

Searching

Kuan-Yu Chen (陳冠宇)

2018/10/31 @ TR-212, NTUST

Review

- A B+ tree is a variant of a B tree
 - A B tree can store both keys and records in its interior nodes
 - A B+ tree stores all the records at the leaf level of the tree and keys are stored in the interior nodes
- In a 2-3 tree, each interior node has either two or three children
 - All the leaf nodes are at the same level

Searching

- Searching means to find whether a particular value is present in an array or not
- There are two popular methods for searching the array elements: **linear search** and **binary search**
 - The algorithm that should be used depends entirely on how the values are organized in the array
 - For example, if the elements of the array are arranged in ascending order, then binary search should be used

Linear Search

- Linear search, also called as **sequential search**, is a very simple method used for searching an array for a particular value
 - It works by comparing the value to be searched with every element of the array one by one in a sequence until a match is found
 - It is mostly used to search an unordered list of elements

LINEAR_SEARCH(A, N, VAL)

Step 1: [INITIALIZE] SET POS = -1

Step 2: [INITIALIZE] SET I = 1

Step 3: Repeat Step 4 while I ≤ N

Step 4: IF A[I] = VAL

SET POS = I

PRINT POS

Go to Step 6

[END OF IF]

SET I = I + 1

[END OF LOOP]

Step 5: IF POS = -1

PRINT "VALUE IS NOT PRESENT
IN THE ARRAY"

[END OF IF]

Step 6: EXIT

Binary Search

- Binary search is a searching algorithm that works efficiently with a **sorted** list
 - Initially, $BEG = \text{lower_bound}$, $END = \text{upper_bound}$, and $POS = MID$
 - If VAL is not equal to $A[MID]$, then the values of BEG , END , and MID will be changed depending on whether VAL is smaller or greater than $A[MID]$
 - If $VAL < A[MID]$, then VAL will be present in the left segment of the array
The value of END will be changed as $END = MID - 1$
 - If $VAL > A[MID]$, then VAL will be present in the right segment of the array
The value of BEG will be changed as $BEG = MID + 1$

Example

- For a data array, please find 9

`int A[] = {0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10}`

- Step1: $BEG = 0$, $END = 10$, $MID = (0 + 10)/2 = 5$
 - $A[MID] = A[5] = 5$
- Step2: $BEG = MID + 1 = 6$, $END = 10$, $MID = (6 + 10)/2 = 16/2 = 8$
 - $A[MID] = A[8] = 8$
- Step3: $BEG = MID + 1 = 9$, $END = 10$, $MID = (9 + 10)/2 = 9$
 - $A[MID] = A[9] = 9$

Binary Search – Algorithm

BINARY_SEARCH(A, lower_bound, upper_bound, VAL)

Step 1: [INITIALIZE] SET BEG = lower_bound

 END = upper_bound, POS = - 1

Step 2: Repeat Steps 3 and 4 while BEG <= END

Step 3: SET MID = (BEG + END)/2

Step 4: IF A[MID] = VAL

 SET POS = MID

 PRINT POS

 Go to Step 6

 ELSE IF A[MID] > VAL

 SET END = MID - 1

 ELSE

 SET BEG = MID + 1

 [END OF IF]

 [END OF LOOP]

Step 5: IF POS = -1

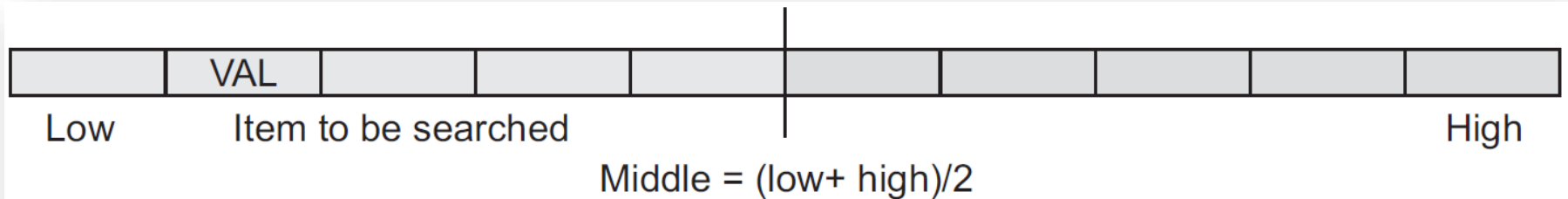
 PRINT "VALUE IS NOT PRESENT IN THE ARRAY"

