

Name: _____

NetID: _____ Lecture: A

Discussion: Monday & Wednesday 1:30 2:30

$$A = \{(x, y) \in \mathbb{Z}^2 \mid y = x^2 + 5x + 9\}$$

$$B = \{(a, b) \in \mathbb{Z}^2 \mid a \leq 2\}$$

$$C = \{(p, q) \in \mathbb{Z}^2 \mid q > 20\}$$

Prove that $A \subseteq B \cup C$.

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1. (4 points) $A = \{\text{apple, maple, elm, } \emptyset\}$ $B = \{\text{tree, oak, } \emptyset\}$

$$A \cap B =$$

$$\{(p, q) : p \in \mathbb{Z}, q \in \mathbb{Z}, \text{ and } pq = 6\} =$$

2. (4 points) Check the (single) box that best characterizes each item.

$$A \cap B \subseteq A$$

true for all sets A and B

true for some sets A and B

false for all sets A and B

$$\forall x \in \mathbb{N}, \text{ if } x^2 < -3, \text{ then } x > 1000.$$

true

false

undefined

3. (7 points) In \mathbb{Z}_{13} , find the value of $[7]^{18} + [7]^4$. You must show your work, keeping all numbers in your calculations small. **You may not use a calculator.** You must express your final answer as $[n]$, where $0 \leq n \leq 12$.