Eigenvalue branches near $\omega_0=1.414\pi, \alpha_1=0.25$

