HW5

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 $\mathbf{Q}\mathbf{1}$

```
library('caret')
## Loading required package: lattice
## Loading required package: ggplot2
library('glmnet')
## Loading required package: Matrix
## Loading required package: foreach
## Loaded glmnet 2.0-10
library('parallel')
library("MASS")
set.seed(1)
#setwd("C:/Users/ce02144/Documents/HW4")
setwd("~/Dropbox/WILL/DataScience/GT Analytics/Introduction_to_Analytics_Modeling/HW4")
#Reading data
uscrime = read.table("uscrime.txt", header = TRUE)
#step seleccion
crime.scale = data.frame(scale(uscrime))
model.lm = lm(Crime ~ ., data = crime.scale)
model.step = step(model.lm, direction = 'both')
## Start: AIC=-45.39
## Crime ~ M + So + Ed + Po1 + Po2 + LF + M.F + Pop + NW + U1 +
##
      U2 + Wealth + Ineq + Prob + Time
##
##
           Df Sum of Sq
                            RSS
                                    AIC
## - So
            1
                0.00019 9.0582 -47.384
## - LF
            1 0.05961 9.1176 -47.077
## - Time
          1 0.06888 9.1269 -47.029
## - Pop
           1 0.09441 9.1524 -46.898
            1 0.12298 9.1810 -46.752
## - NW
## - M.F
           1 0.21371 9.2717 -46.289
## - Wealth 1 0.25145 9.3095 -46.099
## - Po2 1 0.25350 9.3115 -46.088
```

```
## <none>
                         9.0580 -45.385
## - U1
                0.55970 9.6177 -44.567
            1
                0.96471 10.0227 -42.629
## - Po1
## - U2
                1.21360 10.2716 -41.476
            1
## - M
            1
                1.29538 10.3534 -41.103
## - Prob
               1.33394 10.3920 -40.928
            1
## - Ed
                2.68821 11.7462 -35.171
            1
## - Ineq
            1
                2.82803 11.8860 -34.615
##
## Step: AIC=-47.38
## Crime \sim M + Ed + Po1 + Po2 + LF + M.F + Pop + NW + U1 + U2 +
##
      Wealth + Ineq + Prob + Time
##
##
           Df Sum of Sq
                            RSS
                                    AIC
## - Time
                 0.0691 9.1273 -49.027
            1
## - LF
            1
                 0.0727 9.1309 -49.009
## - Pop
                 0.0944 9.1526 -48.897
            1
## - NW
                 0.1446 9.2028 -48.640
            1
## - M.F
                 0.2169 9.2751 -48.272
            1
                 0.2537 9.3119 -48.086
## - Po2
            1
                 0.2622 9.3204 -48.043
## - Wealth 1
## <none>
                         9.0582 -47.384
## - U1
                 0.6446 9.7028 -46.154
            1
## + So
                 0.0002 9.0580 -45.385
            1
## - Po1
                 0.9647 10.0229 -44.628
            1
## - U2
            1
                 1.2692 10.3274 -43.221
## - M
                 1.3042 10.3624 -43.062
            1
## - Prob
                 1.3669 10.4251 -42.779
            1
## - Ed
                 2.6950 11.7532 -37.143
            1
## - Ineq
            1
                 3.2679 12.3261 -34.906
##
## Step: AIC=-49.03
## Crime ~ M + Ed + Po1 + Po2 + LF + M.F + Pop + NW + U1 + U2 +
##
      Wealth + Ineq + Prob
##
           Df Sum of Sq
##
                            RSS
                                    AIC
## - LF
            1
                 0.0704 9.1977 -50.666
## - NW
                 0.1035 9.2308 -50.497
            1
## - Pop
                 0.1460 9.2734 -50.281
            1
## - Po2
                 0.1934 9.3207 -50.042
            1
## - Wealth 1
                 0.2411 9.3685 -49.802
## - M.F
                 0.2793 9.4067 -49.610
            1
## <none>
                         9.1273 -49.027
## - U1
                 0.6112 9.7385 -47.981
            1
## + Time
                 0.0691 9.0582 -47.384
            1
                 0.0004 9.1269 -47.029
## + So
            1
## - Po1
            1
                 0.8967 10.0241 -46.623
## - U2
                 1.2310 10.3584 -45.081
            1
## - M
            1
                 1.2442 10.3715 -45.021
## - Prob
            1
                 1.5877 10.7150 -43.490
## - Ed
                 2.7372 11.8645 -38.700
            1
## - Ineq
            1
                 3.3620 12.4893 -36.288
##
## Step: AIC=-50.67
```

```
## Crime ~ M + Ed + Po1 + Po2 + M.F + Pop + NW + U1 + U2 + Wealth +
##
      Ineq + Prob
##
##
           Df Sum of Sq
                            RSS
                                     AIC
## - NW
            1
                 0.0780 9.2758 -52.269
## - Po2
                 0.1432 9.3409 -51.940
            1
## - Pop
                 0.1859 9.3836 -51.726
            1
## - M.F
                 0.2089 9.4067 -51.610
            1
                 0.2342 9.4320 -51.484
## - Wealth 1
## <none>
                          9.1977 -50.666
## - U1
            1
                 0.5412 9.7389 -49.979
## + LF
                 0.0704 9.1273 -49.027
            1
                 0.0668 9.1309 -49.009
