# STATS 507 Data Analysis in Python

Week 6: Numpy practice & scikit-learn

#### Numpy practice

On Canvas, see Files/in-class practice/week6practice.ipynb



#### scikit-learn

Open-source Python machine learning library
Built atop numpy, scipy and matplotlib

Makes many common ML/stats models easily available API supports simple model fitting, prediction, cross-validation, etc.

#### Installation:

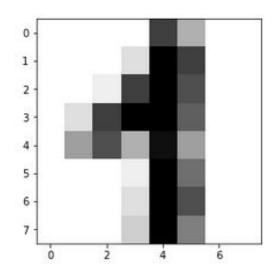
pip install scikit-learn (or conda install scikit-learn) ...or install from source (still not recommended)

```
from sklearn import datasets
digits = datasets.load_digits()
digits.target[42]
```

sklearn includes a number of built-in data sets, among which is a version of the famous MNIST digits data set.

```
plt.imshow(np.reshape(digits.data[42], (8,8)), cmap='binary')
```

<matplotlib.image.AxesImage at 0x10.015748>



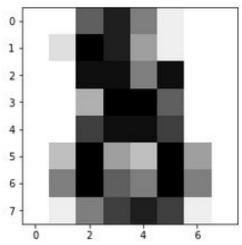
digits.data is an array, entries of which are 64-dimensional vectors, which correspond to images. To display them, we have to reshape them to 8-by-8. The cmap argument specifies a color map. See <a href="https://matplotlib.org/users/colormaps.html">https://matplotlib.org/users/colormaps.html</a>

```
from sklearn import svm
clf = svm.SVC(gamma=0.001, C=100.)
clf.fit(digits.data[:-1], digits.target[:-1])
```

SVC is a support vector machine (SVM) classifier, one of many classifiers that sklearn provides. It requires two hyperparameters (more on these soon, but for now just treat them as magic).

```
SVC(C=100.0, cache_size=200, class_weight=None, coef0=0.0,
  decision_function_shape='ovr', degree=3, gamma=0.001, kernel='rbf',
  max_iter=-1, probability=False, random_state=None, shrinking=True,
  tol=0.001, verbose=False)
```

```
1 clf.predict(digits.data[-1:])
array([8])
```

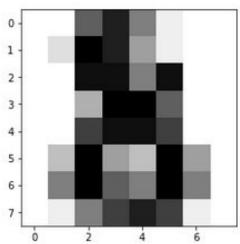


```
from sklearn import svm
clf = svm.SVC(gamma=0.001, C=100.)
clf.fit(digits.data[:-1], digits.target[:-1])
```

Every classifier object supports a fit method, which takes observations and labels and adjusts the model parameters to best fit that data.

```
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  decision_function_shape='ovr', degree=3, gamma=0.001, kernel='rbf',
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  tol=0.001, verbose=False)
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array([8])
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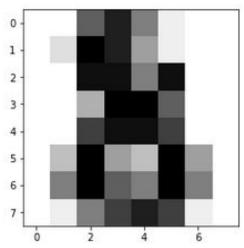


```
from sklearn import svm
clf = svm.SVC(gamra=0.001, C=100.)
clf.fit(digits.data[:-1], ilgits.target[:-1])
```

We are training on all but one of the digits in the collection, keeping one as "held out" data on which we can test our classifier.

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  tol=0.001, verbose=False)
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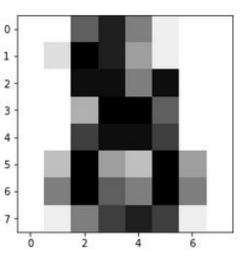


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max_iter=-1, probability=False, random_state=None, shrinking=True,
tol=0.001, verbose=False)
```

```
1 clf.predict(digits.data[-1:])
array([8])
```

Every classifier object also supports a predict method, which takes an observation and tries to guess the "best" label for it, based on the model parameters.



**Review:** linear regression

$$y = X\beta + \epsilon$$

Predictors 
$$X \in \mathbb{R}^{n imes d}$$

Coefficients

$$\beta \in \mathbb{R}^a$$

Noise

$$\epsilon \in \mathbb{R}^n$$

Response

$$y \in \mathbb{R}^n$$

Ordinary least squares (OLS)

$$\min_{\beta} \frac{1}{n} \sum_{i=1}^{n} (y_i - \beta^T x_i)^2$$

Minimizes the sum of the squared residuals between the response and the model prediction. OLS is computationally convenient. The solution can be expressed as an expression of X.

