



Masayu Leylia Khodra

KK IF – Teknik Informatika – STEI ITB

Modul 3: Beyond Classical Search

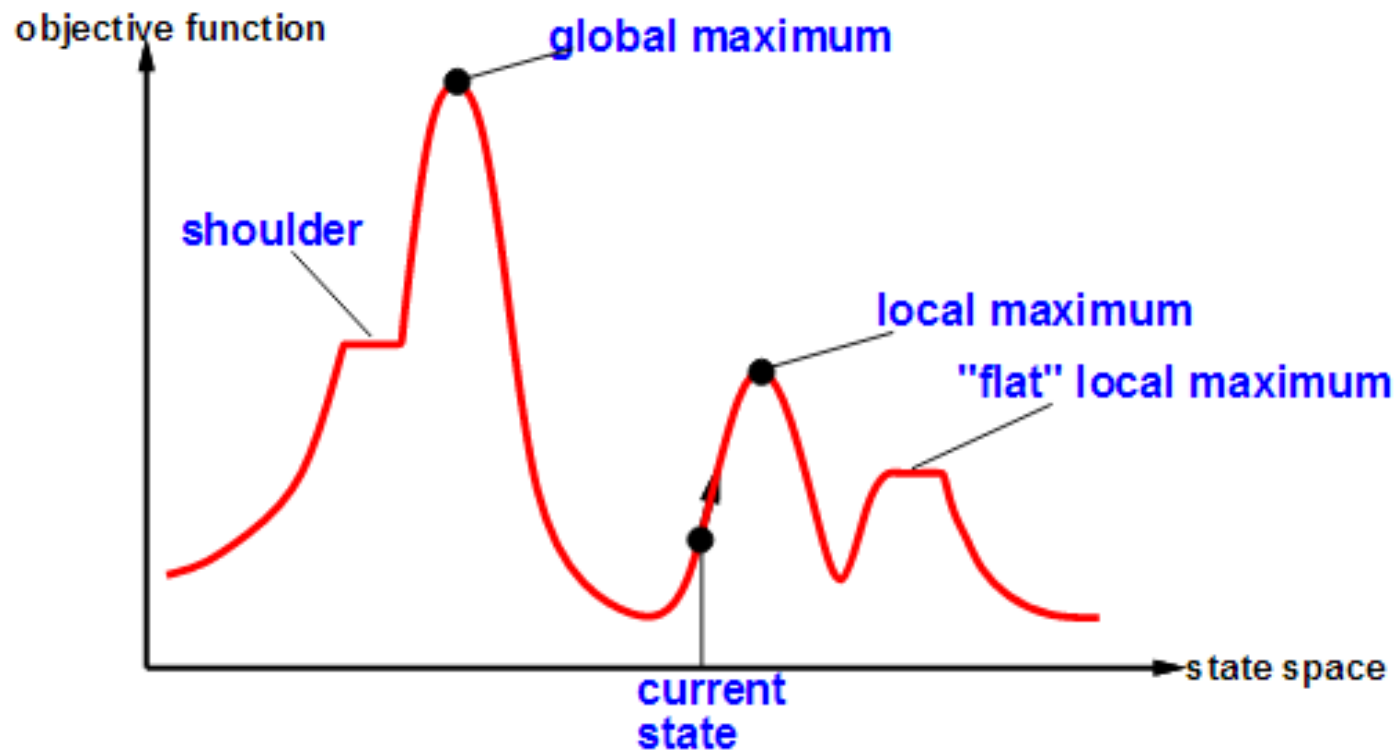
Hill-climbing Search

Inteligensi Buatan
(*Artificial Intelligence*)



Hill-climbing Search

“Like climbing Everest in thick fog with amnesia”



Starting from a randomly generated initial state

Loop that continually moves in the direction of increasing value (objective) or decreasing value (cost)

Terminates when it reaches a “peak” where no neighbor has a higher value



Hill-climbing Search: Steepest Ascent

(Russel & Norvig, 2010)

function HILL-CLIMBING(*problem*) **returns** a state that is a local maximum

current \leftarrow MAKE-NODE(*problem*.INITIAL-STATE)

loop do

neighbor \leftarrow a highest-valued successor of *current*

if *neighbor*.VALUE \leq *current*.VALUE **then return** *current*.STATE

current \leftarrow *neighbor*

Starting from a
randomly generated
initial state

Loop that continually
moves in the direction of
increasing value (objective)
or decreasing value (cost)

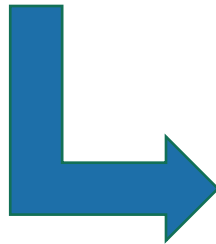
Terminates when it reaches
a “**peak**” including “**flat**”
where no neighbor has a
higher value