## + Time
            1
## + So
                 0.0204 9.1774 -48.770
            1
## - Po1
                 0.8283 10.0260 -48.613
            1
## - U2
            1
                 1.2752 10.4729 -46.564
## - M
                 1.4555 10.6532 -45.761
            1
## - Prob
                 1.5173 10.7151 -45.489
            1
## - Ed
                 2.7627 11.9604 -40.322
            1
## - Ineq
            1
                 3.3489 12.5466 -38.073
##
## Step: AIC=-52.27
## Crime ~ M + Ed + Po1 + Po2 + M.F + Pop + U1 + U2 + Wealth + Ineq +
      Prob
##
           Df Sum of Sq
                            RSS
                                     AIC
## - Po2
                 0.1117 9.3875 -53.706
            1
                 0.1724 9.4482 -53.403
## - Pop
            1
## - M.F
                 0.1791 9.4549 -53.370
            1
## - Wealth 1
                  0.2109 9.4867 -53.212
## <none>
                          9.2758 -52.269
## - U1
            1
                 0.5608 9.8365 -51.510
## + NW
                 0.0780 9.1977 -50.666
            1
## + So
                 0.0482 9.2276 -50.514
            1
## + LF
                 0.0450 9.2308 -50.497
            1
## + Time
                 0.0303 9.2455 -50.423
            1
## - Po1
            1
                 0.7912 10.0670 -50.422
## - U2
                 1.3467 10.6225 -47.897
            1
## - Prob
                 1.4491 10.7249 -47.446
            1
## - M
                 2.0671 11.3429 -44.813
            1
## - Ed
                 2.6925 11.9683 -42.291
            1
## - Ineq
                 3.9425 13.2183 -37.622
            1
## Step: AIC=-53.71
## Crime ~ M + Ed + Po1 + M.F + Pop + U1 + U2 + Wealth + Ineq +
##
      Prob
##
##
            Df Sum of Sq
                            RSS
                                     AIC
## - Pop
            1
                 0.1494 9.5369 -54.964
## - Wealth 1
                  0.2149 9.6024 -54.643
## - M.F
                 0.2461 9.6335 -54.490
            1
## <none>
                         9.3875 -53.706
## - U1
                 0.5774 9.9649 -52.901
            1
## + Po2
                 0.1117 9.2758 -52.269
            1
```

```
## + NW
           1
                0.0465 9.3409 -51.940
## + So
                0.0254 9.3620 -51.834
            1
## + LF
           1
                0.0133 9.3742 -51.773
## + Time
                0.0038 9.3836 -51.725
            1
## - U2
           1
                1.3759 10.7634 -49.278
## - Prob
              1.4614 10.8489 -48.906
           1
## - M
           1 2.0523 11.4398 -46.413
## - Ed
              2.6039 11.9914 -44.200
           1
         1
## - Ineq
                4.0688 13.4562 -38.783
## - Po1
              7.0208 16.4082 -29.461
          1
##
## Step: AIC=-54.96
## Crime ~ M + Ed + Po1 + M.F + U1 + U2 + Wealth + Ineq + Prob
##
           Df Sum of Sq
##
                           RSS
                                  AIC
## - Wealth 1 0.1771 9.7140 -56.099
                        9.5369 -54.964
## <none>
## - M.F
                0.5648 10.1017 -54.260
## - U1
                0.6649 10.2018 -53.797
            1
## + Pop
           1
                0.1494 9.3875 -53.706
## + Po2
            1
              0.0886 9.4482 -53.403
## + NW
           1 0.0396 9.4972 -53.160
## + So
           1
                0.0383 9.4986 -53.153
## + LF
                0.0346 9.5023 -53.135
           1
## + Time
                0.0262 9.5107 -53.093
           1
## - Prob
           1 1.3275 10.8643 -50.839
## - U2
                1.3964 10.9333 -50.542
           1
## - M
                2.1454 11.6823 -47.427
           1
## - Ed
           1 2.5856 12.1225 -45.689
## - Ineq
          1
                3.9762 13.5130 -40.585
## - Po1
           1
                7.5360 17.0729 -29.595
##
## Step: AIC=-56.1
## Crime ~ M + Ed + Po1 + M.F + U1 + U2 + Ineq + Prob
##
##
          Df Sum of Sq
                           RSS
                                  AIC
## <none>
                        9.7140 -56.099
## + Wealth 1
                0.1771 9.5369 -54.964
## - M.F
           1
                0.6896 10.4036 -54.876
## + Pop
                0.1116 9.6024 -54.643
            1
## + Po2
                0.0946 9.6194 -54.559
           1
## + So
                0.0624 9.6516 -54.402
           1
## + LF
                0.0292 9.6847 -54.241
            1
## + NW
                0.0254 9.6886 -54.222
            1
## + Time
                0.0153 9.6986 -54.174
           1
## - U1
                0.8493 10.5633 -54.160
            1
                1.6578 11.3717 -50.694
## - Prob
           1
## - U2
           1 1.7077 11.4216 -50.488
## - M
           1
               1.9841 11.6981 -49.364
## - Ed
           1
                2.9802 12.6941 -45.523
## - Ineq 1 4.9353 14.6492 -38.791
## - Po1
          1 11.1778 20.8918 -22.107
```

