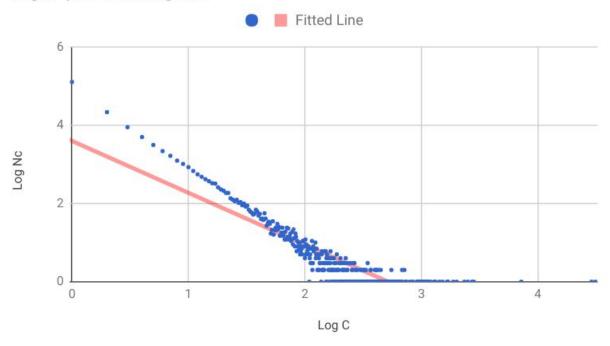
Log FF plot of training data



Question 2:

A)
$$C^* = (C + 1) (N_{c+1} / N_c)$$
 => $C^*_0 = (0 + 1) (N_1 / N_0) = N_1 / N_0$
If we use the conventional calculation for C^* we can then derive the N_1 / N estimation.
$$\sum_{x: count(x) = 0} P(x) = \sum_1^{N_0} [C^*_0 / N] = \sum_1^{N_0} [(N_1 / N_0) / N] = \sum_1^{N_0} [N_1 / (N^* N_0)] = N_1 / (N^* N_0)^* \sum_1^{N_0} [1] = (N_1 / (N^* N_0))^* N_0 = N_1 / N$$

B) The zero mass M_0 is calculated by multiplying the probability given to a zero count token $P(X_0)$ and the number of zero count tokens N_0

For Good Turing smoothing this is calculated as such:

$$P(X_0) = C_0^*/N$$

 $M_0 = N_0^*(C_0^*/N)$

For Laplacian smoothing:

$$P(X_0) = 1 / (N + |V|)$$

 $M_0 = N_0 * (1 / (N + |V|))$

Question 3.1:

A) The number of unseen bigrams N_0 can be found by squaring the number of unique unigrams $|V_{ij}|^2$ then subtracting the number of seen bigrams N.

$$N_0 = |V_u|^2 - N$$

I found the following
 $|V_u| = 21,779 \quad |V_u|^2 = 474,324,841$
 $N = 179,093$
 $N_0 = 474,145,748$

B) Good Turing:

$$\begin{split} &M_0 = N_{0^+} (C^*_{0} / |V_u|^2) \quad C^*_{0} = 0.18295146395320908 \\ &M_0 = 474,145,748 * (0.18295146395320908 / 474,324,841) = 0.18295146395320908 \\ &M_0 = \sim 18.3\% \end{split}$$

Laplacian:

$$\begin{aligned} &M_0 = N_0^* (1 / (N + |V_u|^2)) \\ &M_0 = 474,145,748 * (1 / (179,093 + 474,324,841)) = 0.998168130850942 \\ &M_0 = \sim 99.8\% \end{aligned}$$