 [END OF IF]

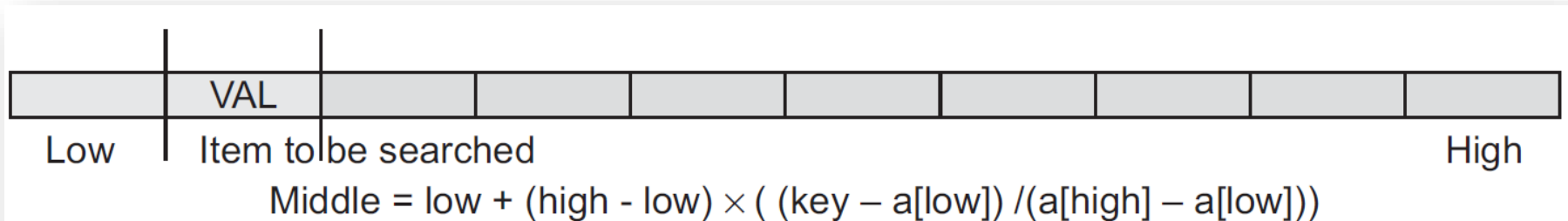
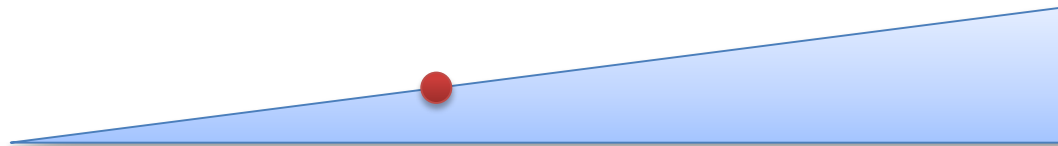
Step 6: EXIT

Interpolation Search

- Interpolation search, also known as extrapolation search, is a searching technique that finds a specified value in a sorted array
 - Interpolation search is similar to the binary search technique



- The major difference is how to select the middle value



Example

- Given a list of numbers, please search for value 19 using interpolation search technique

`a[] = {1, 3, 5, 7, 9, 11, 13, 15, 17, 19, 21}`

- Low = 0, High = 10, VAL = 19, a[Low] = 1, a[High] = 21
- Middle
$$= \text{Low} + (\text{High} - \text{Low}) \times ((\text{VAL} - \text{a}[\text{Low}]) / (\text{a}[\text{High}] - \text{a}[\text{Low}]))$$
$$= 0 + (10 - 0) \times ((19 - 1) / (21 - 1))$$
$$= 0 + 10 \times 0.9 = 9$$
- a[Middle] = a[9] = 19

Interpolation Search – Algorithm

INTERPOLATION_SEARCH (A, lower_bound, upper_bound, VAL)

```
Step 1: [INITIALIZE] SET LOW = lower_bound,
        HIGH = upper_bound, POS = -1
Step 2:   Repeat Steps 3 to 4 while LOW <= HIGH
Step 3:       SET MID = LOW + (HIGH - LOW) ×
              ((VAL - A[LOW]) / (A[HIGH] - A[LOW]))
Step 4:       IF VAL = A[MID]
               POS = MID
               PRINT POS
               Go to Step 6
             ELSE IF VAL < A[MID]
               SET HIGH = MID - 1
             ELSE
               SET LOW = MID + 1
             [END OF IF]
        [END OF LOOP]
Step 5: IF POS = -1
        PRINT "VALUE IS NOT PRESENT IN THE ARRAY"
      [END OF IF]
Step 6: EXIT
```

Jump Search

- When we have an already sorted list, then the other efficient algorithm to search for a value is jump search or block search
 - Given an array, please find value 8

$a[] = \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$

Step 1: First three elements are checked. Since 3 is smaller than 8, we will have to make a jump ahead

1	2	3	4	5	6	7	8	9
---	---	---	---	---	---	---	---	---

Step 2: Next three elements are checked. Since 6 is smaller than 8, we will have to make a jump ahead

1	2	3	4	5	6	7	8	9
---	---	---	---	---	---	---	---	---

Step 3: Next three elements are checked. Since 9 is greater than 8, the desired value lies within the current boundary

1	2	3	4	5	6	7	8	9
---	---	---	---	---	---	---	---	---

Step 4: A linear search is now done to find the value in the array.

Questions?



kychen@mail.ntust.edu.tw