- 10.17 A new curing process developed for a certain type of cement results in a mean compressive strength of 5000 kilograms per square centimeter with a standard deviation of 120 kilograms. To test the hypothesis that  $\mu = 5000$  against the alternative that  $\mu < 5000$ , a random sample of 50 pieces of cement is tested. The critical region is defined to be  $\bar{x} < 4970$ .
- (a) Find the probability of committing a type I error when  $H_0$  is true.
- (b) Evaluate  $\beta$  for the alternatives  $\mu = 4970$  and  $\mu = 4960$ .
- 10.21 An electrical firm manufactures light bulbs that have a lifetime that is approximately normally distributed with a mean of 800 hours and a standard deviation of 40 hours. Test the hypothesis that  $\mu = 800$  hours against the alternative,  $\mu \neq 800$  hours, if a random sample of 30 bulbs has an average life of 788 hours. Use a P-value in your answer.

10.41 A study was conducted by the Department of Zoology at Virginia Tech to determine if there is a significant difference in the density of organisms at two different stations located on Cedar Run, a secondary stream in the Roanoke River drainage basin. Sewage from a sewage treatment plant and overflow from the Federal Mogul Corporation settling pond enter the stream near its headwaters. The following data give the density measurements, in number of organisms per square meter, at the two collecting stations:

Number of Organisms per Square Meter

realiser of organisms per square meter							
Stati	ion 1	Station 2					
5030	4980	2800	2810				
13,700	11,910	4670	1330				
10,730	8130	6890	3320				
11,400	$26,\!850$	7720	1230				
860	17,660	7030	2130				
2200	22,800	7330	2190				
4250	1130						
15,040	1690						

Can we conclude, at the 0.05 level of significance, that the average densities at the two stations are equal? Assume that the observations come from normal populations with different variances. 10.61 In a winter of an epidemic flu, the parents of 2000 babies were surveyed by researchers at a well-known pharmaceutical company to determine if the company's new medicine was effective after two days. Among 120 babies who had the flu and were given the medicine, 29 were cured within two days. Among 280 babies who had the flu but were not given the medicine, 56 recovered within two days. Is there any significant indication that supports the company's claim of the effectiveness of the medicine?

w tel:141%20359%20247%20940%20882 ypes of instruments yield measurements having the same variability. The readings in the following table were recorded for the two instruments.

Sunui Monoxide					
Instrument $B$					
0.87					
0.74					
0.63					
0.55					
0.76					
0.70					
0.69					
0.57					
0.53					

Assuming the populations of measurements to be approximately normally distributed, test the hypothesis that  $\sigma_A = \sigma_B$  against the alternative that  $\sigma_A \neq \sigma_B$ . Use a P-value.

10.77 An experiment was conducted to compare the alcohol content of soy sauce on two different production lines. Production was monitored eight times a day. The data are shown here.

Production line 1:

0.48 0.39 0.42 0.52 0.40 0.48 0.52 0.52 Production line 2:

0.38 0.37 0.39 0.41 0.38 0.39 0.40 0.39

Assume both populations are normal. It is suspected that production line 1 is not producing as consistently as production line 2 in terms of alcohol content. Test the hypothesis that  $\sigma_1 = \sigma_2$  against the alternative that  $\sigma_1 \neq \sigma_2$ . Use a *P*-value.

10.78 Hydrocarbon emissions from cars are known to have decreased dramatically during the 1980s. A study was conducted to compare the hydrocarbon emissions at idling speed, in parts per million (ppm), for automobiles from 1980 and 1990. Twenty cars of each model year were randomly selected, and their hydrocarbon emission levels were recorded. The data are as follows:

## 1980 models:

141 359 247 940 882 94 306 210 105 880 200 223 188 940 241 190 300 435 241 380 1990 models:

140 160 20 20 223 60 20 95 360 70 220 400 217 58 235 380 200 175 85 65

Test the hypothesis that  $\sigma_1 = \sigma_2$  against the alternative that  $\sigma_1 \neq \sigma_2$ . Assume both populations are normal. Use a P-value.

10.93 To determine current attitudes about prayer in public schools, a survey was conducted in four Virginia counties. The following table gives the attitudes of 200 parents from Craig County, 150 parents from Giles County, 100 parents from Franklin County, and 100 parents from Montgomery County:

	${f County}$				
Attitude	Craig	Giles	Franklin	Mont.	
Favor	65	66	40	34	
Oppose	42	30	33	42	
No opinion	93	54	27	24	

Test for homogeneity of attitudes among the four counties concerning prayer in the public schools. Use a P-value in your conclusion.