**Review:** linear regression

$$y = X\beta + \epsilon$$

Predictors 
$$X \in \mathbb{R}^{n imes d}$$

Coefficients

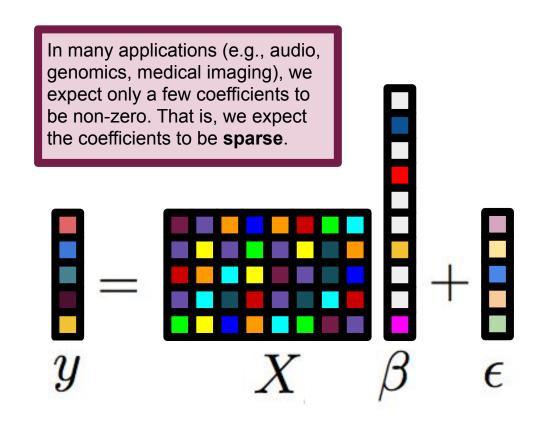
$$\beta \in \mathbb{R}^d$$

Noise

$$\epsilon \in \mathbb{R}^n$$

Response

$$y \in \mathbb{R}^r$$



**Review:** linear regression

$$y = X\beta + \epsilon$$

Predictors 
$$X \in \mathbb{R}^{n imes d}$$

Coefficients 
$$eta \in \mathbb{R}^d$$

Noise

$$\epsilon \in \mathbb{R}^n$$

Response

$$y \in \mathbb{R}^n$$

**Ordinary least squares (OLS)** 

$$\min_{\beta} \frac{1}{n} \sum_{i=1}^{n} (y_i - \beta^T x_i)^2$$

**LASSO** 

$$\min_{\beta} \frac{1}{n} \sum_{i=1}^{n} (y_i - \beta^T x_i)^2 + \alpha \sum_{i=1}^{n} |\beta_i|$$

This penalty term discourages non-zero coefficients. The larger  $\alpha$  is, the more we are penalized for having non-zero coefficients.

**Review:** linear regression

$$y = X\beta + \epsilon$$

Predictors 
$$X \in \mathbb{R}^{n imes d}$$

Coefficients

$$\beta \in \mathbb{R}^d$$

Noise

$$\epsilon \in \mathbb{R}^n$$

Response

$$y \in \mathbb{R}^n$$

LASSO (equivalent formulation)

$$\min_{eta} rac{1}{n} \|y - eta^T X\|^2 + lpha \|eta\|_1$$
L2 objective L1 penalty

