

LOGKOM

PROOF METHOD & PROPOSITIONAL RESOLUTION

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① Premises :

1) $\text{malas} \wedge \text{bolos} \rightarrow \sim \text{lulus}$

2) $\sim \text{lulus} \rightarrow \text{marah}$

3) $\text{bolos} \wedge \sim \text{marah}$

Conclusion : $\sim \text{malas}$

Proof :

4) Hypothetical syllogism 1, 2

$$\text{malas} \wedge \text{bolos} \rightarrow \sim \text{lulus}$$

$$\sim \text{lulus} \rightarrow \text{marah}$$

$$\text{malas} \wedge \text{bolos} \rightarrow \text{marah}$$

5) Simplification 3

$$\text{bolos} \wedge \sim \text{marah}$$

$$\sim \text{marah}$$

6) Modus Tollens 4, 5

$$\text{malas} \wedge \text{bolos} \rightarrow \text{marah}$$

$$\sim \text{marah}$$

$$\sim (\text{malas} \wedge \text{bolos})$$

7) De Morgan's Law 6

$$\sim (\text{malas} \wedge \text{bolos}) \leftrightarrow \sim \text{malas} \vee \sim \text{bolos}$$

8) Simplification 3

$$\text{bolos} \wedge \sim \text{marah}$$

$$\text{bolos}$$

9) Disjunctive syllogism 7, 8

$$\sim \text{malas} \vee \sim \text{bolos}$$

$$\text{bolos}$$

$$\sim \text{malas}$$

\therefore proven that the conclusion is correct, $\sim \text{malas}$.

2) Prove $\{p \rightarrow q, q \rightarrow r\} \models (q \rightarrow r) \rightarrow ((p \rightarrow \sim r) \rightarrow \sim p)$

a) Validity checking

$$((p \rightarrow q) \wedge (q \rightarrow r)) \rightarrow ((q \rightarrow r) \rightarrow ((p \rightarrow \sim r) \rightarrow \sim p))$$

Final

p	q	r	$p \rightarrow q$	\wedge	$q \rightarrow r$	\rightarrow	$q \rightarrow r$	\rightarrow	$p \rightarrow \sim r$	\rightarrow	$\sim p$
T	F	F	F	F	T	T	T	F	T	F	F
F	F	F	T	T	T	T	T	T	T	T	T
T	T	F	T	F	F	T	F	T	T	F	F
F	T	F	T	F	F	T	F	T	T	T	T
T	F	T	F	F	T	T	T	T	F	T	F
F	F	T	T	T	T	T	T	T	T	T	T
T	T	T	T	T	T	T	T	T	F	T	F
F	T	T	T	T	T	T	T	T	T	T	T

valid

Karena hasil $((p \rightarrow q) \wedge (q \rightarrow r)) \rightarrow ((q \rightarrow r) \rightarrow ((p \rightarrow \sim r) \rightarrow \sim p))$ bernilai true semua dgn menggunakan validation checking, maka disimpulkan statement tsb valid.

$$\therefore \{p \rightarrow q, q \rightarrow r\} \models (q \rightarrow r) \rightarrow ((p \rightarrow \sim r) \rightarrow \sim p)$$

b) Unsatisfiability checking

$$((p \rightarrow q) \wedge (q \rightarrow r)) \wedge \sim ((q \rightarrow r) \rightarrow ((p \rightarrow \sim r) \rightarrow \sim p))$$