Hill-climbing: Illustration

$h=-3$

5	6	♔	6	5	6	♔	4
5	5	4	5	♔	5	4	4
6	♔	2	5	7	6	4	3
4	4	3	3	5	6	4	1
4	4	4	4	5	♔	5	3
6	6	4	♔	7	4	5	♔
4	4	2	3	4	4	3	2
♔	5	3	3	4	6	4	2

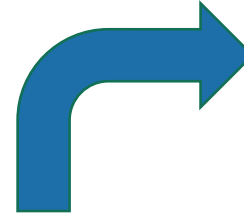


$Q8: 3 \rightarrow 5$

$h=-1$ ($Q8: 3 \rightarrow 5$)

3	4	♔	5	4	4	♔	4
3	3	3	3	♔	4	2	4
4	♔	1	4	4	4	3	3
2	3	3	3	4	4	3	♔
2	3	3	5	3	♔	3	3
3	3	2	♔	3	3	2	3
2	2	1	2	3	2	0	2
♔	3	2	3	2	3	2	2

$Q7: 8 \rightarrow 2$



$h=0$ ($Q7: 8 \rightarrow 2$)

2	2	♔	3	2	2	1	2
2	3	3	2	♔	2	2	2
3	♔	2	3	2	3	3	2
2	2	2	2	3	3	3	♔
1	2	2	3	2	♔	3	2
2	1	2	♔	3	3	2	3
1	2	2	2	2	2	♔	2
♔	2	2	2	1	3	2	2

stop in global optimum (solution)



Hill-climbing: Stuck In Local Optimum

18	12	14	13	13	12	14	14
14	16	13	15	12	14	12	16
14	12	18	13	15	12	14	14
15	14	14	♔	13	16	13	16
♔	14	17	15	♔	14	16	16
17	♔	16	18	15	♔	15	♔
18	14	♔	15	15	14	♔	16
14	14	13	17	12	14	12	18
Q1	Q2	Q3	Q4	Q5	Q6	Q7	Q8

6 step

Step 1: $h=-17 \rightarrow h=-12$
 Step 2: $h=-12 \rightarrow h=-7$
 Step 3: $h=-7 \rightarrow h=-4$
 Step 4: $h=-4 \rightarrow h=-3$
 Step 5: $h=-3 \rightarrow h=-1$
 Step 6: $h=-1$ stop

						♔	
				♔			
	♔						
			♔				
					♔		
							♔
		♔					
♔							
Q1	Q2	Q3	Q4	Q5	Q6	Q7	Q8



Hill-climbing for 8-Queen Problem

function HILL-CLIMBING(*problem*) **returns** a state that is a local maximum

current \leftarrow MAKE-NODE(*problem*.INITIAL-STATE)