##

##

- LF

Wealth + Ineq + Prob

Df Sum of Sq

AIC

RSS

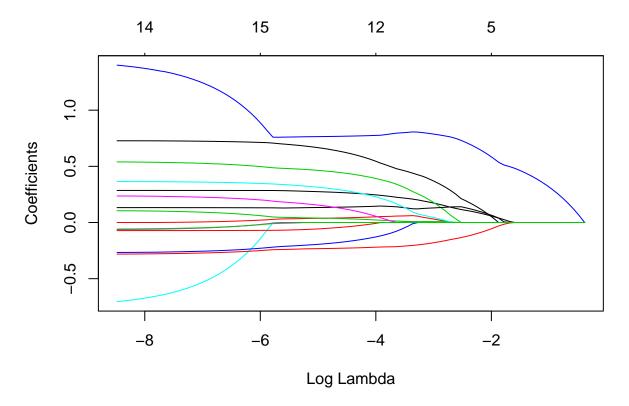
1 0.0704 9.1977 -50.666

```
0.1035 9.2308 -50.497
## - NW
            1
## - Pop
                 0.1460 9.2734 -50.281
            1
## - Po2
            1
                 0.1934 9.3207 -50.042
                 0.2411 9.3685 -49.802
## - Wealth 1
## - M.F
            1
                 0.2793 9.4067 -49.610
## <none>
                         9.1273 -49.027
## - U1
                 0.6112 9.7385 -47.981
            1
## + Time
                 0.0691 9.0582 -47.384
            1
## + So
            1
                 0.0004 9.1269 -47.029
## - Po1
                 0.8967 10.0241 -46.623
            1
## - U2
            1
                1.2310 10.3584 -45.081
## - M
                 1.2442 10.3715 -45.021
            1
## - Prob
            1
                1.5877 10.7150 -43.490
## - Ed
            1
                 2.7372 11.8645 -38.700
## - Ineq
                 3.3620 12.4893 -36.288
            1
##
## Step: AIC=-50.67
## Crime ~ M + Ed + Po1 + Po2 + M.F + Pop + NW + U1 + U2 + Wealth +
##
      Ineq + Prob
##
##
           Df Sum of Sq
                            RSS
                                    AIC
## - NW
            1
                0.0780 9.2758 -52.269
                 0.1432 9.3409 -51.940
## - Po2
            1
## - Pop
                 0.1859 9.3836 -51.726
            1
## - M.F
                 0.2089 9.4067 -51.610
            1
## - Wealth 1
                 0.2342 9.4320 -51.484
## <none>
                         9.1977 -50.666
## - U1
            1
                 0.5412 9.7389 -49.979
## + LF
                 0.0704 9.1273 -49.027
            1
## + Time
            1
                 0.0668 9.1309 -49.009
## + So
            1
                 0.0204 9.1774 -48.770
## - Po1
            1
                 0.8283 10.0260 -48.613
## - U2
            1
                1.2752 10.4729 -46.564
                1.4555 10.6532 -45.761
## - M
            1
## - Prob
            1
                 1.5173 10.7151 -45.489
## - Ed
                 2.7627 11.9604 -40.322
            1
## - Ineq
            1
                 3.3489 12.5466 -38.073
##
## Step: AIC=-52.27
## Crime ~ M + Ed + Po1 + Po2 + M.F + Pop + U1 + U2 + Wealth + Ineq +
##
      Prob
##
           Df Sum of Sq
                            RSS
                                    AIC
## - Po2
                 0.1117 9.3875 -53.706
            1
## - Pop
                 0.1724 9.4482 -53.403
            1
## - M.F
                 0.1791 9.4549 -53.370
            1
## - Wealth 1
                 0.2109 9.4867 -53.212
## <none>
                         9.2758 -52.269
## - U1
            1
                 0.5608 9.8365 -51.510
## + NW
            1
                 0.0780 9.1977 -50.666
## + So
                 0.0482 9.2276 -50.514
            1
## + LF
            1 0.0450 9.2308 -50.497
## + Time
            1 0.0303 9.2455 -50.423
## - Po1
            1 0.7912 10.0670 -50.422
```

```
## - U2
            1
                 1.3467 10.6225 -47.897
## - Prob
                 1.4491 10.7249 -47.446
            1
                 2.0671 11.3429 -44.813
## - M
            1
                 2.6925 11.9683 -42.291
## - Ed
            1
## - Ineq
            1
                 3.9425 13.2183 -37.622
##
## Step: AIC=-53.71
## Crime ~ M + Ed + Po1 + M.F + Pop + U1 + U2 + Wealth + Ineq +
##
      Prob
##
           Df Sum of Sq
##
                            RSS
                                     AIC
## - Pop
                 0.1494 9.5369 -54.964
            1
                  0.2149 9.6024 -54.643
## - Wealth 1
                  0.2461 9.6335 -54.490
## - M.F
            1
## <none>
                          9.3875 -53.706
## - U1
            1
                 0.5774 9.9649 -52.901
## + Po2
                 0.1117 9.2758 -52.269
            1
## + NW
                 0.0465 9.3409 -51.940
            1
## + So
                 0.0254 9.3620 -51.834
            1
## + LF
            1
                 0.0133 9.3742 -51.773
                 0.0038 9.3836 -51.725
## + Time
            1
## - U2
                 1.3759 10.7634 -49.278
            1
## - Prob
                 1.4614 10.8489 -48.906
            1
## - M
                 2.0523 11.4398 -46.413
            1
## - Ed
                 2.6039 11.9914 -44.200
            1
## - Ineq
            1
                 4.0688 13.4562 -38.783
## - Po1
                 7.0208 16.4082 -29.461
            1
##
## Step: AIC=-54.96
## Crime ~ M + Ed + Po1 + M.F + U1 + U2 + Wealth + Ineq + Prob
##
##
           Df Sum of Sq
                            RSS
                                     AIC
## - Wealth 1
                 0.1771 9.7140 -56.099
## <none>
                         9.5369 -54.964
## - M.F
            1
                 0.5648 10.1017 -54.260
## - U1
                 0.6649 10.2018 -53.797
            1
## + Pop
            1
                 0.1494 9.3875 -53.706
## + Po2
                 0.0886 9.4482 -53.403
            1
## + NW
                 0.0396 9.4972 -53.160
            1
## + So
                 0.0383 9.4986 -53.153
            1
## + LF
                 0.0346 9.5023 -53.135
            1
## + Time
                 0.0262 9.5107 -53.093
            1
                 1.3275 10.8643 -50.839
## - Prob
            1
## - U2
                 1.3964 10.9333 -50.542
            1
## - M
                 2.1454 11.6823 -47.427
            1
                 2.5856 12.1225 -45.689
## - Ed
            1
                 3.9762 13.5130 -40.585
## - Ineq
            1
## - Po1
                 7.5360 17.0729 -29.595
            1
##
## Step: AIC=-56.1
## Crime ~ M + Ed + Po1 + M.F + U1 + U2 + Ineq + Prob
##
##
           Df Sum of Sq
                            RSS
                                    AIC
## <none>
                          9.7140 -56.099
```

```
0.1771 9.5369 -54.964
## + Wealth 1
## - M.F 1
                0.6896 10.4036 -54.876
                0.1116 9.6024 -54.643
## + Pop
## + Po2
                0.0946 9.6194 -54.559
            1
## + So
            1
                0.0624 9.6516 -54.402
## + LF
            1 0.0292 9.6847 -54.241
## + NW
          1 0.0254 9.6886 -54.222
## + Time
          1 0.0153 9.6986 -54.174
            1 0.8493 10.5633 -54.160
## - U1
## - Prob
            1 1.6578 11.3717 -50.694
## - U2
            1
                1.7077 11.4216 -50.488
## - M
                1.9841 11.6981 -49.364
            1
## - Ed
                2.9802 12.6941 -45.523
            1
## - Ineq
          1
                4.9353 14.6492 -38.791
## - Po1
            1 11.1778 20.8918 -22.107
model.step.aic$anova
## Stepwise Model Path
## Analysis of Deviance Table
## Initial Model:
## Crime ~ M + So + Ed + Po1 + Po2 + LF + M.F + Pop + NW + U1 +
##
      U2 + Wealth + Ineq + Prob + Time
## Final Model:
## Crime ~ M + Ed + Po1 + M.F + U1 + U2 + Ineq + Prob
##
##
        Step Df
                    Deviance Resid. Df Resid. Dev
                                   31 9.058009 -45.38542
## 1
## 2
        - So 1 0.0001910216
                                   32 9.058200 -47.38443
## 3
      - Time 1 0.0691288785
                                  33 9.127329 -49.02710
## 4
       - LF 1 0.0704156967
                                   34 9.197745 -50.66590
## 5
       - NW 1 0.0780466621
                                   35 9.275791 -52.26876
                                   36 9.387476 -53.70625
## 6
       - Po2 1 0.1116843137
## 7
       - Pop 1 0.1493820171
                                   37 9.536858 -54.96423
## 8 - Wealth 1 0.1771111995
                                  38 9.713969 -56.09938
x = as.matrix(crime.scale[-16])
y = as.matrix(crime.scale[16])
# Lasso, ridge, elastic net cross validation
model.lasso = glmnet(x = x, y = y,
                     family = 'gaussian', alpha = 1)
#Results
#Numbers of coefficients upper, lambda x, mse y
```