The key tradeoff here is that whereas OLS had a nice closed-form solution, we have to find a solution to the LASSO using optimization techniques, but that's okay, because sklearn will solve the optimization for us.

```
(n \text{ samp, dim, } k) = (200, 500, 10)
    X = np.random.randn(n samp, dim)
    beta = np.zeros(dim)
    inds = np.random.choice(np.arange(dim), size=k, replace=False)
    beta[inds] = 5*np.random.randn(k)
    y = np.dot(X, beta) + 0.1*np.random.randn(n samp)
                                                             Generate data; split into train/test.
    # Split data into train set and test set
    X train, y train = X[:(n_samp//2)], y[:(n_samp//2)]
    X test, y test = X[n samp // 2:], y[n samp // 2:]
    #import and train the model.
    from sklearn.linear model import Lasso
                                              Fit the model based on the train set.
    lasso = Lasso(alpha=1)
    lasso.fit(X train, y train)
16
    y pred lasso = lasso.predict(X test)
   from sklearn.metrics import r2 score
                                            Assess how well the model fits the test data.
19 r2 score(y test, y pred lasso)
```

```
(n \text{ samp, dim, } k) = (200, 500, 10)
                                                      200 points in 500 dimensions. Sparsity k=10.
    X = np.random.randn(n samp, dim)
   beta = np.zeros(dim)
    inds = np.random.choice(np.arange(dim), size=k, replace=False)
   beta[inds] = 5*np.random.randn(k)
    y = np.dot(X, beta) + 0.1*np.random.randn(n samp)
    # Split data into train set and test set
    X train, y train = X[:(n_samp//2)], y[:(n_samp//2)]
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   beta = np.zeros(dim)
   inds = np.random.choice(np.arange(dim), size=k, replace=False)
   beta[inds] = 5*np.random.randn(k)
                                                             Choose 10 coefficients at
                                                             random to be nonzero.
   # Split data into train set and test set
   X train, y train = X[:(n samp//2)], y[:(n samp//2)]
   X test, y test = X[n samp // 2:], y[n samp // 2:]
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    inds = np.random.choice(np.arange(dim), size=k, replace=False)
   beta[inds] = 5*np.random.randn(k)
    y = np.dot(X, beta) + 0.1*np.random.randn(n samp)
                                                                     Now generate the responses:
                                                                     inner product of independent
    # Split data into train set and test set
                                                                     variable with coefficients, plus
    X train, y train = X[:(n_samp//2)], y[:(n_samp//2)]
                                                                     normal noise.
    X test, y test = X[n samp // 2:], y[n samp // 2:]
    #import and train the model.
    from sklearn.linear model import Lasso
                                               Fit the model based on the train set.
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    beta[inds] = 5*np.random.randn(k)
    y = np.dot(X, beta) + 0.1*np.random.randn(n samp)
                                                                      Split into train and test sets.
                                                                      Typically the train set is chosen
    # Split data into train set and test set
                                                                      to be much larger than the test
    X train, y train = X[:(n samp//2)], y[:(n samp//2)]
                                                                      set, but this is just demo code.
    X test, y test = X[n samp // 2:], y[n samp // 2:]
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                                               Fit the model based on the train set.
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0.9635771805872204

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    beta[inds] = 5*np.random.randn(k)
    y = np.dot(X, beta) + 0.1*np.random.randn(n samp)
                                                              Generate data; split into train/test.
    # Split data into train set and test set
   X train, y train = X[:(n_samp//2)], y[:(n_samp//2)]
   X_test, y_test = X[n_samp // 2:], y[n_samp // 2:]
                                                             The alpha parameter controls how
    #import and train the model.
                                                             much regularization we use. Larger
    from sklearn.linear model import Lasso
                                                             values encourage sparser solutions.
    lasso = Lasso(alpha=1)
14
                                                            More on this in a few slides.
    lasso.fit(X train, y train)
15
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                                                              Generate data; split into train/test.
    # Split data into train set and test set
   X train, y train = X[:(n_samp//2)], y[:(n_samp//2)]
   X test, y test = X[n_samp // 2:], y[n_samp // 2:]
                                                            lasso is a Lasso object, which
    #import and train the model.
                                                            supports both fit and predict
13
    from sklearn.linear model import Lasso
                                                            methods (as do all "estimator"
    lasso = Lasso(alpha=1)
14
                                                            objects in sklearn).
    lasso.fit(X train, y train)
15
16
   y pred lasso = lasso.predict(X test)
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                                            Assess how well the model fits the test data.
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    X test, y test = X[n_samp // 2:], y[n_samp // 2:]
    #import and train the model.
    from sklearn.linear model import Lasso
                                                Fit the model based on the train set.
    lasso = Lasso(alpha=1)
    lasso.fit(X train, y train)
                                                       Now that we've called fit, the coefficients of
    y pred lasso = lasso.predict(X test)
                                                       lasso have been updated to fit the training
18
    from sklearn.metrics import r2 score
                                                       data. Now it's time to tell if the model we
    r2 score(y test, y pred lasso)
                                                       learned actually fits the held out data.
```

0.9635771805872204

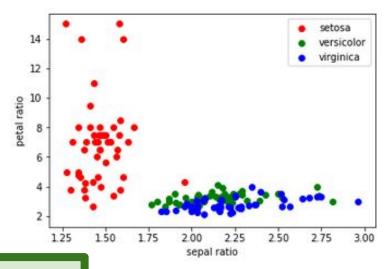
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                                                              Generate data; split into train/test.
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    #import and train the model.
    from sklearn.linear model import Lasso
                                               Fit the model based on the train set.
    lasso = Lasso(alpha=1)
    lasso.fit(X train, y train)
    y pred lasso = lasso.predict(X test)
                                                        lasso supports the predict method, which
    from sklearn.metrics import r2 score
18
                                                       takes in data points and outputs responses
    r2 score(y test, y pred lasso)
                                                        based on the current estimate of beta.
```

0.9635771805872204

```
(n \text{ samp, dim, } k) = (200, 500, 10)
    X = np.random.randn(n samp, dim)
    beta = np.zeros(dim)
    inds = np.random.choice(np.arange(dim), size=k, replace=False)
    beta[inds] = 5*np.random.randn(k)
    y = np.dot(X, beta) + 0.1*np.random.randn(n samp)
                                                                Generate data; split into train/test.
    # Split data into train set and test set
    X train, y train = X[:(n_samp//2)], y[:(n_samp//2)]
    X test, y test = X[n_samp // 2:], y[n_samp // 2:]
    #import and train the model.
    from sklearn.linear model import Lasso
                                                Fit the model based on the train set.
    lasso = Lasso(alpha=1)
    lasso.fit(X train, y train)
                                                     r2score is just one of the many ways to assess
    y pred lasso = lasso.predict(X test)
                                                      whether or not we're doing well. 1 is perfect
18
    from sklearn.metrics import r2 score
    r2 score(y test, y pred lasso)
                                                      performance, 0 is "chance".
                                                     https://en.wikipedia.org/wiki/Coefficient of determination
0.9635771805872204
```

