

Exercise 1.1.1

a) Suppose L is a reg language & k is pumping lemma constant

$$w = 0^n 1^n, n \geq 1$$

↳ For $w = xyz$, $|xy| \leq n$, therefore y consists only 0's

↳ For $k=0$, xz must be in L , but xz consists of fewer than n 0's & followed by n 1's, therefore $xz \notin L$

∴ L not regular language

b) Suppose L is a reg language & k is pumping lemma constant

$$w = "(n)"^n$$

↳ For $w = xyz$, $|xy| \leq n$, therefore y consists only "("'s

↳ For $k=0$, xz must be in L , but xz consists of fewer than n "("'s & followed by n ")"'s, therefore $xz \notin L$

∴ L not regular language

c) Suppose L is a reg language & k is pumping lemma constant

$$w = 0^n 1^n, n \geq 1$$

↳ For $w = xyz$, $|xy| \leq n$, therefore y consists only 0's

↳ For $k=0$, xz must be in L , but xz consists of fewer than n 0's, followed by 1 and n 0's, therefore $xz \notin L$

∴ L is not regular language

d) Suppose L is a reg language, $w = 0^n 1^m 2^n$, $m \neq n$ are arbitrary integers

↳ For $w = xyz$, $|xy| \leq n$, therefore y consists of only 0's

↳ For $k=0$, xz must be in L , but xz consists of fewer than n 0's followed by m 1's and n 2's, therefore $xz \notin L$

∴ L is not regular language

e) Suppose L is a reg language, $w = 0^n 1^m$, $n \leq m$

↳ For $w = xyz$, $|xy| \leq n$, therefore y consists only 0's

↳ For $k=m$, $xy^m z$ must be in L , but $xy^m z$ consists of more than m 0's & m 1's, therefore $xy^m z \notin L$

∴ L is not regular language

f) Suppose L is a reg language, $w = 0^n 1^{2n}$, $n \geq 1$

↳ For $w = xyz$, $|xy| \leq n$, therefore y consists only 0's

↳ For $k=0$, xz must be in L , but xz consists of fewer than n 0's & followed by $2n$ 1's, therefore $xz \notin L$

∴ L is not regular language.

Exercise 4.4.1

Table DFA to be minimized

	0	1
→ A	B	A
B	A	C
C	D	B
*D	D	A
E	D	F
F	G	E
G	F	G
H	G	D

a) Draw the table of distinguishabilities for this automaton

B	x						
C	x	x					
D	x	x	x				
E	x	x		x			
F	x		x	x	x		
G		x	x	x	x	x	
H	x	x	x	x	x	x	x
	A	B	C	D	E	F	G

↳ 0 Equivalence

{A, B, C, E, F, G, H}, {D}

↳ 1 Equivalence

{A, B, F, G}, {C, E}, {H}, {D}

↳ 2 Equivalence

{A, B}, {B, F}, {C, E}, {H}, {D}

↳ 3 Equivalence

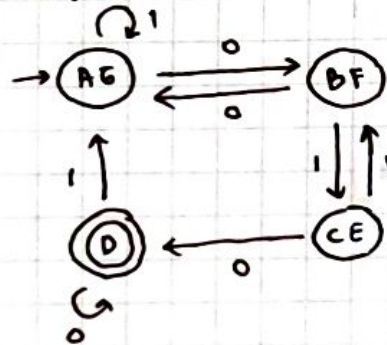
{A, G}, {B, F}, {C, E}, {H}, {D}

Lanjutan Exercise 4.4.1

b) Construct the minimum-state equivalent DFA

	0	1
→ AG	BF	AG
BF	AG	CE
CE	D	BF
D	D	AG

Diagram transisi



Exercise 4.4.2

Table DFA to be minimized

	0	1
→ A	B	E
B	C	F
*C	D	H
D	E	H
E	F	I
*F	G	B
G	H	B
H	I	C
*I	A	E

a) Draw the table of distinguishabilities for the automaton

B	x						
C	x	x					
D	.	x	x				
E	x	.	x	x			
F	x	x	.	x	x		
G	.	x	x	.	x	x	
H	x	.	x	x	.	x	x
I	x	x	.	x	x	.	x
A							

G 0 Equivalence

{A, B, D, E, G, H}, {C, F, I}

G 1 Equivalence

{A, D, G}, {B, E, H}, {C, F, I}

G 2 Equivalence

{A, D, G}, {B, E, H}, {C, F, I}

b) Construct the minimum-state equivalent DFA

	0	1
→ ADG	BEH	BEH
BEH	CFI	CFI
*CFI	ADG	BEH