plot(model.lasso, xvar = "lambda")



```
coef(model.lasso, s = model.lasso$lambda.min)
```

```
## 16 x 88 sparse Matrix of class "dgCMatrix"
      [[ suppressing 88 column names 's0', 's1', 's2' ... ]]
##
## (Intercept) -1.465841e-16 -1.460278e-16 -1.455209e-16 -1.450591e-16
## So
## Ed
## Po1
                              6.108488e-02 1.167432e-01 1.674569e-01
## Po2
## LF
## M.F
## Pop
## NW
## U1
## U2
## Wealth
## Ineq
## Prob
## Time
## (Intercept) -1.446382e-16 -1.442548e-16 -1.439054e-16 -1.435870e-16
## M
## So
## Ed
## Po1
              2.136654e-01 2.557688e-01 2.941319e-01 3.290869e-01
```

```
## Po2
## LF
## M.F
## Pop
## NW
## U1
## U2
## Wealth
## Ineq
## Prob
## Time
## (Intercept) -1.432970e-16 -1.430327e-16 -1.427919e-16 -1.425724e-16
## M
## So
## Ed
## Po1
          3.609366e-01 3.899569e-01 4.163991e-01 4.404922e-01
## Po2
## LF
## M.F
## Pop
## NW
## U1
## U2
## Wealth
## Ineq
## Prob
## Time
##
## (Intercept) -1.423725e-16 -1.421903e-16 -1.487712e-16 -1.617987e-16
## M
                                                     5.369483e-03
## So
## Ed
             4.624450e-01 4.824475e-01 4.983904e-01 5.117919e-01
## Po1
## Po2
                           •
## LF
## M.F
                                       9.947910e-03 2.567674e-02
## Pop
## NW
## U1
## U2
## Wealth
## Ineq
                                       -4.123119e-03 -1.552643e-02
## Prob
## Time
## (Intercept) -1.886374e-16 -2.222194e-16 -2.528547e-16 -2.807552e-16
## M 3.870868e-02 5.309193e-02 6.604337e-02 7.798625e-02
## So
## Ed
## Po1
             5.362635e-01 5.723862e-01 6.054400e-01 6.354735e-01
## Po2
## LF
## M.F 4.018237e-02 5.875653e-02 7.573368e-02 9.116445e-02
```

```
## Pop
## NW
## U1
## U2
## Wealth
                    3.943430e-02 7.558726e-02 1.083589e-01
## Ineq
## Prob
              -3.037812e-02 -4.966918e-02 -6.722508e-02 -8.323537e-02
## Time
## (Intercept) -3.061654e-16 -3.293185e-16 -3.504148e-16 -3.694731e-16
             8.879298e-02 9.864001e-02 1.076123e-01 1.157874e-01
## So
## Ed
                                                      1.884051e-04
             6.628522e-01 6.877991e-01 7.105297e-01 7.311501e-01
## Po1
## Po2
## LF
## M.F
             1.052353e-01 1.180562e-01 1.297381e-01 1.403030e-01
## Pop
## NW
## U1
## U2
## Wealth
             1.382753e-01 1.655342e-01 1.903715e-01 2.130764e-01
## Ineq
## Prob
             -9.781545e-02 -1.111003e-01 -1.232049e-01 -1.342423e-01
## Time
## (Intercept) -3.647061e-16 -3.583455e-16 -3.464805e-16 -3.360968e-16
       1.257430e-01 1.364218e-01 1.494782e-01 1.614566e-01
## So
                            7.360847e-04 1.080558e-02 2.082223e-02
              3.324326e-02 6.651345e-02 1.067465e-01 1.425311e-01
## Ed
              7.488734e-01 7.622047e-01 7.709699e-01 7.789440e-01
## Po1
## Po2
## LF
## M.F
             1.397168e-01 1.385868e-01 1.353634e-01 1.326629e-01
## Pop
## NW
             2.127491e-03 6.923580e-03 7.823401e-03 8.163900e-03
## U1
## U2
                            4.909071e-03 1.919877e-02 3.204789e-02
## Wealth
              2.532281e-01 2.870115e-01 3.168773e-01 3.431307e-01
## Ineq
## Prob
             -1.433736e-01 -1.524170e-01 -1.621758e-01 -1.712377e-01
## Time
## (Intercept) -3.266856e-16 -3.181104e-16 -3.094884e-16 -2.982973e-16
              1.723602e-01 1.822966e-01 1.913769e-01 2.007211e-01
              2.985787e-02 3.809355e-02 4.579905e-02 5.617018e-02
## So
              1.751316e-01 2.048353e-01 2.316164e-01 2.538630e-01
## Ed
## Po1
             7.863357e-01 7.930698e-01 7.994261e-01 8.046182e-01
## Po2
                                         1.238633e-03 7.469092e-03
## LF
## M.F
             1.301819e-01 1.279215e-01 1.253784e-01 1.214060e-01
## Pop
## NW
             8.380552e-03 8.577376e-03 8.439516e-03 6.861683e-03
## U1
```

```
4.374018e-02 5.439408e-02 6.453463e-02 7.576208e-02
## Wealth
                           •
                                         .
              3.672462e-01 3.892159e-01 4.093795e-01 4.243990e-01
              -1.794371e-01 -1.869089e-01 -1.934599e-01 -1.992222e-01
## Prob
## Time
##
## (Intercept) -2.943771e-16 -2.983091e-16 -3.016557e-16 -3.046715e-16
               2.083090e-01 2.143137e-01 2.197813e-01 2.247676e-01
## M
              6.143352e-02 5.938496e-02 5.830696e-02 5.738635e-02
## So
## Ed
              2.758070e-01 3.000769e-01 3.213600e-01 3.407168e-01
## Po1
              8.063720e-01 8.020148e-01 7.986546e-01 7.955957e-01
## Po2
## LF
              9.414414e-03 5.762247e-03 2.887387e-03 3.021195e-04
## M.F
              1.221930e-01 1.288092e-01 1.345463e-01 1.397577e-01
## Pop
## NW
              6.355609e-03 9.368004e-03 1.148901e-02 1.340837e-02
## U1
              -1.076307e-02 -3.577858e-02 -5.754773e-02 -7.733692e-02
## U2
              9.343705e-02 1.207421e-01 1.447435e-01 1.665824e-01
## Wealth
              4.393192e-01 4.538892e-01 4.669237e-01 4.787490e-01
## Prob
              -2.039764e-01 -2.079189e-01 -2.115324e-01 -2.148360e-01
## Time
##
## (Intercept) -3.074901e-16 -3.103874e-16 -3.129545e-16 -3.133367e-16
              2.309848e-01 2.368530e-01 2.420757e-01 2.465627e-01
## So
              5.507658e-02 5.397527e-02 5.295032e-02 5.042014e-02
## Ed
              3.569551e-01 3.701484e-01 3.820119e-01 3.933085e-01
## Po1
              7.892436e-01 7.825085e-01 7.767127e-01 7.750817e-01
## Po2
## LF
## M.F
              1.425856e-01 1.447811e-01 1.464657e-01 1.445178e-01
## Pop
                                         -9.083221e-04 -8.622515e-03
              1.598125e-02 1.822232e-02 2.022464e-02 2.306971e-02
## NW
## U1
              -9.390151e-02 -1.073457e-01 -1.195053e-01 -1.296086e-01
              1.858803e-01 2.017781e-01 2.162493e-01 2.295687e-01
## U2
## Wealth
              1.242575e-02 2.782691e-02 4.244624e-02 5.781035e-02
## Ineq
              4.961557e-01 5.130815e-01 5.291168e-01 5.479412e-01
## Prob
              -2.160509e-01 -2.170651e-01 -2.181077e-01 -2.200107e-01
## Time
##
## (Intercept) -3.138094e-16 -3.142308e-16 -3.146152e-16 -3.149655e-16
              2.505483e-01 2.541835e-01 2.574941e-01 2.605084e-01
## M
              4.850116e-02 4.674977e-02 4.515873e-02 4.371560e-02
## So
## Ed
              4.033644e-01 4.125514e-01 4.209180e-01 4.285369e-01
              7.735709e-01 7.721855e-01 7.709252e-01 7.697799e-01
## Po1
## Po2
## LF
## M.F
              1.429518e-01 1.415339e-01 1.402431e-01 1.390686e-01
## Pop
              -1.546299e-02 -2.168851e-02 -2.736017e-02 -3.252669e-02
              2.542826e-02 2.758818e-02 2.955422e-02 3.134311e-02
## NW
## U1
              -1.387641e-01 -1.471333e-01 -1.547556e-01 -1.616968e-01
## U2
              2.415699e-01 2.525356e-01 2.625229e-01 2.716181e-01
## Wealth
             7.160073e-02 8.411750e-02 9.551875e-02 1.058998e-01
              5.647348e-01 5.800000e-01 5.939043e-01 6.065654e-01
## Ineq
```