```
A different but equally important measure
                                                 of performance is how well we recovered
    y pred lasso = lasso.predict(X test)
                                                the non-zero entries of beta.
    np.where( lasso.coef !=0 )
                                                           Note that we committed both type I and
                                                           type II errors by missing some entries of
                    66, 83, 86, 117, 197, 388]),)
(array([ 51,
                                                           beta and by incorrectly identifying
                                                           certain entries as non-zero.
    np.where( beta !=0 )
                                         197, 352
(array([ 51, 66, 83, 86, 117, 125
    from sklearn.metrics import fl score
    fl score(lasso.coef !=0, beta!=0, average='binary')
0.7777777777777777
```

F1 score is a good way to assess performance on these kinds of problems. It is a harmonic mean between the recall and precision. <a href="https://scikit-learn.org/stable/modules/generated/sklearn.metrics.f1">https://scikit-learn.org/stable/modules/generated/sklearn.metrics.f1</a> score.html



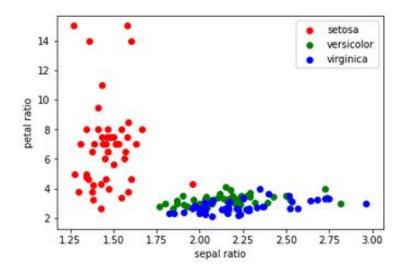
Here's the famous iris data set again. Clearly there's a cluster structure in the data. How can we discover it without using the label information?

**Basic idea:** model data as mixture of Gaussians each Gaussian generates one cluster

For each cluster, estimate mean and covariance Computationally hard...

...but can approximate via EM

https://en.wikipedia.org/wiki/Expectation-maximization\_algorithm

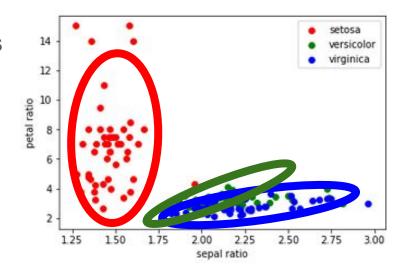


**Basic idea:** model data as mixture of Gaussians each Gaussian generates one cluster

For each cluster, estimate mean and covariance Computationally hard...

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Letting these ellipses represent the level sets of three Gaussians, we hope to see something like this picture.

**Basic idea:** model data as mixture of Gaussians each Gaussian generates one cluster

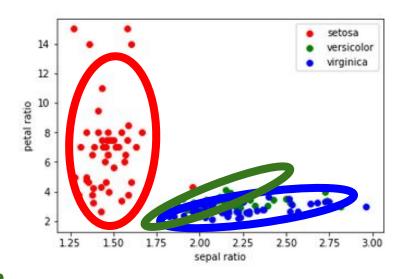
For each cluster, estimate mean and covariance Computationally hard...

...but can approximate via EM

https://en.wikipedia.org/wiki/Expectation-maximization\_algorithm

Of course, GMM is just one of many clustering algorithms we could choose from. For other options (though hardly an exhaustive list) and a good overview, see here:

https://scikit-learn.org/stable/modules/clustering.html



Letting these ellipses represent the level sets of three Gaussians, we hope to see something like this picture.

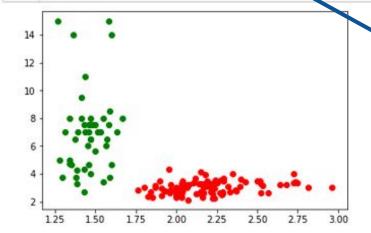
```
from sklearn import mixture
  R = np.stack([sepal ratio,petal ratio], axis=1)
                                                                Fit the model to the data.
  gmm = mixture.GaussianMixture(n components=2, n init=10,
                                  covariance type='full')
  gmm.fit(R)
  labs = gmm.predict(R)
                          Retrieve the (estimated) labels.
      plt.scatter(sepal
                                                            ==i].
                   c=colors[i])
12
10
```

1.50

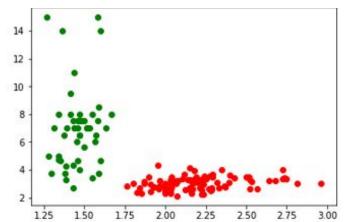
Gathering the sepal and petal ratios into a single array.

The GaussianMixture object has a number of attributes that specify how to go about finding a good fit.

More about this in a moment.



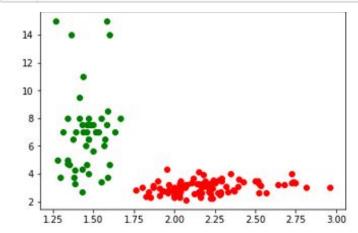
Every sklearn model supports the fit method. In this case, fitting consists of estimating the means and covariances of n=2 components.



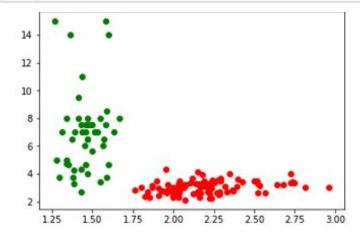
Fit a model with 2 components.

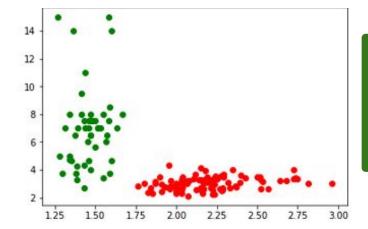
**Note:** we can already see a hard problem here. In this case, we happen to know that there are really three classes here (there are three species in the data), but typically, we don't know the classes ahead of time, so we don't know how to choose  $n\_components$ . This is called **model selection**. More on this in a few slides.

The EM algorithm is sensitive to its starting conditions, so we tell sklearn to run the EM algorithm multiple times (10, in this case), with different (random) starting conditions, and it keeps the one with the highest likelihood.

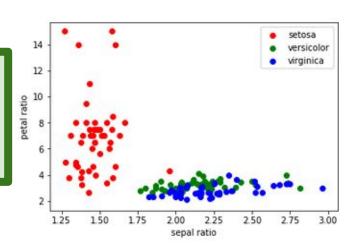


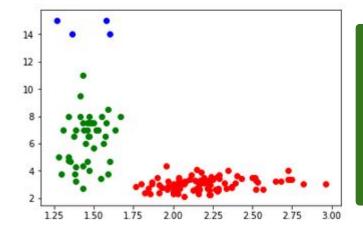
This tells sklearn to estimate a covariance matrix separately for each cluster. Other options include estimating one covariance shared across all clusters ('tied') and estimating spherical covariances for each cluster ('spherical').



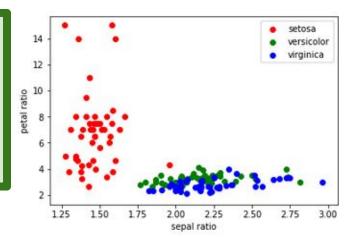


Of course, because we chose the wrong number of components, we fail to recover the true cluster structure of the data.





But even if we choose the correct number of components, the "ratio" representation of the data collapses the versicolor and virginica species, and we get a weird solution.



