The point types are:

2	2	2	2	2	2	2	2	2	1	1	1	0	0	0	0	0	0	0
4	3	3	3	3	3	3	3	3	3	3	3	1	1	0	0	0	0	0
4	3	3	3	3	3	3	3	3	3	3	3	3	3	1	1	0	0	0
4	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	1	0	0
4	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	1	0	0
4	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	1	0
4	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	1	0
4	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	1
4	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	7
6	5	5	5	5	5	5	5	5	5	5	5	5	5	5	5	5	5	8

The boundary condition on the curved edge is

$$\nabla T(x,y,t) \cdot n = -1 \quad \rightarrow \quad \frac{\partial T(x,y,t)}{\partial x} n_x + \frac{\partial T(x,y,t)}{\partial y} n_y = -1 \quad \rightarrow \quad \frac{\partial T_{j,k,i}}{\partial x} n_x + \frac{\partial T_{j,k,i}}{\partial y} n_y = -1$$

At points of type 1 using one sided differences this is:

$$\begin{split} &\frac{n_x}{2h}\left(T_{j,k-2,i}-4T_{j,k-1,i}+3T_{j,k,i}\right)+\frac{n_y}{2h}\left(-3T_{j,k,i}+4T_{j+1,k,i}-T_{j+2,k,i}\right)=-1\\ &\frac{3n_x}{2h}T_{j,k,i}-\frac{3n_y}{2h}T_{j,k,i}=-1+\frac{n_x}{2h}(4T_{j,k-1,i}-T_{j,k-2,i})+\frac{n_y}{2h}(T_{j+2,k,i}-4_{j+1,k,i})\\ &T_{j,k,i}=\left(\frac{3n_x-3n_y}{2h}\right)^{-1}\left(-1+\frac{n_x}{2h}(4T_{j,k-1,i}-T_{j,k-2,i})+\frac{n_y}{2h}(T_{j+2,k,i}-4_{j+1,k,i})\right) \end{split}$$

At points of type 7 using one sided differences this is:

$$\begin{split} \frac{n_x}{2h} \left(T_{j,k-2,i} - 4T_{j,k-1,i} + 3T_{j,k,i} \right) + \frac{n_y}{2h} \left(-4T_{j,k,i} + 4T_{j+1,k,i} \right) &= -1 \\ \frac{3n_x}{2h} T_{j,k,i} - \frac{4n_y}{2h} T_{j,k,i} &= -1 + \frac{n_x}{2h} (4T_{j,k-1,i} - T_{j,k-2,i}) - \frac{n_y}{2h} T_{j+1,k,i} \\ T_{j,k,i} &= \left(\frac{3n_x - 4n_y}{2h} \right)^{-1} \left(-1 + \frac{n_x}{2h} (4T_{j,k-1,i} - T_{j,k-2,i}) - \frac{n_y}{2h} T_{j+1,k,i} \right) \end{split}$$

At points of type 8 using one sided differences this is:

$$\frac{n_x}{2h} \left(T_{j,k-2,i} - 4T_{j,k-1,i} + 3T_{j,k,i} \right) = -1$$
$$T_{j,k,i} = -\frac{2h}{n_x} + 4T_{j,k-1,i} - T_{j,k-2,i}$$

The 2 dimensional discretization of the wave equation on an equally spaced grid is:

$$u_{i,j}^{k+1} = 2u_{i,j}^k - u_{i,j}^{k-1} + r\left(u_{i+1,j}^k + u_{i-1,j}^k + u_{i,j+1}^k + u_{i,j-1}^k - 4u_{i,j}^k\right)$$

where $h = \Delta x = \Delta y$ and

$$r = \left(\frac{H\Delta t^2}{\rho h^2}\right).$$

Substituting $u(x, y, t_n) = g(\xi)^n e^{I\xi xy}$ where $I = \sqrt{-1}$ yields:

$$g(\xi)^{k+1}e^{I\xi h^2ij} = 2g(\xi)^k e^{I\xi h^2ij} - g(\xi)^{k-1}e^{I\xi h^2ij} + rg(\xi)^k \left(e^{I\xi h^2(i+1)j} + e^{I\xi h^2(i-1)j} + e^{I\xi h^2i(j+1)} + e^{I\xi h^2i(j-1)} - 4e^{I\xi h^2ij}\right).$$

Dividing by $g(\xi)^{k-1}$ on both sides yields:

$$g(\xi)^2 e^{I\xi h^2 ij} = 2g(\xi) e^{I\xi h^2 ij} - e^{I\xi h^2 ij} + rg(\xi) \left(e^{I\xi h^2 (i+1)j} + e^{I\xi h^2 (i-1)j} + e^{I\xi h^2 i(j+1)} + e^{I\xi h^2 i(j-1)} - 4e^{I\xi h^2 ij} \right).$$

Dividing by $e^{I\xi h^2ij}$ on both sides yields:

$$\begin{split} g(\xi)^2 &= 2g(\xi) - 1 + rg(\xi) \left(e^{I\xi h^2} + e^{-I\xi h^2} + e^{I\xi h^2} + e^{-I\xi h^2} - 4 \right), \\ g(\xi)^2 &= 2g(\xi) - 1 + rg(\xi) \left(2e^{I\xi h^2} + 2e^{-I\xi h^2} - 4 \right), \\ g(\xi)^2 &= -1 + rg(\xi) \left(4\cos(\xi h^2) - 2 \right) \end{split}$$