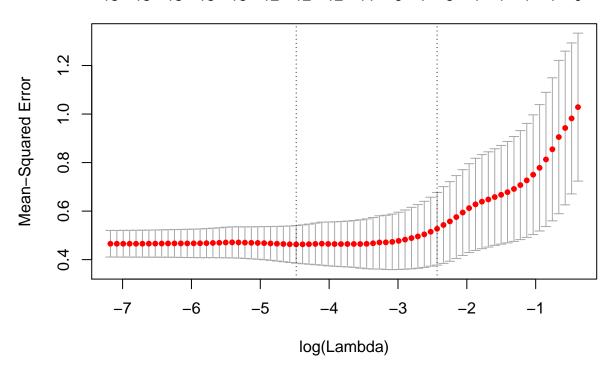
```
## Prob
              -2.217979e-01 -2.234308e-01 -2.249200e-01 -2.262789e-01
## Time
##
## (Intercept) -3.152844e-16 -3.155748e-16 -3.158388e-16 -3.160786e-16
               2.632526e-01 2.657502e-01 2.680230e-01 2.700905e-01
## So
              4.240729e-02 4.122200e-02 4.014910e-02 3.917902e-02
## Ed
              4.354745e-01 4.417910e-01 4.475416e-01 4.527764e-01
              7.687395e-01 7.677946e-01 7.669372e-01 7.661597e-01
## Po1
## Po2
## LF
## M.F
              1.380001e-01 1.370285e-01 1.361453e-01 1.353429e-01
              -3.723288e-02 -4.151960e-02 -4.542407e-02 -4.898014e-02
## Pop
               3.297085e-02 3.445197e-02 3.579975e-02 3.702627e-02
## NW
## U1
              -1.680174e-01 -1.737725e-01 -1.790121e-01 -1.837816e-01
## U2
              2.799004e-01 2.874420e-01 2.943082e-01 3.005588e-01
## Wealth
              1.153505e-01 1.239529e-01 1.317809e-01 1.389017e-01
              6.180932e-01 6.285875e-01 6.381394e-01 6.468310e-01
## Ineq
## Prob
              -2.275193e-01 -2.286519e-01 -2.296865e-01 -2.306323e-01
## Time
##
## (Intercept) -3.164261e-16 -3.166270e-16 -3.168075e-16 -3.169715e-16
              2.719011e-01 2.736089e-01 2.751650e-01 2.765794e-01
               3.830128e-02 3.752564e-02 3.681096e-02 3.616710e-02
## So
## Ed
               4.573892e-01 4.617094e-01 4.656575e-01 4.692482e-01
## Po1
              7.656205e-01 7.650043e-01 7.644342e-01 7.639208e-01
## Po2
## LF
## M.F
              1.345736e-01 1.339095e-01 1.333085e-01 1.327626e-01
## Pop
              -5.233185e-02 -5.528182e-02 -5.796845e-02 -6.041533e-02
## NW
              3.796430e-02 3.896378e-02 3.988365e-02 4.071987e-02
## U1
              -1.880392e-01 -1.919650e-01 -1.955583e-01 -1.988246e-01
## U2
              3.061123e-01 3.112647e-01 3.159763e-01 3.202606e-01
## Wealth
              1.456921e-01 1.515767e-01 1.569261e-01 1.617894e-01
              6.551871e-01 6.623830e-01 6.689315e-01 6.748882e-01
## Ineq
## Prob
              -2.314593e-01 -2.322522e-01 -2.329755e-01 -2.336374e-01
## Time
## (Intercept) -3.171155e-16 -3.175001e-16 -3.177270e-16 -3.179885e-16
               2.780147e-01 2.796905e-01 2.809979e-01 2.823311e-01
## M
## So
              3.553718e-02 3.431198e-02 3.381973e-02 3.296149e-02
              4.724557e-01 4.752143e-01 4.775428e-01 4.798922e-01
## Ed
              7.635040e-01 7.622323e-01 7.616035e-01 7.606867e-01
## Po1
## Po2
## LF
## M.F
              1.320827e-01 1.311250e-01 1.304618e-01 1.297632e-01
              -6.252660e-02 -6.411680e-02 -6.551911e-02 -6.684162e-02
## Pop
## NW
              4.151610e-02 4.295821e-02 4.393970e-02 4.501316e-02
## U1
              -2.018168e-01 -2.049728e-01 -2.075236e-01 -2.101810e-01
## U2
              3.242001e-01 3.282070e-01 3.314973e-01 3.348574e-01
               1.662041e-01 1.713263e-01 1.748378e-01 1.786966e-01
## Wealth
              6.803189e-01 6.858792e-01 6.900246e-01 6.943435e-01
## Ineq
## Prob
              -2.344990e-01 -2.361113e-01 -2.375701e-01 -2.388128e-01
## Time
              -6.845437e-04 -2.665347e-03 -4.253191e-03 -5.767509e-03
##
```

```
## (Intercept) -3.183098e-16 -3.204461e-16 -3.220302e-16 -3.092099e-16
## M
               2.834650e-01 2.842335e-01 2.848985e-01 2.849671e-01
## So
               3.230554e-02 3.075310e-02 2.797934e-02 2.457911e-02
## Ed
               4.818075e-01 4.841922e-01 4.873763e-01 4.917930e-01
## Po1
               7.600610e-01 7.588239e-01 7.595837e-01 8.131146e-01
## Po2
                                          -3.320027e-03 -6.238935e-02
## LF
              -3.670299e-05 -2.174018e-03 -5.012740e-03 -1.052120e-02
               1.291136e-01 1.297524e-01 1.305851e-01 1.307988e-01
## M.F
## Pop
              -6.808607e-02 -6.890612e-02 -6.947080e-02 -6.987925e-02
## NW
               4.583804e-02 4.720623e-02 4.938949e-02 5.442931e-02
## U1
              -2.123677e-01 -2.154383e-01 -2.193124e-01 -2.236148e-01
               3.376290e-01 3.402012e-01 3.432623e-01 3.450458e-01
## U2
## Wealth
               1.822399e-01 1.855857e-01 1.899468e-01 1.960539e-01
## Ineq
               6.983460e-01 7.022820e-01 7.068486e-01 7.105986e-01
## Prob
              -2.399513e-01 -2.411287e-01 -2.420455e-01 -2.452590e-01
