

## Exercise 6.3.1

Convert the grammar

$$S \rightarrow 0s1 \mid A$$

$$A \rightarrow as \mid bs \mid a$$

to a PDA that accepts the same language by empty stack.

$$PDA = (\{q\}, \{0,1\}, \{0,1, A, s\}, \delta, q, s)$$

$$\delta : \begin{aligned} 1) & \delta(q, \epsilon, s) = \{(q, 0s1), (q, A)\} \\ 2) & \delta(q, \epsilon, A) = \{(q, 1A0), (q, s), (q, \epsilon)\} \\ 3) & \delta(q, 0, 0) = \{(q, \epsilon)\} \\ 4) & \delta(q, 1, 1) = \{(q, \epsilon)\} \end{aligned}$$

## Exercise 6.3.2

Convert the grammar

$$S \rightarrow aAA$$

$$A \rightarrow as \mid bs \mid a$$

to a PDA that accepts the same language by empty stack.

$$PDA = (\{q\}, \{a,b\}, \{a,b, A, s\}, \delta, q, s)$$

$$\delta : \begin{aligned} 1) & \delta(q, \epsilon, s) = \{(q, aAA)\} \\ 2) & \delta(q, \epsilon, A) = \{(q, as), (q, bs), (q, a)\} \\ 3) & \delta(q, a, a) = \{(q, \epsilon)\} \\ 4) & \delta(q, b, b) = \{(q, \epsilon)\} \end{aligned}$$

## Exercise 6.3.3

Convert the PDA  $P = (\{r, q\}, \{0,1\}, \{x, z_0\}, \delta, q, z_0)$  to a CFE, if  $\delta$  is given by :

$$1) \delta(q, 1, z_0) = \{(q, xz_0)\}$$

$s$  = start string

$\epsilon$  = empty string

$z = z_0$

in  $s \rightarrow [qzq] \mid [qzp]$

$$- [qzq] \rightarrow 1 [qxq] [qzq]$$

$$- [qzq] \rightarrow 1 [qxp] [pzq]$$

$$- [qzp] \rightarrow 1 [qxq] [qzq]$$

$$- [qzp] \rightarrow 1 [qxp] [pzp]$$

$$2) \delta(q, 1, x) = \{(q, xx)\}$$

$s$  = start string

$\epsilon$  = empty string

$z = z_0$

in  $s \rightarrow [qzq] \mid [qzp]$

$$- [qxq] \rightarrow 1 [qxq] [qxq]$$

$$- [qxq] \rightarrow 1 [qxp] [pxq]$$

$$- [qxp] \rightarrow 1 [qxq] [qxp]$$

$$- [qxp] \rightarrow 1 [qxp] [pxp]$$



$$3) \delta(q, 0, x) = \{(p, x)\}$$

$s$  = start string

$e$  = empty string

$z = z_0$

$$\text{in } s \rightarrow [qzq] \mid [qzp]$$

$$- [qxq] \rightarrow 0 [pxq]$$

$$- [qxp] \rightarrow 0 [pxp]$$

$$4) \delta(q, \varepsilon, x) = \{(q, \varepsilon)\}$$

$s$  = start string

$e$  = empty string

$z = z_0$

$$\text{in } s \rightarrow [qzq] \mid [qzp]$$

$$- [qxq] \rightarrow \varepsilon$$

$$5) \delta(p, 1, x) = \{(p, \varepsilon)\}$$

$s$  = start string

$e$  = empty string

$z = z_0$

$$\text{in } s \rightarrow [qzq] \mid [qzp]$$

$$- [pxp] \rightarrow 1$$

$$6) \delta(p, 0, z_0) = \{(q, z_0)\}$$

$s$  = start string

$e$  = empty string

$z = z_0$

$$\text{in } s \rightarrow [qzq] \mid [qzp]$$

$$- [pzp] \rightarrow 0 [qzq]$$

$$- [pzp] \rightarrow 0 [qzp]$$