```
gmm = mixture.GaussianMixture(n components=3, n init=10,
                                       covariance type='full')
    gmm.fit(X)
                                             Note use of X, the full data, instead of the "ratios" R.
    labs = gmm.predict(X)
    for i in np.unique(labs):
         plt.scatter(sepal ratio[labs==i], petal ratio[labs==i],
                       c=colors[i])
                                                                                                      versicolor
12
                                        Clustering with the correct
10
                                        number of components in
                                                                      petal ratio
                                        the original 4-dimensional
                                         space recovers the truth.
           1.75
```

#### Model selection in sklearn

How should we choose the number of clusters in practice?

Again, typically we don't know, e.g., that there are three species in the data

One popular solution is to use an information criterion

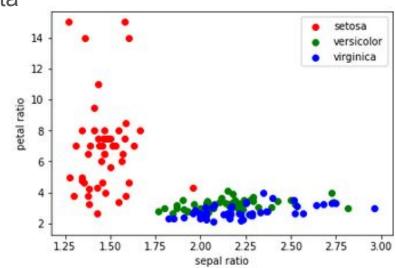
- measures how well a model reflects data
- penalizes model complexity

#### Examples:

https://en.wikipedia.org/wiki/Bayesian\_information\_criterion https://en.wikipedia.org/wiki/Akaike\_information\_criterion https://en.wikipedia.org/wiki/Mallows%27s\_Cp

See also

https://en.wikipedia.org/wiki/Minimum\_description\_length



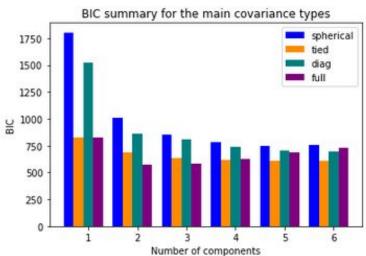
```
iris = datasets.load iris()
   X = iris.data
   y = iris.target
   n components range = range(1, 7)
   covar types = ['spherical', 'tied', 'diag', 'full']
   bics = np.zeros(shape=(len(covar_types),len(n_components_range)))
   for i in range(len(covar types)):
       cvtype = covar types[i]
        for j in range(len(n components range)):
            n comps = n components range[j]
            # Fit a Gaussian mixture with EM
12
            gmm = mixture.GaussianMixture(n components=n comps,
13
                                          covariance type=cvtype)
14
            qmm.fit(X)
15
            bics[i,j] = gmm.bic(X)
```

For different numbers of components and different covariance estimation methods, we're going to fit a GMM with that many components and using that covariance estimation method.

Measure BIC of each such choice; store it in the array bics.

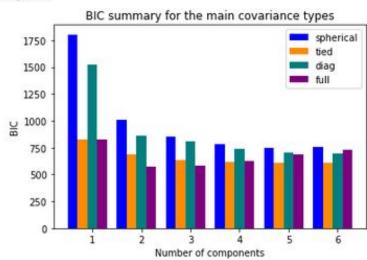
This is a simplified version of the demo here: <a href="https://scikit-learn.org/stable/auto-examples/mixture/plot-gmm-selection.html">https://scikit-learn.org/stable/auto-examples/mixture/plot-gmm-selection.html</a>

Now, let's have a look at the BIC scores. Within each covariance estimation method, the number of components with the lowest BIC is the one we should choose.



Now, let's have a look at the BIC scores. Within each covariance estimation method, the number of components with the lowest BIC is the one we should choose.

Spherical and diagonal covariance both seem to think that more components is always better (at least up to 6, anyway). This is unsurprising given the data: it's simple to check that the dimensions of the iris data are correlated.



Now, let's have a look at the BIC scores. Within each covariance estimation method, the number of components with the lowest BIC is the one we should choose.

