Wind accretion in a circular binary system

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ABSTRACT

Commentary on Tejeda & Toalá (2025).

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1 INTRODUCTION

2 BINARY SYSTEM AND WIND PARAMETERS

Consider a binary system in which the secondary star with mass M_2 accretes from the wind of the primary star with mass M_1 . The orbit is assumed to be circular with separation r. The orbital speed of the secondary in the rest frame of the primary is v_0 . Kepler's laws gives the orbital period T as

$$T = 2\pi G(M_1 + M_2)/v_0^3 = 2\pi r/v_0.$$
 (1)

The isotropic stellar wind from the primary has mass-loss rate $\dot{M}_{\rm W}$ and hypersonic terminal velocity $v_{\rm W}$. The undisturbed wind density $\rho_{\rm W}$ at the position of the secondary is therefore

$$\rho_{\rm W} = \dot{M}_{\rm W}/4\pi r^2 v_{\rm W}.\tag{2}$$

The orbital velocity is purely tangential and thus perpendicular to the purely radial wind velocity. The relative speed between the wind and the secondary star is therefore

$$v_{\rm r} = \left(v_{\rm W}^2 + v_{\rm o}^2\right)^{1/2}.\tag{3}$$

The system is characterized by two dimensionless parameters:

Mass ratio:
$$q = M_2/(M_1 + M_2)$$
, (4)

Velocity ratio:
$$w \equiv v_{\rm W}/v_{\rm o}$$
. (5)

3 BONDI-HOYLE-LITTLETON ACCRETION

Following Hoyle & Lyttleton (1939); Bondi & Hoyle (1944), the mass accretion rate is

$$\dot{M}_{\rm acc} = \pi r_{\rm B}^2 v_{\rm r} \, \rho_{\rm w},\tag{6}$$

where

$$r_{\rm B} = 2GM_2/v_{\rm r}^2 \tag{7}$$

is the accretion radius. From equations (1, 3, 4, 5) we find that the ratio of the accretion radius to the orbital radius is

$$r_{\rm B}/r = 2q/(1+w^2)$$
. (8)

We define a dimensionless accretion efficiency as the fraction of the stellar wind that is captured by the secondary:

$$\eta_{\rm B} \equiv \dot{M}_{\rm acc} / \dot{M}_{\rm W},\tag{9}$$

which from equations (2, 6) yields

$$\eta_{\rm B} = \frac{1}{4} \left(\frac{v_{\rm r}}{v_{\rm w}} \right) \left(\frac{r_{\rm B}}{r} \right)^2. \tag{10}$$

The boost of the relative wind speed due to the orbital motion is

$$v_{\rm r}/v_{\rm W} = w^{-1} (1 + w^2)^{1/2},$$
 (11)

which combine with equations (10, 8) implies

$$\eta_{\rm B} = \frac{q^2}{w \left(1 + w^2\right)^{3/2}}.\tag{12}$$

The BHL analysis assumes that the wind density and velocity vector are constant over the entire accretion capture zone of radius $r_{\rm B}$. For accretion from a wind, this is only true in the limit that $r_{\rm B} \ll r$.

4 A PROBLEMATIC GEOMETRIC CORRECTION

Tejeda & Toalá (2025) point out an issue with equation (12) when the wind velocity is much smaller than the orbital velocity ($w \ll 1$): in the limit $w \to 0$ then $\eta_{\rm B} \to q^2/w$, which can become larger than unity. This is clearly non-physical since the mass accretion rate cannot exceed the wind mass-loss rate. They propose to remedy this deficiency by making a geometric correction to the mass accretion rate. $\dot{M}_{\rm acc}$ is multiplied by a factor of $\cos\theta$, where θ is the angle between the relative velocity vector and the radial direction from the primary, which accounts for

... the projected area of the accretion cylinder's cross section onto a sphere centered around the primary. This projection accounts for the effective area capturing the wind.

This yields a different equation for the accretion efficiency:

$$\eta_{\rm T} = \eta_{\rm B} = \left(\frac{q}{1+w^2}\right)^2. \tag{13}$$

This clearly resolves the issue mentioned above since as $w \to 0$ then $\eta_T \to q^2$, guaranteeing that $\eta_T < 1$. On the other hand, in the

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opposite limit of large wind velocity the two efficiencies agree: as $w \to \infty$ then $\eta_T \to \eta_B \to q^2/w^4$.

However, the physical basis for making this "correction" is unclear. Unlike the BHL theory, which is entirely local to the rest frame of the accreting secondary, the correction factor introduces quantities from the rest frame of the primary, which casts doubt on its validity.

For circular orbits $\cos \theta = v_{\rm W}/v_{\rm r}$, so an alternative way of writing the Tejeda efficiency is

$$\eta_{\rm T} = \frac{1}{4} \left(\frac{r_{\rm B}}{r} \right)^2 = \frac{\pi \, r_{\rm B}^2}{4\pi \, r^2},\tag{14}$$

which is simply the area covering factor of the BHL capture zone of a stationary accretor. However, this is inconsistent with the welldefined physical limit for a fast-orbiting accretor, as we will show in the following section.

5 ASYMPTOTIC EFFICIENCY OF A FAST-ORBITING ACCRETOR IN A SLOW WIND

During one orbital period, T, the accretion capture zone will sweep out a torus that fully encircles the primary star with a total covering factor of $r_{\rm B}/r$. If T is sufficiently short compared with the time $2r_{\rm B}/v_{\rm W}$ for the wind to cross the accretion capture zone, then all of the wind that passes within a distance $r_{\rm B}$ of the orbital path will be captured. This corresponds to $w \ll 1$ and yields a limiting accretion efficiency of

$$\eta_{\lim} = \lim_{w \to 0} \frac{r_{\rm B}}{r} = 2q. \tag{15}$$

Note that this is inconsistent with the Tejeda result, $\eta_T \approx q^2$, in the same limit, casting further doubt on the correctness of that result.

It is also inconsistent with the naive BHL result, $\eta_B \to \infty$, so we clearly require some correction to BHL. In the following section we outline a physically motivated correction that is consistent with η_{lim} .

6 STARVATION BY FINITE REFILL TIME

Tejeda & Toalá (2025) discuss the refill time, which is the time needed for the wind to replenish the material inside the accretion torus (see previous section) but they do not explicitly calculate its influence on the accretion efficiency. However, we will show that consideration of this effect is entirely sufficient in order to eliminate the divergence of η_B for small w.

During a single orbital period, the wind will propagate a distance $v_{\rm w}T$, which represents a fraction f of the diameter of the accretion torus:

$$f = \frac{v_{\rm w}T}{2r_{\rm B}} = \frac{\pi w}{r_{\rm B}/r} \approx \frac{w(1+w^2)}{q}$$
 (16)

7 GRAVITATIONAL INFLUENCE OF THE PRIMARY

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