

CO450 Computer Architectures Week 7 Exercise Handout

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Recap on Signed Magnitude Notation

1. Represent the following decimal number in binary using Signed Magnitude Notation:

+107₁₀

128	64	32	16	8	4	2	1
2^7	2^6	2^5	2^4	2^3	2^2	2^1	2^0
.	1	1	.	1	.	1	1

The correct answer is:

.	1	1	.	1	.	1	1
---	---	---	---	---	---	---	---

Recap on Binary Excess Notation to Decimal

1. What is the decimal number that is represented by 10111011₂ in Excess Notation?

	128	64	32	16	8	4	2	1
	2^7	2^6	2^5	2^4	2^3	2^2	2^1	2^0
	1	.	1	1	1	.	1	1
Unsigned binary to decimal conversion using positional notation								
Unsigned decimal value minus Excess ($2^{(n-1)}$) Note: n = number of bits								

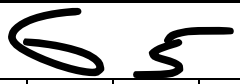
The correct answer is:

59

Recap on Decimal to Binary Excess Notation

1. What is the binary Excess Notation representation of the following decimal number:

-63_{10}

Decimal plus Excess ($2^{(n-1)}$) Note: n = number of bits								
	128	64	32	16	8	4	2	1
	2^7	2^6	2^5	2^4	2^3	2^2	2^1	2^0
Convert Decimal with Excess to binary using positional notation		1						1

The correct answer is:

.	1	/
---	---	---	---	---	---	---	---

Recap on Two's Complement

1. Convert 59_{10} to binary then use Two's Complement to convert the unsigned binary representation of 59_{10} in to the Two's Complement binary representation for -59_{10} , what is the correct answer:

	128	64	32	16	8	4	2	1
	2^7	2^6	2^5	2^4	2^3	2^2	2^1	2^0
Positional notation used to convert decimal to binary	.	.	1	1	1	.	1	1
Flipped bits	1	1	.	.	.	1	.	.
One to add to the flipped bits above								1
Result of addition of flipped bits and one								
Carry Bits								

The correct answer is:

1	/	.	.	.	1	.	1
---	---	---	---	---	---	---	---

Recap on Two's Complement Binary Additions

1. Add the following numbers together using two's complement binary representation and then answer the questions below:

$$-43_{10} + -27_{10} =$$

			128	64	32	16	8	4	2	1
			2^7	2^6	2^5	2^4	2^3	2^2	2^1	2^0
					.		.		.	
						.	.		.	
				.				.		.

Did the calculation produce an overflow? YES NO

Did the calculation produce a carryout? YES NO

Would the calculation produce a correct result in an 8 bit system? YES NO

How many bits were carried to the left during the calculation? 4

Recap on Decimal to Excess 50 Notation

1. Represent -16_{10} in excess 50 notation:

-16	+	50 ₁₀	=	34
-----	---	------------------	---	----

The correct answer is:

34

Recap on Conversion of Decimal Numbers to SEEZMMMM Format

1. Convert $+0.000548701_{10}$ into the SEEZMMMM format:

We have done this first one for you.

S = signed magnitude notation	=	.
EE = Exponent Excess 50 notation	=	47
ZMMMM = Mantissa	=	548701.
Normalise Mantissa	=	

The correct answer is:

0 47 54870

Recap on Conversion of SEEZMMMM Format to Decimal Number

1. Convert 04476823 in the SEEZMMMM Format to a decimal number:

We have done this first one for you.

S = signed magnitude notation	=		=	+
EE = Exponent Excess 50 notation	=		=	-6
ZMMMM = Mantissa	=		=	

The correct answer is:

0.0000076823

Recap on Conversion of Decimal Exponent to Excess 127 Binary

1. Represent an Exponent of -23_{10} in the Excess 127 format:

Excess	127	=								
Two's Complement Exponent	-23	=								
Result of addition of excess and exponent										
Carry's										

The correct answer is:

104

Recap on Conversion of IEEE 754 Single Precision Binary Float to Decimal

1. Convert the following IEEE 754 single precision binary float to decimal:

Q10000111101100110000000000000000₂

Sign		=	+						
Excess		=	1	1	1
Convert excess binary unsigned to decimal and subtract excess 127 to get exponent		=	8						

Mantissa	1.10110011
Shift decimal point with exponent	
Convert shifted binary mantissa to decimal	
Add sign to converted decimal	

11.111111

The correct answer is:

435

Recap on the Little Man Computer

1. Look at the Little Man Computer code below. What number will be in the Accumulator after the CPU executes the instruction held in memory location 4?

```

LDA  first
STA  second
ADD  first
SUB  second
OUT
stop  HLT
first DAT 010
second DAT

```

10

The Register Transfer Language (RTL)

1. What does the following RTL notation indicate?

We have done this first one for you.

$[2_{(0:3)}] \leftarrow 1$

The RTL notation indicates that bits 0 to 3 of memory address 2 are to be set to one.