```
barwidth=0.2
inds = np.array(list(n_components_range))
colors = ['blue', 'darkorange', 'teal', 'purple']

for i in range(
    plt.bar(ind)
    widt

Just have a look at the plot.

plt.xticks(inds)

plt.xticks(inds)

plt.xtlabel('BIC summary for the main covariance types')

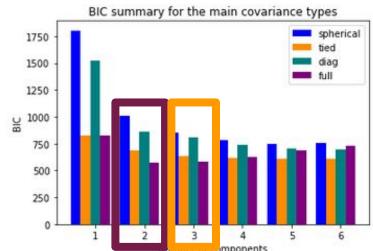
plt.xlabel('Number of components')

plt.ylabel('BIC')
    _ = plt.legend()

Editacousiance background DIC at 2
```

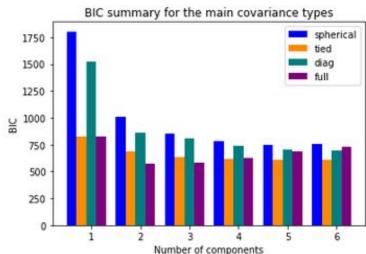
Full covariance has lowest BIC at 2. Tied covariance selects (the correct) number of components to be 3.

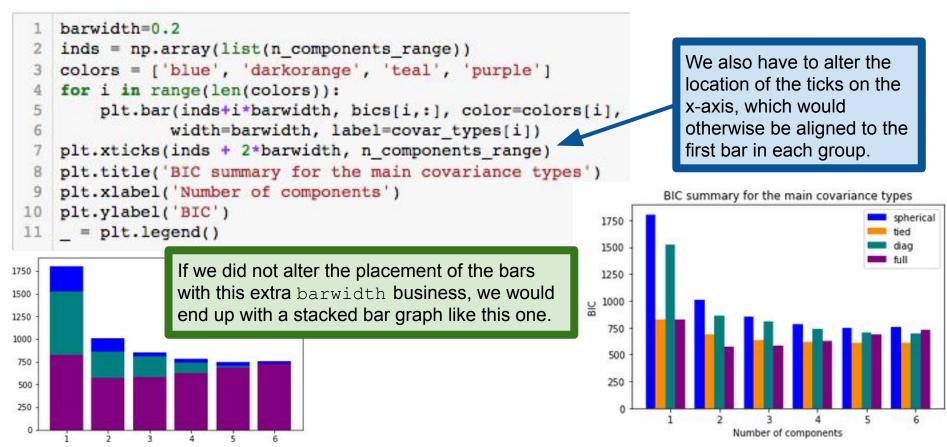
The lesson here is not that one of these methods will always be best, but that even a principled technique like BIC may sometimes give us the wrong answer.