## Time
               -7.122194e-03 -8.331078e-03 -9.616500e-03 -1.387851e-02
##
  (Intercept) -2.948081e-16 -2.816649e-16 -2.696963e-16 -2.588104e-16
## M
               2.850174e-01 2.850629e-01 2.851044e-01 2.851425e-01
## So
               2.203148e-02 1.970874e-02 1.759287e-02 1.566635e-02
## Ed
               4.963750e-01 5.005533e-01 5.043592e-01 5.078240e-01
## Po1
               8.697180e-01 9.213688e-01 9.684053e-01 1.011193e+00
              -1.241773e-01 -1.805567e-01 -2.319001e-01 -2.786073e-01
## Po2
              -1.559049e-02 -2.021373e-02 -2.442477e-02 -2.825770e-02
## LF
## M.F
               1.309785e-01 1.311417e-01 1.312905e-01 1.314266e-01
## Pop
              -7.008828e-02 -7.027856e-02 -7.045199e-02 -7.061020e-02
## NW
               5.933925e-02 6.381805e-02 6.789723e-02 7.160930e-02
              -2.278044e-01 -2.316239e-01 -2.351033e-01 -2.382717e-01
## U1
## U2
               3.469555e-01 3.486953e-01 3.502805e-01 3.517252e-01
## Wealth
               1.998966e-01 2.033993e-01 2.065904e-01 2.094966e-01
               7.123039e-01 7.138558e-01 7.152704e-01 7.165612e-01
## Ineq
## Prob
              -2.486984e-01 -2.518358e-01 -2.546933e-01 -2.572936e-01
## Time
              -1.814620e-02 -2.203920e-02 -2.558484e-02 -2.881136e-02
##
## (Intercept) -2.489188e-16 -2.398597e-16 -2.316000e-16 -2.240879e-16
## M
               2.851777e-01 2.852090e-01 2.852375e-01 2.852636e-01
## So
               1.391290e-02 1.231186e-02 1.085256e-02 9.523711e-03
## Ed
               5.109766e-01 5.138564e-01 5.164813e-01 5.188708e-01
## Po1
               1.050079e+00 1.085680e+00 1.118139e+00 1.147664e+00
              -3.210597e-01 -3.599200e-01 -3.953498e-01 -4.275786e-01
## Po2
              -3.174448e-02 -3.493114e-02 -3.783594e-02 -4.047990e-02
## LF
               1.315512e-01 1.316637e-01 1.317661e-01 1.318597e-01
## M.F
## Pop
              -7.075462e-02 -7.088580e-02 -7.100528e-02 -7.111428e-02
## NW
               7.498496e-02 7.807203e-02 8.088625e-02 8.344716e-02
## U1
              -2.411558e-01 -2.437884e-01 -2.461876e-01 -2.483724e-01
               3.530420e-01 3.542410e-01 3.553334e-01 3.563290e-01
## U2
## Wealth
               2.121429e-01 2.145575e-01 2.167582e-01 2.187627e-01
## Ineq
               7.177399e-01 7.188097e-01 7.197842e-01 7.206736e-01
## Prob
              -2.596583e-01 -2.618208e-01 -2.637921e-01 -2.655859e-01
## Time
              -3.174542e-02 -3.442873e-02 -3.687487e-02 -3.910076e-02
## (Intercept) -2.172688e-16 -2.110100e-16 -2.053768e-16 -2.001477e-16
## M
               2.852878e-01 2.853092e-01 2.853299e-01 2.853472e-01
               8.314490e-03 7.209321e-03 6.206800e-03 5.286810e-03
## So
```

```
5.210441e-01 5.230317e-01 5.248321e-01 5.264877e-01
## Ed
## Po1
               1.174472e+00 1.199065e+00 1.221220e+00 1.241758e+00
## Po2
              -4.568454e-01 -4.836887e-01 -5.078787e-01 -5.302919e-01
## LF
              -4.288382e-02 -4.508369e-02 -4.707399e-02 -4.890722e-02
               1.319456e-01 1.320229e-01 1.320951e-01 1.321586e-01
## M.F
              -7.121383e-02 -7.130410e-02 -7.138694e-02 -7.146151e-02
## Pop
               8.577449e-02 8.790626e-02 8.983206e-02 9.161007e-02
## NW
              -2.503607e-01 -2.521771e-01 -2.538257e-01 -2.553373e-01
## U1
## U2
               3.572366e-01 3.580631e-01 3.588175e-01 3.595036e-01
## Wealth
               2.205876e-01 2.222536e-01 2.237668e-01 2.251516e-01
## Ineq
               7.214866e-01 7.222232e-01 7.229009e-01 7.235091e-01
              -2.672159e-01 -2.687090e-01 -2.700575e-01 -2.713027e-01
## Prob
## Time
              -4.112347e-02 -4.297625e-02 -4.464965e-02 -4.619491e-02
##
## (Intercept) -1.954954e-16 -1.911923e-16 -1.872435e-16 -1.836398e-16
               2.853649e-01 2.853800e-01 2.853933e-01 2.854054e-01
## M
## So
               4.455855e-03 3.694865e-03 2.999679e-03 2.366176e-03
## Ed
               5.279795e-01 5.293486e-01 5.306007e-01 5.317427e-01
               1.260060e+00 1.276970e+00 1.292478e+00 1.306629e+00
## Po1
## Po2
               -5.502790e-01 -5.687373e-01 -5.856628e-01 -6.011057e-01
## LF
              -5.055463e-02 -5.206854e-02 -5.345359e-02 -5.471652e-02
## M.F
               1.322193e-01 1.322731e-01 1.323214e-01 1.323654e-01
              -7.153032e-02 -7.159242e-02 -7.164868e-02 -7.169979e-02
