### Escherichia Coli Network

Example for GeneNet 1.2.13 (August 2015) or later

This note reproduces the "Escherichia coli" network example from J. Schäfer and K. Strimmer. 2005. A shrinkage approach to large-scale covariance estimation and implications for functional genomics. Statist. Appl. Genet. Mol. Biol. 4: 32 (http://dx.doi.org/10.2202/1544-6115.1175)

#### Load GeneNet package

```
library("GeneNet")

## Loading required package: corpcor

## Loading required package: longitudinal

## Loading required package: fdrtool

E. Coli data set (9 time points for 102 genes):

data(ecoli)
dim(ecoli)

## [1] 9 102
```

# Estimation of partial correlations

Estimate matrix of partial correlation using a shrinkage estimator:

```
pc = ggm.estimate.pcor(ecoli)

## Estimating optimal shrinkage intensity lambda (correlation matrix): 0.1804

dim(pc)
```

## [1] 102 102

Assign p-values, q-values and empirical posterior probabilities to all 5151 potential edges in the network:

```
ecoli.edges = network.test.edges(pc, direct=TRUE, fdr=TRUE)
## Estimate (local) false discovery rates (partial correlations):
## Step 1... determine cutoff point
## Step 2... estimate parameters of null distribution and eta0
## Step 3... compute p-values and estimate empirical PDF/CDF
## Step 4... compute q-values and local fdr
## Step 5... prepare for plotting
##
## Estimate (local) false discovery rates (log ratio of spvars):
## Step 1... determine cutoff point
## Step 2... estimate parameters of null distribution and eta0
## Step 3... compute p-values and estimate empirical PDF/CDF
## Step 4... compute q-values and local fdr
## Step 5... prepare for plotting
dim(ecoli.edges)
## [1] 5151
              10
```

The table lists all edges in the order strength of partial correlations:

ecoli.edges[1:5,]

```
##
          pcor node1 node2
                                                qval
                                                          prob
                                                                  log.spvar
                        53 2.220446e-16 3.612205e-13 1.0000000 -0.043537019
## 1 0.2318566
                  51
                  52
## 2 0.2240555
                        53 2.220446e-16 3.612205e-13 1.0000000 -0.040249854
## 3 0.2150782
                  51
                        52 2.220446e-16 3.612205e-13 1.0000000 -0.003287165
                  7
## 4 0.1732886
                        93 3.108624e-15 3.792816e-12 0.9999945 -0.025293430
## 5 -0.1341889
                  29
                        86 1.120812e-09 1.093997e-06 0.9999516 0.022305368
     pval.dir qval.dir
                            prob.dir
## 1 0.3803869 0.7557272 1.110223e-15
## 2 0.4173922 0.7724561 1.110223e-15
## 3 0.9471949 0.8851073 1.110223e-15
## 4 0.6103234 0.8323249 1.110223e-15
## 5 0.6531371 0.8415749 1.110223e-15
```

## Decide which edges to include in the network

To obtain a graph you need to select top ranking edges according to a suitable criterion. Here are some suggestions:

1. Use local fdr cutoff 0.2, i.e. include all edges with posterior probability of at least 0.8.

```
ecoli.net = extract.network(ecoli.edges)
```

```
##
## Significant edges: 125
##
       Corresponding to 2.43 % of possible edges
##
## Significant directions: 377
       Corresponding to 7.32 % of possible directions
## Significant directions in the network: 17
       Corresponding to 13.6 % of possible directions in the network
dim(ecoli.net)
## [1] 125 11
  2. Use local fdr cutoff 0.1, i.e. i.e. include all edges with posterior probability of at least 0.9.
ecoli.net = extract.network(ecoli.edges, cutoff.ggm=0.9, cutoff.dir=0.9)
##
## Significant edges: 65
       Corresponding to 1.26 \% of possible edges
##
##
## Significant directions: 269
       Corresponding to 5.22 % of possible directions
## Significant directions in the network: 6
##
       Corresponding to 9.23 % of possible directions in the network
dim(ecoli.net)
## [1] 65 11
  3. Include a fixed number of edges, say the 70 strongest edges
ecoli.net = extract.network(ecoli.edges, method.ggm="number", cutoff.ggm=70)
##
## Significant edges: 70
##
       Corresponding to 1.36 % of possible edges
##
## Significant directions: 377
       Corresponding to 7.32 % of possible directions
## Significant directions in the network: 9
       Corresponding to 12.86 % of possible directions in the network
dim(ecoli.net)
```