```
barwidth=0.2
     inds = np.array(list(n components range))
     colors = ['blue', 'darkorange', 'teal',
                                                 purple']
     for i in range(len(colors)):
         plt.bar(inds+i*barwidth, bics[i,:], color=colors[i],
                 width=barwidth, label=covar types[i])
     plt.xticks(inds + 2*barwidth, n components range)
     plt.title('BIC summary for the main covariance types')
     plt.xlabel('Number of components')
     plt.ylabel('BIC')
     = plt.legend()
                  If we did not alter the placement of the bars
1750
                  with this extra barwidth business, we would
1500
                  end up with a stacked bar graph like this one.
1250
1000
750
250
```

We need to do a bit of annoying work because matplotlib doesn't have good support for "grouped" bar plots like this.





Similar to model selection, sklearn includes tools for cross-validation (CV)

CV is how we choose parameters like alpha in the LASSO

#### Basic idea:

Try many different choices of parameter

Keep the one that gives the best performance on the train data

There are many ways to do this, but we'll focus on K-fold CV See <a href="https://en.wikipedia.org/wiki/Cross-validation">https://en.wikipedia.org/wiki/Cross-validation</a> (statistics) for more

# Cross-validation in sklearn: K-fold CV

We split the training data into K "folds" (K=5 in the example at right). For each fold, we train on the other K-1 folds and evaluate the trained model on the "held-out" fold.

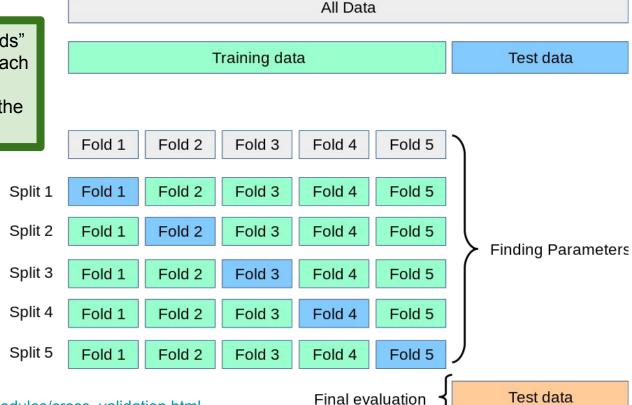


Image credit: <a href="https://scikit-learn.org/stable/modules/cross\_validation.html">https://scikit-learn.org/stable/modules/cross\_validation.html</a>

# Cross-validation in sklearn: K-fold CV

We split the training data into K "folds" (K=5 in the example at right). For each fold, we train on the other K-1 folds and evaluate the trained model on the "held-out" fold.

On each fold, we evaluate all of the models that are under consideration. We then average each model over the folds and keep the model with the best average score.

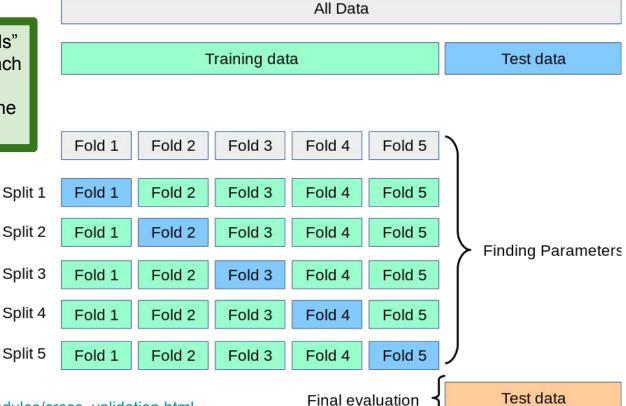


Image credit: <a href="https://scikit-learn.org/stable/modules/cross\_validation.html">https://scikit-learn.org/stable/modules/cross\_validation.html</a>

```
from sklearn.model selection import cross val score
    (n \text{ samp, dim, k}) = (200, 500, 10)
   beta = np.zeros(dim)
    inds = np.random.choice(np.arange(dim), size=k, replace=False)
    beta[inds] = 5*np.random.randn(k)
    X = np.random.randn(n samp, dim)
                                                          Generating sparse
    y = np.dot(X, beta) + 0.1*np.random.randn(n samp)
                                                          data just like before.
    lasso = Lasso(alpha=5)
    scores = cross val score(lasso, X, y, cv=10)
    scores
array([0.48286732, 0.31126123, 0.21513214, 0.40061088, 0.40758368,
       0.38318857, 0.25855801, 0.30367255, 0.52062931, 0.41335016)
```

