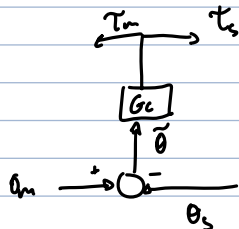
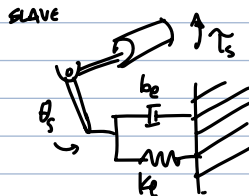
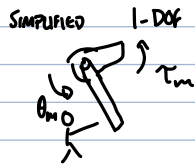
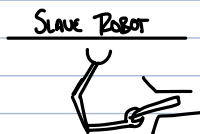
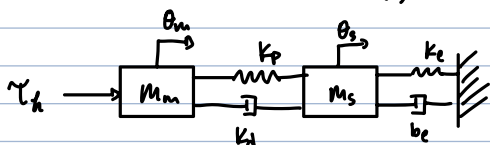


24 TELE OPERATION + HAPTICS



BILATERAL SERVO

CHOOSE $G_c = K_p + K_d s = \frac{\tau(s)}{\theta(s)}$ ← PASSED INTO BOTH MASTER + SLAVE



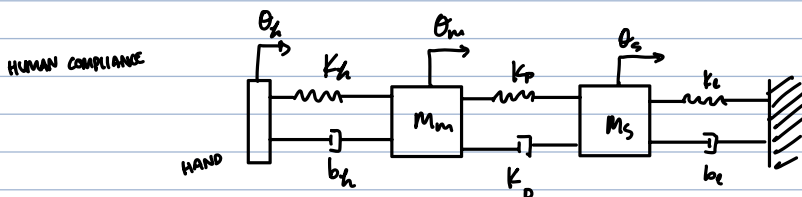
τ_h = HUMAN-INPUT TORQUE

How CAN WE ENSURE STABILITY?

NEGLECTING DAMPING

$$\frac{\theta_m(s)}{\tau_h(s)} = \frac{m_s s^2 + (k_e + k_p)}{m_m m_s s^4 + [(k_p + k_e) m_m + k_p m_s] s^2 + k_e + k_p}$$

LET'S SAY WE MODEL THE HUMAN AS A POSITION INPUT w/ SOME COMPLIANCE



CONTROL LAW:

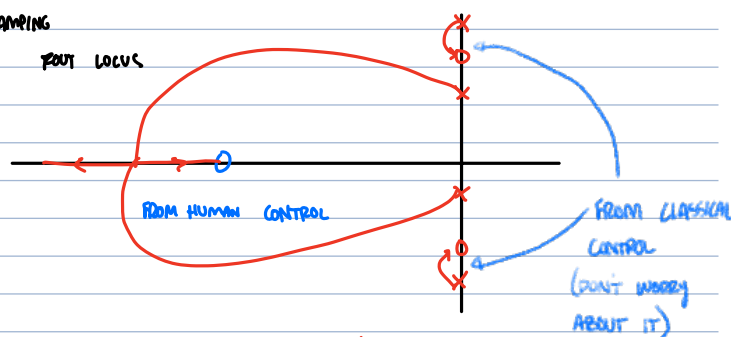
$$\tau_h = K_h (\theta_h - \theta_m) + b_h (\dot{\theta}_h - \dot{\theta}_m)$$

$$= (K_h + b_h s) (\theta_h - \theta_m)$$

HUMAN ACTS LIKE PD CONTROLLER

← NEGLECTED ALL DAMPING IN SYSTEM

ROOT LOCUS



O.L. POLES/ZEROS FROM PLANT

OUR CONTROLLER IS STABLE FOR ALL GAINS

TRANSPARENCY: WE'D LIKE THE OPERATOR TO ONLY FEEL DYNAMICS FROM SLAVE'S ENVIRONMENT

WHAT DOES OUR HUMAN FEEL IN THIS SCENARIO?

$$\tau_h \rightarrow \boxed{m_m} \begin{matrix} \leftarrow \tau_m \\ \leftarrow \end{matrix} \quad \text{DYNAMICS OF MASTER} \quad = k_p \tilde{\theta} + k_d \dot{\tilde{\theta}} = \tau_s \quad \tau_s \rightarrow \boxed{m_s} \begin{matrix} \leftarrow \tau_e \\ \leftarrow \end{matrix} \quad \text{DYNAMICS OF SLAVE}$$