Final

p	q	r	$p \rightarrow q$	\wedge	$q \rightarrow r$	\wedge	$q \rightarrow r$	\sim	$p \rightarrow \sim r$	\rightarrow	$\sim p$
T	F	F	F	F	T	F	T	T	T	F	F
F	F	F	T	T	T	F	T	F	T	T	T
T	T	F	T	F	F	F	F	T	T	F	F
F	T	F	T	F	F	F	F	T	T	T	T
T	F	T	F	F	T	F	T	F	F	T	F
F	F	T	T	T	T	F	T	F	T	T	T
T	T	T	T	T	T	F	T	F	F	T	F
F	T	T	T	T	T	F	T	F	T	T	T

unsatisfiable

Karena hasil $((p \rightarrow q) \wedge (q \rightarrow r)) \wedge \sim ((q \rightarrow r) \rightarrow ((p \rightarrow \sim r) \rightarrow \sim p))$ bernilai false semua dgn menggunakan unsatisfiability checking, maka disimpulkan statement tsb unsatisfiable.

$$\therefore \{p \rightarrow q, q \rightarrow r\} \models (q \rightarrow r) \rightarrow ((p \rightarrow \sim r) \rightarrow \sim p)$$

- ② c) Axiom Schemata, Rule of Inference (without Deduction Theorem)
 $\{p \rightarrow q, q \rightarrow r\} \vdash (q \rightarrow r) \rightarrow ((p \rightarrow \sim r) \rightarrow \sim p)$

Premises: 1) $p \rightarrow q$
 2) $q \rightarrow r$

Conclusion: $(q \rightarrow r) \rightarrow ((p \rightarrow \sim r) \rightarrow \sim p)$

Proof:

1) $p \rightarrow q$	Premise
2) $q \rightarrow r$	Premise
3) $(q \rightarrow r) \rightarrow (p \rightarrow (q \rightarrow r))$	Implication introduction 2
4) $p \rightarrow (q \rightarrow r)$	Modus Ponens 2, 3
5) $(p \rightarrow (q \rightarrow r)) \rightarrow ((p \rightarrow q) \rightarrow (p \rightarrow r))$	Implication distribution 4
6) $(p \rightarrow q) \rightarrow (p \rightarrow r)$	Modus Ponens 4, 5
7) $p \rightarrow r$	Modus Ponens 1, 6
8) $(p \rightarrow r) \rightarrow ((p \rightarrow \sim r) \rightarrow \sim p)$	Contradiction Realization 7
9) $(p \rightarrow \sim r) \rightarrow \sim p$	Modus Ponens 7, 8
10) $((p \rightarrow \sim r) \rightarrow \sim p) \rightarrow ((q \rightarrow r) \rightarrow ((p \rightarrow \sim r) \rightarrow \sim p))$	Implication introduction 9
11) $(q \rightarrow r) \rightarrow ((p \rightarrow \sim r) \rightarrow \sim p)$	Modus Ponens 9, 10

$\therefore \{p \rightarrow q, q \rightarrow r\} \vdash (q \rightarrow r) \rightarrow ((p \rightarrow \sim r) \rightarrow \sim p)$

- ⑤ Use propositional resolution to show that the following sets of clauses are unsatisfiable.

a) $\{p, q\}, \{\sim p, r\}, \{\sim p, \sim r\}, \{p, \sim q\}$

1) $\{p, q\}$	premise
2) $\{\sim p, r\}$	premise
3) $\{\sim p, \sim r\}$	premise
4) $\{p, \sim q\}$	premise
5) $\{p\}$	1, 4
6) $\{\sim p\}$	2, 3
7) $\{\}$	5, 6

karena terbentuk himpunan kosong, maka terbukti clauses tsb unsatisfiable.

⑤ b) $\{p, q, \sim r, s\}, \{\sim p, r, s\}, \{\sim q, \sim r\}, \{p, \sim s\}, \{\sim p, \sim r\}, \{r\}$

1) $\{p, q, \sim r, s\}$	premise
2) $\{\sim p, r, s\}$	premise
3) $\{\sim q, \sim r\}$	premise
4) $\{p, \sim s\}$	premise
5) $\{\sim p, \sim r\}$	premise
6) $\{r\}$	premise
7) $\{\sim q\}$	3, 6
8) $\{p, \sim r, s\}$	1, 7
9) $\{p, \sim r\}$	4, 8
10) $\{\sim r\}$	5, 9
11) $\{\}$	6, 10

Karena terbentuk himpunan kosong, terbukti clause tsb unsatisfiable.