## Pop
               9.320336e-02 9.467029e-02 9.601365e-02 9.723896e-02
## NW
              -2.567045e-01 -2.579562e-01 -2.590997e-01 -2.601422e-01
## U1
## U2
               3.601314e-01 3.607022e-01 3.612223e-01 3.616963e-01
## Wealth
               2.264050e-01 2.275506e-01 2.285955e-01 2.295468e-01
               7.240733e-01 7.245807e-01 7.250399e-01 7.254568e-01
## Ineq
## Prob
              -2.724182e-01 -2.734455e-01 -2.743864e-01 -2.752447e-01
## Time
              -4.757897e-02 -4.885363e-02 -5.002094e-02 -5.108570e-02
##
## (Intercept) -1.804446e-16 -1.774602e-16 -1.747758e-16 -1.731350e-16
## M
               2.854180e-01 2.854281e-01 2.854380e-01 2.855739e-01
## So
               1.795995e-03 1.271454e-03 7.970977e-04 9.134709e-06
               5.327702e-01 5.337165e-01 5.345738e-01 5.353907e-01
## Ed
## Po1
               1.319196e+00 1.330915e+00 1.341462e+00 1.348861e+00
## Po2
              -6.148298e-01 -6.276202e-01 -6.391342e-01 -6.481716e-01
## LF
              -5.584826e-02 -5.689471e-02 -5.784010e-02 -5.889040e-02
               1.324078e-01 1.324443e-01 1.324785e-01 1.327824e-01
## M.F
              -7.174687e-02 -7.178942e-02 -7.182822e-02 -7.166464e-02
## Pop
               9.833369e-02 9.934853e-02 1.002643e-01 1.013957e-01
## NW
## U1
              -2.610840e-01 -2.619480e-01 -2.627321e-01 -2.638455e-01
## U2
               3.621308e-01 3.625239e-01 3.628835e-01 3.635015e-01
## Wealth
               2.304039e-01 2.311926e-01 2.319051e-01 2.334486e-01
## Ineq
               7.258424e-01 7.261887e-01 7.265048e-01 7.270515e-01
              -2.760117e-01 -2.767230e-01 -2.773652e-01 -2.778658e-01
## Prob
## Time
              -5.203669e-02 -5.291889e-02 -5.371492e-02 -5.445790e-02
##
## (Intercept) -1.707058e-16 -1.684404e-16 -1.664492e-16 -1.645955e-16
               2.855666e-01 2.855471e-01 2.855308e-01 2.855150e-01
## M
## So
## Ed
               5.361002e-01 5.367345e-01 5.373031e-01 5.378264e-01
## Po1
               1.357566e+00 1.365716e+00 1.372886e+00 1.379558e+00
## Po2
              -6.576675e-01 -6.664877e-01 -6.742569e-01 -6.814805e-01
```

```
## LF
              -5.953043e-02 -6.011408e-02 -6.063445e-02 -6.111482e-02
## M.F
              1.327475e-01 1.327229e-01 1.327054e-01 1.326871e-01
## Pop
              -7.170476e-02 -7.173601e-02 -7.176329e-02 -7.178871e-02
              1.020210e-01 1.025834e-01 1.030820e-01 1.035436e-01
## NW
## U1
              -2.643453e-01 -2.647937e-01 -2.652008e-01 -2.655730e-01
## U2
              3.637193e-01 3.639081e-01 3.640851e-01 3.642442e-01
## Wealth
              2.340725e-01 2.345001e-01 2.348841e-01 2.352350e-01
              7.272184e-01 7.272832e-01 7.273472e-01 7.274019e-01
## Ineq
## Prob
              -2.784360e-01 -2.789692e-01 -2.794429e-01 -2.798812e-01
## Time
              -5.508981e-02 -5.567007e-02 -5.618447e-02 -5.666082e-02
## (Intercept) -1.628821e-16 -1.614254e-16 -1.599722e-16 -1.588429e-16
              2.854997e-01 2.854881e-01 2.854751e-01 2.854717e-01
## So
                                                       -1.272354e-04
## Ed
              5.383064e-01 5.387287e-01 5.391318e-01 5.394732e-01
## Po1
               1.385723e+00 1.390974e+00 1.396199e+00 1.400532e+00
## Po2
              -6.881507e-01 -6.938468e-01 -6.994970e-01 -7.042016e-01
## LF
              -6.155628e-02 -6.194199e-02 -6.231340e-02 -6.267794e-02
## M.F
              1.326692e-01 1.326590e-01 1.326421e-01 1.326530e-01
## Pop
              -7.181216e-02 -7.183203e-02 -7.185201e-02 -7.186545e-02
## NW
              1.039684e-01 1.043361e-01 1.046948e-01 1.050429e-01
## U1
              -2.659129e-01 -2.662179e-01 -2.665016e-01 -2.667971e-01
              3.643876e-01 3.645229e-01 3.646409e-01 3.647735e-01
## U2
## Wealth
              2.355529e-01 2.358389e-01 2.361070e-01 2.363407e-01
## Ineq
              7.274482e-01 7.274996e-01 7.275368e-01 7.276124e-01
## Prob
              -2.802845e-01 -2.806348e-01 -2.809747e-01 -2.812518e-01
## Time
              -5.709938e-02 -5.747880e-02 -5.784903e-02 -5.817274e-02
# Lasso cross validation
model.lasso.cv = cv.glmnet(x = x, y = y,
                     family = 'gaussian', alpha = 1, nfolds = 5)
#Results
#suggest between 5 to 12 coerfficients
plot(model.lasso.cv, xvar="lambda")
```

