

PR 3 TBFO

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Exercise 2.5.1

consider the following ϵ -NFA

	ϵ	a	b	c
$\rightarrow p$	\emptyset	$\{p\}$	$\{q\}$	$\{r\}$
q	$\{p\}$	$\{q\}$	$\{r\}$	\emptyset
$*r$	$\{q\}$	$\{r\}$	\emptyset	$\{p\}$

a) ϵ -closure for each state

$$\epsilon \text{ closure } (p) = \{p\}$$

$$\epsilon \text{ closure } (q) = \{p, q\}$$

$$\epsilon \text{ closure } (r) = \{p, q, r\}$$

b) Give all the strings of length three or less accepted by the automaton

	a	b	c
$\rightarrow p$	$\{p\}$	$\{p, q\}$	$\{p, q, r\}$
q	$\{p, q\}$	$\{p, q, r\}$	$\{p, q, r\}$
$*r$	$\{p, q, r\}$	$\{p, q, r\}$	$\{p, q, r\}$

→ Table NFA

Inputs :

Length 1 : c

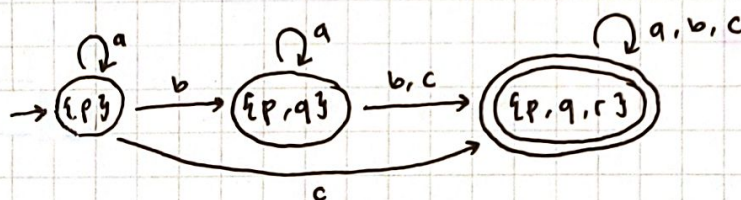
Length 2 : a-c, b-b, b-c, c-b, c-c, c-a

Length 3 : semua string dgn max input 'a' 1 kali

semua string dgn min input 'c' 2 kali dan 'a' 1 kali

c) Convert the automaton to a DFA

	a	b	c
$\rightarrow p$	$\{p\}$	$\{p, q\}$	$\{p, q, r\}$
$\{p, q\}$	$\{p, q\}$	$\{p, q, r\}$	$\{p, q, r\}$
$*\{p, q, r\}$	$\{p, q, r\}$	$\{p, q, r\}$	$\{p, q, r\}$



Exercise 2.5.2

	ϵ	a	b	c
$\rightarrow p$	$\{q, r\}$	\emptyset	$\{q\}$	$\{r\}$
q	\emptyset	$\{p\}$	$\{r\}$	$\{p, q\}$
r	\emptyset	\emptyset	\emptyset	\emptyset

a) Compute ϵ -closure of each state

$$\epsilon \text{ closure } (p) = \{p, q, r\}$$

$$\epsilon \text{ closure } (q) = \{q\}$$

$$\epsilon \text{ closure } (r) = \{r\}$$

b) Give all strings of length three or less accepted by automaton

	a	b	c
$\rightarrow p$	$\{p, q, r\}$	$\{q, r\}$	$\{p, q, r\}$
q	$\{p, q, r\}$	$\{r\}$	$\{p, q, r\}$
r	\emptyset	\emptyset	\emptyset

\rightarrow Table NFA

Inputs :

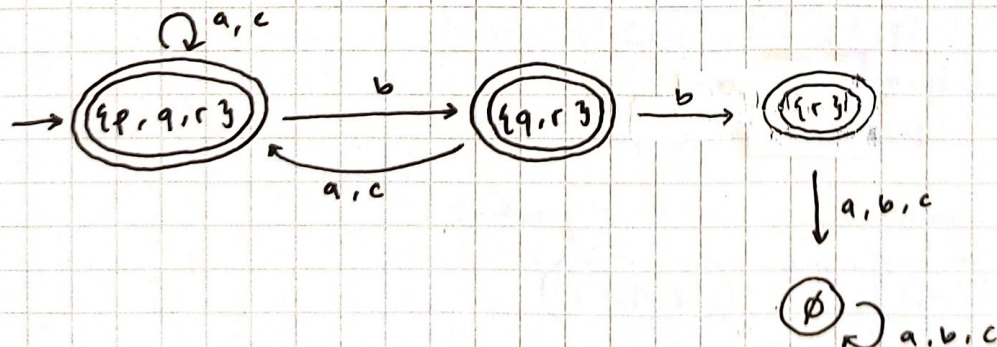
length 1 : a, b, c

length 2 : semua set string dgn panjang 2

length 3 : semua set string dgn panjang 3 kecuali yg dimulai dengan $b-b$ ($b-b-a, b-b-b, b-b-c$)

c) Convert the automaton to DFA

	a	b	c
$\rightarrow \epsilon^* \{p, q, r\}$	$\{p, q, r\}$	$\{q, r\}$	$\{p, q, r\}$
$\epsilon^* \{q, r\}$	$\{p, q, r\}$	$\{r\}$	$\{p, q, r\}$
$\epsilon^* \{r\}$	\emptyset	\emptyset	\emptyset
\emptyset	\emptyset	\emptyset	\emptyset

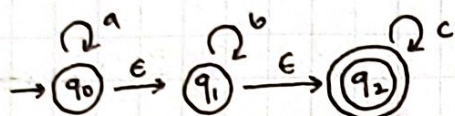


Exercise 1.5.3

Design ϵ -NFA's for the following languages

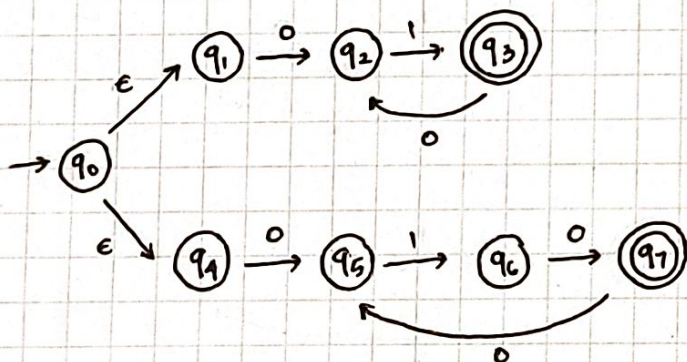
- a) The set of strings consisting of zero or more a's followed by zero or more b's, followed by zero or more c's.

	ϵ	a	b	c
$\rightarrow q_0$	q_1	q_0	\emptyset	\emptyset
q_1	q_2	\emptyset	q_1	\emptyset
$*q_2$	\emptyset	\emptyset	\emptyset	q_2



- b) set of strings that consist of either 01 repeated one or more times or 010 repeated one or more times

	ϵ	0	1
$\rightarrow q_0$	$\{q_1, q_4\}$	\emptyset	\emptyset
q_1	\emptyset	q_2	\emptyset
q_2	\emptyset	\emptyset	q_3
$*q_3$	\emptyset	q_2	\emptyset
q_4	\emptyset	q_5	\emptyset
q_5	\emptyset	\emptyset	q_6
q_6	\emptyset	q_7	\emptyset
$*q_7$	\emptyset	q_5	\emptyset



c) Set of strings of 0's and 1's such that at least one of the last ten positions is a 1.

	ϵ	0	1
$\rightarrow q_0$	\emptyset	q_0	$\{q_0, q_1\}$
q_1	q_2	q_2	q_2
q_2	q_3	q_3	q_3
q_3	q_4	q_4	q_4
q_4	q_5	q_5	q_5
q_5	q_6	q_6	q_6
q_6	q_7	q_7	q_7
q_7	q_8	q_8	q_8
q_8	q_9	q_9	q_9
q_9	q_{10}	q_{10}	q_{10}
$*q_{10}$	\emptyset	\emptyset	\emptyset