2. What does the following RTL notation indicate?

$[4] \leftarrow [8]$

mem addrs 4 set same as mem addrs 8

3. What does the following RTL notation indicate?

$[8] \leftarrow [5]+1$

mem addrs 8 set to mem addrs 5 + 1

4. What does the following RTL notation indicate?

$[PC] \leftarrow [PC]+1$

adds 1 to program counter

MIPS Program One: Addition

The following MIPS Assembly Program was developed in the code editor MIPster (<http://www.downcastsystems.com/mipster/>) and then run in the QtSpm MIPS Simulator (<http://spimsimulator.sourceforge.net/>)

A Program to Add 10 to 10

```

        .data                # Data declaration section

result: .asciiz "\n We Added 10 to 10 \n and the Result is: " #Memory location

        .text                # Text declaration section

main:   # Start of code section

        addi    $t0, $t0, 10  # Place immediate number 10 into t0 register
        addi    $t1, $t1, 10  # Place immediate number 10 into t1 register
        add     $t3, $t0, $t1  # Add the contents of t1 to t0 and place the result in t3
        li      $v0, 4        # Load immediate number 4 into v0 register (Print String)
        la      $a0, result    # Load memory address labelled 'result' and place into a0
        syscall                                # System call to carry out operation
        li      $v0, 1        # Load immediate number 1 into v0 register
        move    $a0, $t3      # Copy contents of register t3 to a0
        syscall                                # System call to carry out operation
        li      $v0, 10       # Load immediate number 10 into v0 register
        syscall                                # System call to carry out operation

# END OF PROGRAM

```


MIPS Program Two: Subtraction

A Program to Subtract 10 from 20

```
.data                                # Data declaration section
result: .asciiz "\n We Subtracted 10 from 20 \n and the Result is: "

.text                                # Text declaration section
main:                                # Start of code section

    addi    $t0, $t0, 20
    addi    $t1, $t1, 10
    sub     $t3, $t0, $t1  # Subtract contents of t1 from t0 and place result in t3
    li      $v0, 4
    la      $a0, result
    syscall

    li      $v0, 1
    move    $a0, $t3
    syscall

    li      $v0, 10
    syscall

# END OF PROGRAM
```

MIPS Program Three: Multiplication

A Program to Multiply 10 by 10

```
.data                                # Data declaration section
result: .asciiz "\n We Multiply 10 by 10 \n and the Result is: "

.text                                # Text declaration section
main:                                # Start of code section
    addi $t0, $t0, 10
    mult $t0, $t0                    # Multiply t0 by t0
    mfhi $t1                         # Move contents of Hi register to t1
    mflo $t2                         # Move contents of Lo register to t2
    li $v0, 4
    la $a0, result
    syscall
    li $v0, 1
    move $a0, $t2
    syscall
    li $v0, 10
    syscall
# END OF PROGRAM
```

MIPS: Program Four: Division

A Program to Divide 10 by 3

```
        .data                # Data declaration section
result: .asciiz "\n We Divide 10 by 3 \n and the Result is: "
remain: .asciiz "\n Remainder: "

        .text                # Text declaration section
main:   # Start of code section

        addi $t0, $t0, 10
        addi $t1, $t1, 3
        div $t0, $t1         # Divide the contents of t0 by t1
        mfhi $t2
        mflo $t3
        li $v0, 4
        la $a0, result
        syscall
        li $v0, 1
        move $a0, $t3
        syscall
        li $v0, 4
        la $a0, remain
        syscall
        li $v0, 1
        move $a0, $t2
        syscall
        li $v0, 10
        syscall

# END OF PROGRAM
```

MIPS: Program Five: Branching Control

A Program to Count Up to 10

```

        .data                # Data declaration section

count: .asciiz "\n Look, I can count to 10: "
end:   .asciiz "\n Well done me!"
new:   .asciiz "\n"

        .text                # Text declaration section

main:                                # Start of code section

    addi    $t0, $t0, 10
    addi    $t1, $t1, 0
    li      $v0, 4
    la      $a0, count
    syscall

    li      $v0, 4
    la      $a0, new
    syscall

loop:   addi    $t0, $t0, -1
        addi    $t1, $t1, 1
        li      $v0, 1
        move    $a0, $t1
        syscall

        li      $v0, 4
        la      $a0, new
        syscall

        blez    $t0, out        # Branch if t0 contents less than or equal to zero
        b       loop           # Branch always

out:    li      $v0, 4
        la      $a0, end
        syscall

        li      $v0, 10
        syscall

```

END OF PROGRAM

MIPS: Program Six: Jumping

A Program that Calls a Function

```

        .data                # Data declaration section
enter:  .asciiz "\n Please Enter a Number: "
result: .asciiz "\n The result of adding the two numbers together is: "

        .text                # Text declaration section
main:                                # Start of code section
        jal userent           # Jump to address labelled 'userent'
        move $t1, $t0
        jal userent
        move $t2, $t0
        add $t3, $t1, $t2
        li $v0, 4
        la $a0, result
        syscall
        li $v0, 1
        move $a0, $t3
        syscall
        li $v0, 10
        syscall

userent:
        li $v0, 4
        la $a0, enter
        syscall
        li $v0, 5
        syscall
        move $t0, $v0
        jr $ra                # Jump to contents of return address register

# END OF PROGRAM

```

The Answers

Signed Magnitude Notation

1. 01101011_2

Binary Excess Notation to Decimal

1. $+59_{10}$

Decimal to Binary Excess Notation

1. 01000001_2

Two's Complement

1. 11000101_2

Two's Complement Binary Additions

1. No, Yes, Yes, 4

Decimal to Excess 50 Notation

1. $+34_{10}$

Conversion of Decimal Numbers to SEEZMMMM Format

1. 04754870

Conversion of SEEZMMMM Format to Decimal Number

1. $+0.00000076823_{10}$

Conversion of Decimal Exponent to Excess 127 Binary

1. $01101000_2 = 104_{10}$

Conversion of IEEE 754 Single Precision Binary Float to Decimal

1. $+435_{10}$

Recap on the Little Man Computer

1. 10

The Register Transfer Language

1. The RTL notation indicates that bits 0 to 3 of memory address 2 are to be set to one.
2. The RTL notation indicates that the contents of memory address 8 are transferred (copied) to memory address 4
3. The RTL notation indicates that the contents of memory address 5 are incremented by 1 and the result placed in to memory address 8
4. The RTL notation indicates that the Program Counter (PC) register will be incremented by 1.