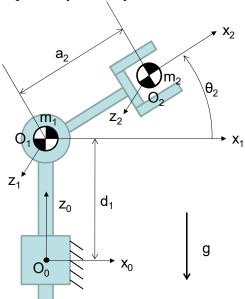
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## ME EN 5230/6230, CS 6330, ECE 6651 Intro to Robot Control Practice Midterm Exam Spring 2023 80 minutes

- Closed Book
- 1 sheets of notes allowed plus Newton/Euler reference sheet

## **Problem 1: Dynamics (Total 40 Points)**

The figure below shows a planar 2-DOF robot with a prismatic joint and a rotary joint. Assume that the rotational inertia  $I_2$  is negligible and the COGs of  $m_1$  and  $m_2$  are at  $O_1$  and  $O_2$  respectively. Gravity is in the  $-z_0$  direction.



The forward kinematics are given by:

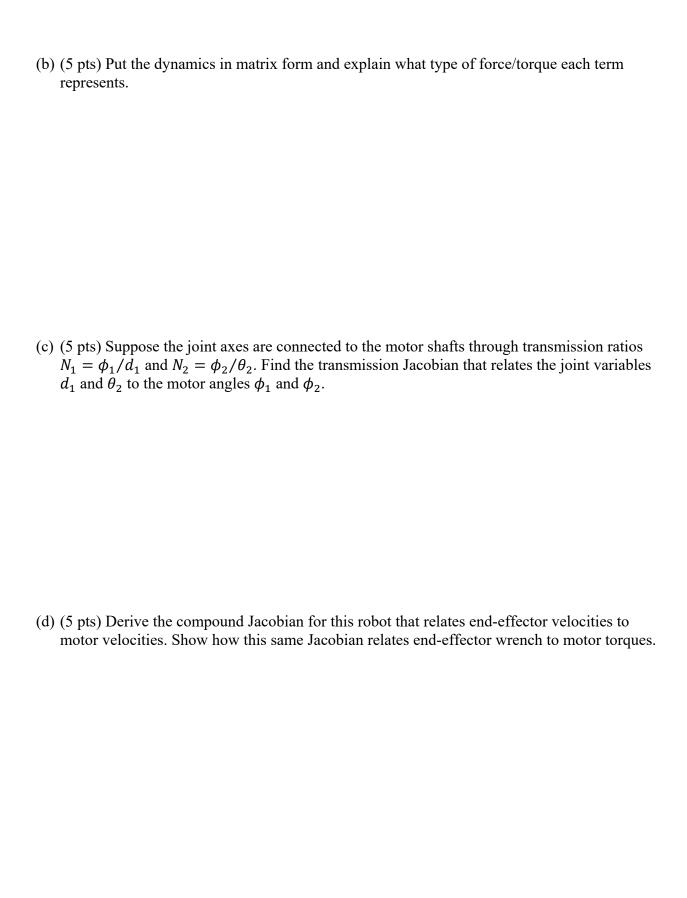
$$x = a_2 \cos(\theta_2)$$
  
$$y = d_1 + a_2 \sin(\theta_2)$$

The manipulator dynamics are given by:

$$f_1 = (m_1 + m_2)\ddot{d}_1 + a_2 m_2 \ddot{\theta}_2 \cos\theta_2 - a_2 m_2 \dot{\theta}_2^2 \sin\theta_2 + (m_1 + m_2)g$$

$$\tau_2 = a_2 m_2 \ddot{d}_1 \cos \theta_2 + a_2^2 m_2 \ddot{\theta}_2 + a_2 m_2 g \cos \theta_2$$

(a) (5 pts) Use the forward kinematics to find the manipulator Jacobian for this robot.



(e)	(e) (15 pts) Transform your manipulator dynamics to motor space.					ace.	

(f)	(5 pts) Suppose the motor shafts have rotational inertias $J_1$ and $J_2$ and viscous damping constants $b_1$ and $b_2$ . Show how these augment the dynamic equations in motor space.		

## **Problem 2: Decentralized Control (Total 40 Points)**

Suppose you decide to design a simple decentralized PD control system for the robot. To do this, you decide to neglect inertial coupling and use a simple feedback compensator to cancel out all the centripetal and gravity forces/torques. Use the following parameter values:

$$m_1=78$$
  
 $m_2=50$   
 $a_2=2$   
 $J_1=J_2=2$   
 $b_1=b_2=8$ 

(a) (10 pts) Use impedance matching to find the optimal gear ratios  $N_1$  and  $N_2$  to maximize the ability to accelerate each joint from rest. Use these values in the remainder of this problem.

(b) (10 pts) Sketch a block diagram of your control system including the PD control and feedback compensator. Also write your control law in terms of the dynamic parameters.

(c) (5 pts) Assuming that you have now cancelled out centripetal and gravity forces/torques (and neglecting inertial coupling), show that you get the same open-loop transfer function for both joints:

$$\frac{\phi_1(s)}{\tau_{m1}(s)} = \frac{1}{4s^2 + 8s}$$
 and  $\frac{\phi_2(s)}{\tau_{m2}(s)} = \frac{1}{4s^2 + 8s}$ 

(d) (15 pts) Since both joints happen to have the same transfer function, we can use the same PD gains for both. Sketch the root locus and use the angle and magnitude conditions to find the PD gains necessary to place the closed loop poles at  $s = -2 \pm 2j$ .

## **Problem 3: Centralized Control (Total 20 Points)**

11001cm of Schillanzon Sonition (100m zo 10mis)
Design an Inverse Dynamics Controller for the robot.
(a) (10 pts) Draw a complete block diagram of the control system.
(b) (5 pts) Write the control law in terms of the dynamic parameters.
(c) (5 pts) Why is this controller superior to the one in Problem 2? Would you use the same PD
gains as you designed in Problem 2? Explain.