#### ## [1] 70 11

Plot network

For plotting we use the graph and Rgraphviz packages from Bioconductor.

```
library("Rgraphviz")
## Loading required package: graph
## Loading required package: BiocGenerics
## Attaching package: 'BiocGenerics'
## The following objects are masked from 'package:stats':
##
##
       IQR, mad, sd, var, xtabs
## The following objects are masked from 'package:base':
##
##
       anyDuplicated, aperm, append, as.data.frame, basename, cbind,
##
       colnames, dirname, do.call, duplicated, eval, evalq, Filter, Find,
       get, grep, grepl, intersect, is.unsorted, lapply, Map, mapply,
##
##
       match, mget, order, paste, pmax, pmax.int, pmin, pmin.int,
##
       Position, rank, rbind, Reduce, rownames, sapply, setdiff, table,
       tapply, union, unique, unsplit, which.max, which.min
##
## Loading required package: grid
Create graph object from the list of edges:
node.labels = colnames(ecoli)
gr = network.make.graph(ecoli.net, node.labels, drop.singles=TRUE)
table( edge.info(gr)$dir )
##
## forward
              none
##
         9
                61
sort( node.degree(gr), decreasing=TRUE)
                                                asnA
         cspG fixC
                      yheI
                            lacA lacY
                                         lacZ
                                                      {\tt eutG}
                                                                   yedE
##
                                                             yceP
                                                                         ygcE
                                                                               pspA
##
             8
                    7
                          7
                                6
                                      6
                                             6
                                                   5
                                                         5
                                                                5
                                                                      5
                                                                            5
      11
    atpD b1191 b1583
##
                      cspA
                             icdA
                                   mopB
                                         pspB
                                                tnaA
                                                      yaeM
                                                            ycgX
                                                                   yfaD
                                                                         dnaG
                                                                                dnaK
##
       3
             3
                    3
                          3
                                3
                                      3
                                             3
                                                   3
                                                         3
                                                                3
                                                                      3
                                                                            2
                                                                                   2
##
    hupB
          ibpB
                yfiA
                      aceB
                             atpG b1963
                                         cchB
                                                dnaJ
                                                      flgD
                                                            folK
                                                                   ftsJ
                                                                         gltA
##
       2
             2
                    2
                          1
                                                         1
                                                                      1
                                1
                                      1
                                             1
##
    nmpC
          nuoM sucD
                      yec0
                             ygbD
                                   yhdM
                                         yjb0
##
       1
             1
                    1
                          1
```

Set node and edge attributes for more beautiful graph plotting:

```
globalAttrs = list()
globalAttrs$edge = list(color = "black", lty = "solid", lwd = 1, arrowsize=1)
globalAttrs$node = list(fillcolor = "lightblue", shape = "ellipse", fixedsize = FALSE)

nodeAttrs = list()
nodeAttrs$fillcolor = c('sucA' = "yellow")

edi = edge.info(gr)
edgeAttrs = list()
edgeAttrs$dir = edi$dir # set edge directions
edgeAttrs$lty = ifelse(edi$weight < 0, "dotted", "solid") # negative correlation -> dotted
edgeAttrs$color = ifelse(edi$dir == "none", "black", "red")
edgeAttrs$label = round(edi$weight, 2) # use partial correlation as edge labels

plot(gr, attrs = globalAttrs, nodeAttrs = nodeAttrs, edgeAttrs = edgeAttrs, "fdp")
```