```
from sklearn.model selection import cross val score
    (n \text{ samp, dim, } k) = (200, 500, 10)
    beta = np.zeros(dim)
    inds = np.random.choice(np.arange(dim), size=k, replace=False)
    beta[inds] = 5*np.random.randn(k)
    X = np.random.randn(n samp, dim)
    y = np.dot(X, beta) + 0.1*np.random.randn(n samp)
                                                          We pass a model, observations,
    lasso = Lasso(alpha=5)
                                                          labels, and a number of folds to
    scores = cross val score(lasso, X, y, cv=10)
                                                          the cross val score function.
    scores
array([0.48286732, 0.31126123, 0.21513214, 0.40061088, 0.40758368,
       0.38318857, 0.25855801, 0.30367255, 0.52062931, 0.41335016])
```

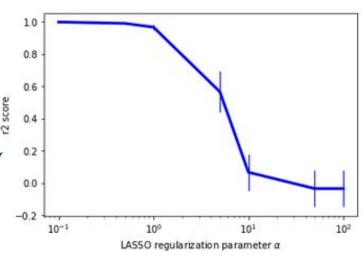
cross\_val\_score performs cv splits. On each split, we hold out one fold, train on the rest, and evaluate on the held-out fold. cross\_val\_score returns an array of the scores obtained in this way.

```
from sklearn.model selection import cross val score
   alphavals = np.array([0.1, 0.5, 1.0, 5, 10.0, 50, 100])
   mean scores = np.zeros(alphavals.shape)
   sd scores = np.zeros(alphavals.shape)
   for i in range(len(alphavals)):
       lasso = Lasso(alpha=alphavals[i])
       scores = cross val score(lasso, X, y, cv=10)
       mean scores[i] = np.mean(scores)
       sd scores[i] = np.std(scores)
   plt.errorbar(alphavals, mean scores, yerr=2*sd scores,
                color='blue', linewidth=3, elinewidth=1)
13
14
   plt.xscale('log'); plt.ylabel('r2 score')
   =plt.xlabel(r'LASSO regularization parameter $\alpha$'
```

The score method of the Lasso model is the r2score, which we saw a few slides ago.

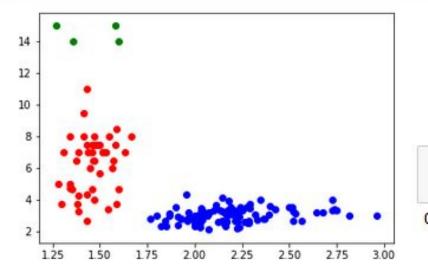
Now, we're going to do exactly the same thing, but for several different choices of alpha.

By default, cross\_val\_score evaluates based on the score method supplied by the model.
This can be changed by specifying the scoring parameter.



# Assessing Models: sklearn.metrics

sklearn.metrics contains a bunch of useful methods for evaluating models.



**Example:** the adjusted Rand index measures how well two clusterings agree. It's a good measure of how well a clustering that we come up with agrees with the truth. ARI=1 is perfect, ARI=0 is random chance.

```
from sklearn.metrics import adjusted_rand_score
adjusted_rand_score(labs, iris.target)
```

0.5075234747132037

https://scikit-learn.org/stable/modules/model\_evaluation.html

# Model persistence: pickling model objects

```
beta = np.zeros(dim)
    inds = np.random.choice(np.arange(dim), size=k, replace=False)
    beta[inds] = 5*np.random.randn(k)
    (n \text{ samp, dim, k}) = (200, 500, 10)
                                                                 Using the pickle module, we can train
    X = np.random.randn(n samp, dim)
                                                                 a model, and save it in a file and load
    y = np.dot(X, beta) + 0.1*np.random.randn(n train)
                                                                 it again later (e.g., for use in a different
                                                                 program, on a different data set, etc.).
    lasso = Lasso(alpha=1)
    lasso.fit(X, y)
                                                                 We'll see a similar pattern again soon
                                                                 when we discuss PyTorch.
    import pickle
    s = pickle.dumps(lasso)
    xtest = np.random.randn(1,dim)
    ytest = np.dot(xtest,beta) + 0.1*np.random.randn(1)
    lasso2 = pickle.loads(s)
    lasso.predict(xtest), lasso2.predict(xtest)
16
                                                       Here we're picking lasso, and
                                                       reloading it into lasso2. Note that the
(array([-0.60337359]), array([-0.60337359]))
                                                       two models are indeed the same.
```