Eigenvalue branches near $\omega_0=1.414\pi$