loop do

neighbor \leftarrow a highest-valued successor of *current*

if *neighbor*.VALUE \leq *current*.VALUE **then return** *current*.STATE

current \leftarrow *neighbor*

State space:
 $8^8 \approx 16.8$ million states

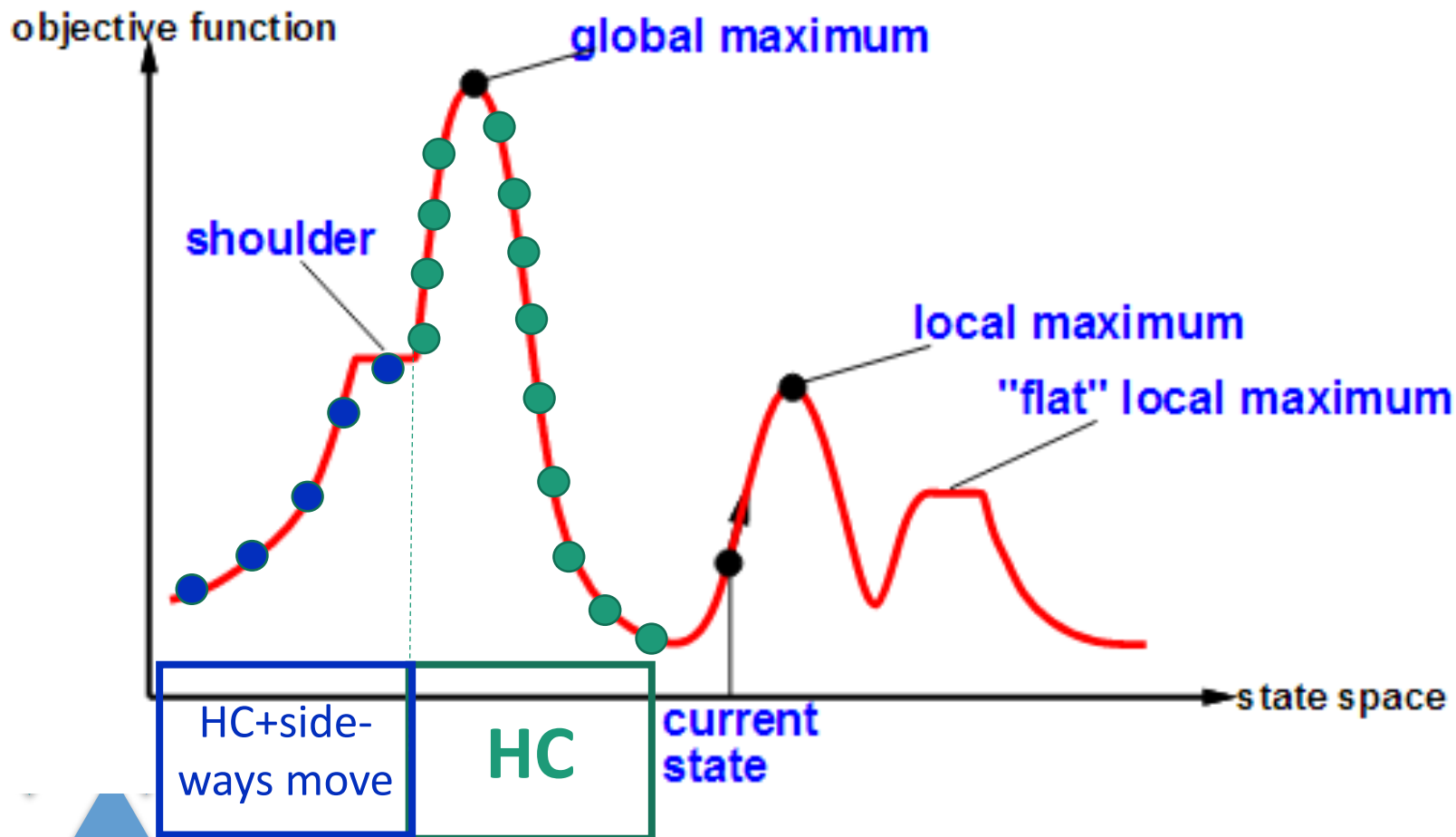
Average case: works quickly
when **success**: avg 4 steps
when **stuck**: avg 3 steps

Best case:
initial state = goal state
Prob: $92 / 8^8 = 0.00054\%$

Get **stuck** 86%,
solving only 14% of
problem instances



Hill-climbing Search: Final State



Success: global maximum

Stuck: 1) local maximum, 2) flat local maximum, 3) shoulder

Shoulder: still possible to global max.
Variant HC: + **sideways move** with limit on number of consecutive ways



bolehin tetangga nilainya sama, jd an langsung berhenti

Variant 1: Hill-climbing with Sideways Move

function HILL-CLIMBING(*problem*) **returns** a state that is a local maximum

current \leftarrow MAKE-NODE(*problem*.INITIAL-STATE)

loop do

neighbor \leftarrow a highest-valued successor of *current*

if *neighbor*.VALUE $<$ *current*.VALUE **then return** *current*.STATE

current \leftarrow *neighbor*

Terminates when it reaches a “peak”
~~including “flat”~~

Increase success for 8-queens problem.
Limit=100:
14% \rightarrow 94% success

Works **slower**:
when **success**: avg 4 \rightarrow 21 steps
when **stuck**: avg 3 \rightarrow 64 steps



cara kesama persis dgn
steepest tp din
regulang 2.

Variant 2: Random Restart Hill-climbing

QOTD

If at first you don't succeed, try, try again. It conducts **a series of hill climbing** searches (random initial states, until a goal is found)



Expected nb of restarts = $1/p \rightarrow p=0.14$: 7 restart
Expected nb of steps = $s + f(1-p)/p \rightarrow p=0.14, s=4, f=3$: 22 steps.

Very effective for n-queens problem: solving 3 million queens in under a minute (Luby et al., 1993)



hanya membangkitkan 1
successor secara random.

Variant 3: Stochastic Hill-climbing

cek nilai tetangga
lebih bagus.

kalah worse (\leq), statenya
tetap
selama
iterasinya
belum
sampai
nmax.

function HILL-CLIMBING(*problem*) **returns** a state that is a local maximum

current \leftarrow MAKE-NODE(*problem*.INITIAL-STATE)

repeat *nmax* **times**

neighbor \leftarrow a **random** successor of *current*

if *neighbor*.VALUE **>** *current*.VALUE **then** *current* \leftarrow *neighbor*

Terminates
when it reaches
nmax iteration

Generating a
successor randomly
(**not all** successor)

Move to neighbor
if it is better than
current state.

Works **slower**
(more steps)



Summary: Hill-climbing

continually moves in the direction of increasing value (objective) or decreasing value (cost)

Depending on initial state, can get stuck in local maxima.

Variant: steepest ascent HC, HC with sideways move, stochastic HC, random restart HC

Next:

- Simulated annealing



THANK YOU