⑥ Premises

- 1) $p \rightarrow q$
- 2) $\sim p \rightarrow \sim t$
- 3) $\sim s \rightarrow \sim r$
- 4) $q \rightarrow r$

conclusion : $t \rightarrow s$

Negated conclusion : $\sim (t \rightarrow s)$

Proof (Implications)

6) $\sim p \vee q$	premise
7) $p \vee \sim t$	premise
8) $s \vee \sim r$	premise
9) $\sim q \vee r$	premise
10) $\sim (\sim t \vee s)$	negated conclusion

Proof (Negation)

11) $\sim p \vee q$	premise
12) $p \vee \sim t$	premise
13) $s \vee \sim r$	premise
14) $\sim q \vee r$	premise
15) $t \wedge \sim s$	negated conclusion

Proof (Distribution)

16) $\sim p \vee q$	premise
17) $p \vee \sim t$	- " -
18) $s \vee \sim r$	- " -
19) $\sim q \vee r$	- " -
20) $t \wedge \sim s$	negated conclusion

⑥ Proof (Operators)

- 1) $\{ \sim p, q \}$
- 2) $\{ p, \sim t \}$
- 3) $\{ s, \sim r \}$
- 4) $\{ \sim q, r \}$
- 5) $\{ t \}, \{ \sim s \}$

premise

— " —

— " —

— " —

negated conclusion

Proportional Resolution

- 1) $\{ \sim p, q \}$
- 2) $\{ p, \sim t \}$
- 3) $\{ s, \sim r \}$
- 4) $\{ \sim q, r \}$
- 5) $\{ t \}$
- 6) $\{ \sim s \}$
- 7) $\{ p \}$
- 8) $\{ q \}$
- 9) $\{ r \}$
- 10) $\{ s \}$
- 11) $\{ \}$

premise

premise

premise

premise

negated conclusion

negated conclusion

2, 5

1, 7

4, 8

3, 9

6, 10

∴ Knn diperoleh himpunan kosong,
terbukti bahwa konklusi dr
premise tsb benar.

⑨ a) Premises :

- 1) $\sim b \wedge c$: Ang
- 2) $\sim a \rightarrow \sim c$: Beng
- 3) $c \wedge (\sim a \vee \sim b)$: Cing

b) Ang, Beng, Cing tdk bersalah $\rightarrow a, b, c$ True

Tabel Kebenaran

a	b	c	$\sim b \wedge c$	$\sim a \rightarrow \sim c$	$c \wedge (\sim a \vee \sim b)$
T	T	T	F	T	F

Pernyataan Ang & Cing False, maka Ang & Cing berbohong.

— " — Beng True, maka Beng jujur.

- 9) c) tdk bersalah \rightarrow jujur
bersalah \rightarrow bohong

final

a	b	c	$a \leftrightarrow (\sim b \wedge c)$	\wedge	$b \leftrightarrow (\sim a \rightarrow \sim c)$	\wedge	$c \leftrightarrow (c \wedge (\sim a \vee \sim b))$
T	F	F	F	F	F	F	T
F	F	F	T	F	F	F	T
T	T	F	F	F	T	F	T
F	T	F	T	T	T	T	T
T	T	T	F	F	T	F	F
F	T	T	T	F	F	F	T
T	F	T	T	F	F	F	T
F	F	T	F	F	T	F	T

True hanya 1

Nilai true didapatkan dari $a = F$, $b = T$, $c = F$;
maka disimpulkan bahwa Ang & Ceng berbohong, Beng jujur.

Perkataan Beng adlh jika Ang bersalah, maka Cing juga. Krn Beng jujur, maka Beng tdk bersalah. Dan krn perkataan Beng benar, maka disimpulkan bahwa Ang & Cing bersalah.