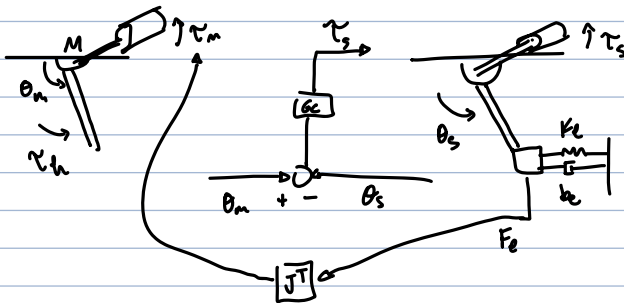
HUMAN FEELS DYNAMICS OF MASTER AND SLAVE IN ADDITION TO τ_e

IF SLAVE IS NOT VERY TRACKABLE (LARGE INERTIA / FRICTION), THEN τ_e NEEDS TO BE VERY LARGE BEFORE HUMAN FEELS IT

- CAN DAMAGE ENVIRONMENT
- JEOPARDIZE SUCCESS OF TASK (WEDGING/JAMMING)

\therefore BILATERAL SERVO HAS GOOD STABILITY BUT POOR TRANSPARENCY

LET'S PUT A FORCE SENSOR ON SLAVE END-EFFECTOR & FEEDBACK ENVIRONMENT FORCE TO MASTER

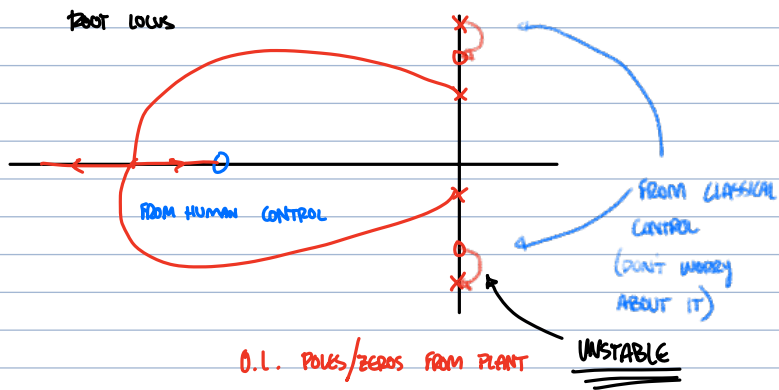


WE'VE IMPROVED TRANSPARENCY, BUT WE DON'T KNOW ABOUT STABILITY

"PLANT"
$$\frac{\theta_s(s)}{\tau_h(s)} = \frac{m_s s^2 + (k_e + k_p)}{m_m m_s s^4 + m_m (k_e + k_p) s^2 + k_f k_e k_p}$$

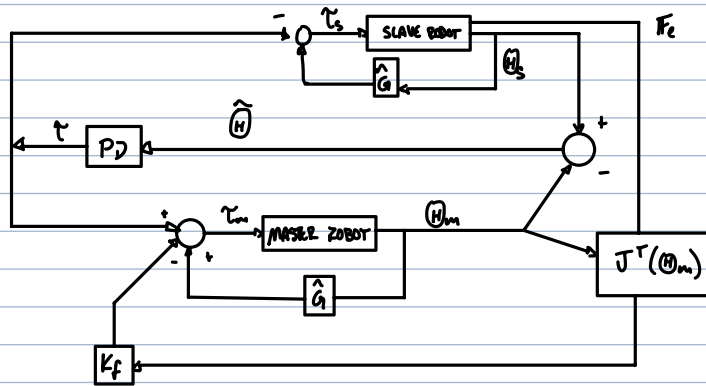
ASSUME HUMAN ACTS LIKE A CONTROLLER ON THIS PLANT

$$\tau_h = (k_h + b_h s) (\theta_h - \theta_m)$$

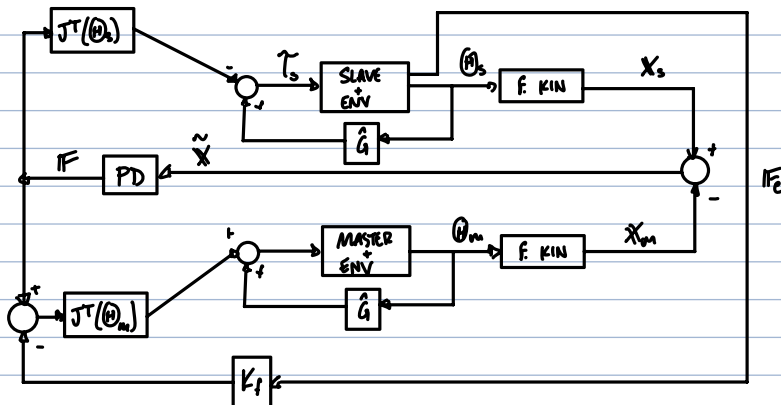


∴ Direct force feedback is more transparent but less stable

In practice, we can use a combo of bilateral servo & direct force feedback



As we increase K_f , we will get more transparency at the expense of stability



TAKEAWAYS:

- IN OP-SPACE, THE MASTER & SLAVE CAN TOGGLE @ SINGULARITIES
(ELBOW-UP VS ELBOW-DOWN)
- IN OP-SPACE, CAN USE PI CONTROL