

AT THE UNIVERSITY OF FREIBURG

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# Master Thesis

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## Abstract

A raw writing of hard sphere nucleation, a simulation to measure quantities, and an analysis of data generated by means of the simulation.

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# 1 Theory

## 1.1 Theory and Background

### 1.1.1 Hard sphere system

Explain the Hard sphere system and the first predictions of the phase transition

### 1.1.2 metastable fluid/ phase diagram

maybe include disperisty of radii

### 1.1.3 Classical nucleation theory :/

Estimate of  $r_{crit}$  by  $\Delta_\mu$

SOMehow this wshould be doable ;)

### 1.1.4 Computer Precision

Explain a little about what numerics does, compared to the real world.

Maybe include the time evolution of minimal changes

### 1.1.5 Comparsion to Real world experiments

Compare, regadring the solvent. Esspeically with Hajos finding.

## 2 Simulation details

### 2.1 Simulation

#### 2.1.1 Algorithm explanation

Explain the EDMD algorithm

#### 2.1.2 Simulation

Add Details of for example FEL, and backupevent handling, double time precision, reset sim

#### 2.1.3 Estimate of calculation times

Give some profiling numbers of the simulation Also conclude that missing q6q6  $O(N^2)$ , broke the walltime.

#### 2.1.4 Produced Data

Overview of produced data with visualized snapshot?

## **3 Data Analysis**

### **3.1 Data analysis**

This is the analysis part

#### **3.1.1 Diffusion of the liquid**

This contains analysis of diffusion in the liquid to prove the simulations accurate

#### **3.1.2 Diffusion of the metastable liquid**

This contains Diffusion constants to normalize the rates

#### **3.1.3 Cluster growth**

Cluster growth depending on density

#### **3.1.4 ToG**

Well only swamp here, but it can be shown to conclude the swamp.

#### **3.1.5 ACF largest cluster?**

Just in case anything can be seen here

#### **3.1.6 Induction time dilemma**

Evaluation of induction time. Problem with accuracy and precision. Compare methods.

#### **3.1.7 Induction time by exponential distribution**

Obtain exp assumption and best estimator

#### **3.1.8 Nucleation rate comparison**

All Nucleation rates that can be found.-> maybe ask Hajo.

### **3.1.9 Memory Kernels**

Memory kernels of systems at various densities. Depends strongly on what is found here



## 4 Conclusion - Summary

### 4.1 Conclusion

## **.1 appendix a**