15 15 15 15 13 12 12 12 11 9 7 5 4 1 1 1 0



model.lasso.cv\$lambda.min

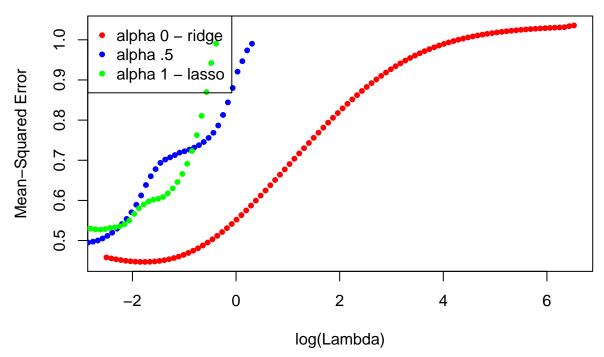
[1] 0.01134726

model.lasso.cv\$lambda.1se

[1] 0.08785769

coef(model.lasso.cv, s = model.lasso.cv\$lambda.min) #best coefficients

```
## 16 x 1 sparse Matrix of class "dgCMatrix"
## (Intercept) -3.152844e-16
## M
                2.632526e-01
## So
                4.240729e-02
## Ed
                4.354745e-01
## Po1
                7.687395e-01
## Po2
## LF
                1.380001e-01
## M.F
## Pop
               -3.723288e-02
## NW
                3.297085e-02
## U1
               -1.680174e-01
## U2
                2.799004e-01
## Wealth
                1.153505e-01
                6.180932e-01
## Ineq
## Prob
               -2.275193e-01
## Time
```



$\mathbf{Q2}$

To determine if which type of music to listen when a person drive to home after work reduce stress. I suggest to evaluate if the driver start drives agressive, temperature, if taking longer than usual to arrive some destination (with gps historial data), car smell. We could evaluate to start playlist to calm down and manipulate car temperature and car smell.

$\mathbf{Q3}$

```
library('FrF2')
```

Loading required package: DoE.base

```
## Loading required package: grid
## Loading required package: conf.design
##
## Attaching package: 'DoE.base'
## The following objects are masked from 'package:stats':
##
##
                              aov, lm
## The following object is masked from 'package:graphics':
##
##
                              plot.design
## The following object is masked from 'package:base':
##
                              lengths
library(knitr)
features <- c('Feature 1', 'Feature 2', 'Feature 3', 'Feature 4', 'Feature 5', 'Feature 6', 'Feature 7', 'Feature 7', 'Feature 5', 'Feature 6', 'Feature 7', 'Feature 8', 'Fea
experiment <- FrF2(nruns = 16, factor.names = features, default.levels = c("include", "not include"))</pre>
kable(experiment, caption = "Experiment Features")
```

Table 1: Experiment Features

Feature.1	Feature.2	Feature.3	Feature.4	Feature.5	Feature.6	Feature.7	Feature.8	Feature.9
not include								
include	include	include	not include	not include	not include	not include	include	not include
not include	include	include	not include	include	include	not include	not include	not include
not include	include	not include	include	include	not include	include	include	not include
not include	include	include	include	include	include	not include	include	include
include	not include	include	not include	include	not include	include	include	include
include	not include	include	include	include	not include	include	not include	not include
include	include	not include	not include	not include	include	include	include	include
include	include	include	include	not include	not include	not include	not include	include
include	not include	not include	not include	include	include	not include	include	not include
not include	not include	include	not include	not include	include	include	not include	include
not include	not include	include	include	not include	include	include	include	not include
include	not include	not include	include	include	include	not include	not include	include
not include	not include	not include	include	not include	not include	not include	include	include
include	include	not include	include	not include	include	include	not include	not include
not include	include	not include	not include	include	not include	include	not include	include
### Q4								

a. Binomial: The number of successful sales calls

- b. Geometric: Expected number of trade win before a bad trade with a robot system
- c. Poisson: The daily number of emergency calls in Dallas $\,$
- d. Exponential: The length of time between arrivals at a service station
- e. Weibull