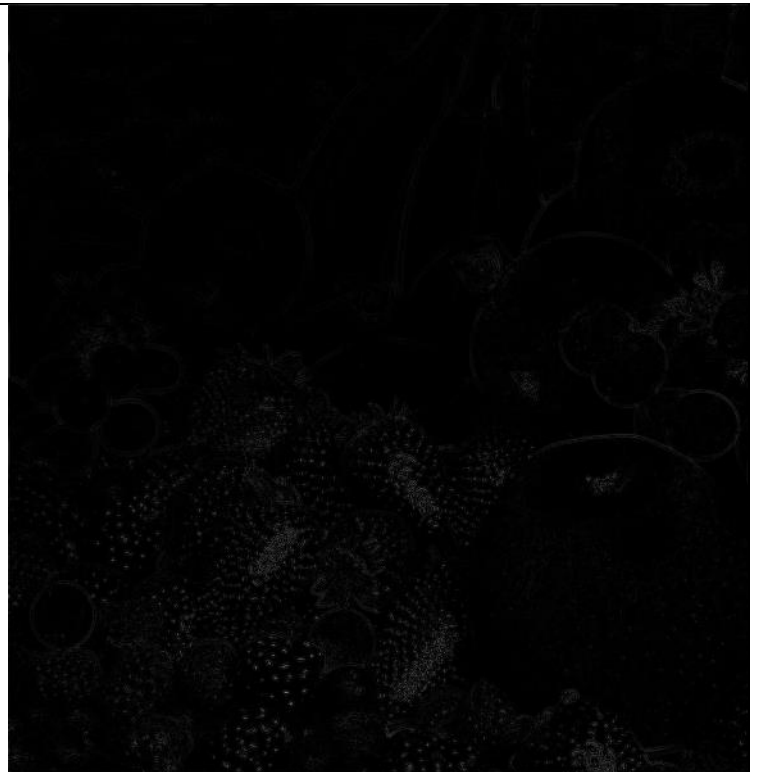


(d) 4 output images

Kid LPF, HPF



Furit LPF, HPF



(e) start from left top

Kid	Fruit
[299. 301.]	[299. 300.]
[299. 300.]	[298. 300.]
[299. 299.]	[299. 303.]
[298. 299.]	[296. 299.]
[298. 300.]	[297. 303.]
[297. 299.]	[299. 299.]
[299. 297.]	[295. 299.]
[298. 302.]	[298. 303.]
[298. 298.]	[297. 298.]
[298. 294.]	[299. 306.]
[298. 301.]	[296. 300.]
[298. 304.]	[298. 299.]
[299. 298.]	[298. 301.]
[296. 302.]	[296. 301.]
[284. 302.]	[297. 301.]
[297. 300.]	[296. 294.]
[299. 294.]	[299. 298.]
[299. 304.]	[297. 302.]
[283. 302.]	[299. 296.]
[296. 296.]	[296. 296.]
[296. 298.]	[294. 301.]
[284. 303.]	[297. 296.]
[283. 300.]	[299. 297.]
[298. 292.]	[298. 305.]
[297. 296.]	[296. 298.]