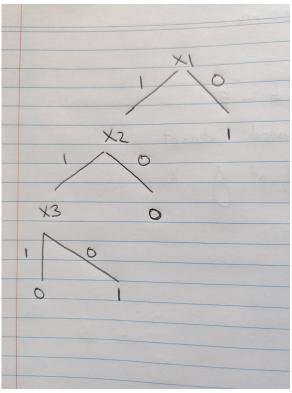
Question 1

a



i.From the working here 0.1, we can see that X_1 has the largest gain when splitting the data and therefore should be the first branch. X_2 and X_3 both have 0 gain. For the next split at $X_{1,1}$, both X_2 and X_3 produce the same gain which is $gain(X_{1,1},X_2)=gain(X_{1,1},X_3)=0.39317$ which is why it doesn't matter which one is selected. I chose X_2 to be the next split and then finished the tree.

The training error for this tree is 0 since our tree uses every feature and there are no observations where the exact same values for each feature is given but it maps to a separate output.

ii. There is no depth 2 decision tree that has a lower training error than the one found with ID3. The training error is already the lowest it can be at 0. This tells us that ID3 can fit any dataset with no conflicting classifications and therefore has very high complexity. Without specifying the ID3 algorithm to stop early and with a non-conflicting dataset, ID3 can always achieve 0 training error.

b

I generated the data with the following code:

```
def generate_data_set(positive_classes):
    # Assume all tuples are the same length
    dimensions = len(positive_classes[0])
    domain = list(itertools.product([0, 1], repeat=dimensions))

# Loop over domain
Y = []
for vector in domain:
# If vector is in positive_classes, then mark as positive
if vector in positive_classes:
    | Y.append([1])
else:
    | Y.append([-1])

return np.array(domain), np.array(Y)
```

The perceptron is then trained with:

```
def train_perceptron(X, y, eta):
31
         w = np.random.random((1, len(X[0])))
         nmb_iter = 0
         MAX_ITER = 10000
         for _ in range(MAX_ITER):
             nmb_iter += 1
             # check which indices we make mistakes on, and pick one randomly to update
40
             yXw = (y * X) @ w.T
             mistake_idxs = np.where(yXw < 0)[0]</pre>
             if mistake_idxs.size > 0:
                 i = np.random.choice(mistake_idxs)
                 w = w + eta * y[i] * X[i]
                                                            # update w
45
                 print(f"Converged after {nmb_iter} iterations")
         print(f"Did not converge after {MAX_ITER} iterations")
```

The spaces were then tested with:

Note that this produces **non-linearly separable** for all spaces which I'm assuming is not correct. The issues is that the vector for **w** doesn't iterate in a direction that separates the data better and keeps moving further and further away from the classifications.

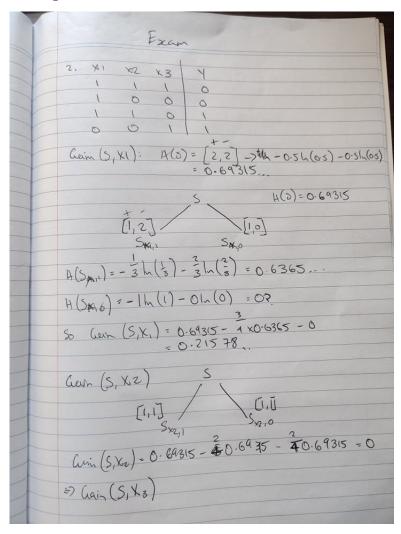
d

I had already started working on this before its removal. This is what I had:

```
def q2d():
    matplotlib.rc("font", **{"size" : 14}) # make plot text more visible
    y_dict = np.load(Q2D_DIR, allow_pickle=True).item()
    fig, ax = plt.subplots(3,2, figsize=(14,14))
plot_titles = ["(i)", "(ii)", "(iii)", "(iv)", "(v)", "(vi)"]
    for i, ax in enumerate(ax.flat):
        y = y_dict[plot_titles[i]]
        x = np.arange(y.shape[0])
        betahat = your_function(np.array(y)) ### update this line
        ax.scatter(x, y, marker="o", label="y")
        ax.plot(x, betahat,color="orange", linestyle="-", marker="s",label=r"$\hat{\beta}$")
        mse_bh = np.round(mse(y,betahat), 4)
        ax.set_title(f"part={plot_titles[i]}, mse={mse_bh}")
        ax.legend(loc="best")
    plt.tight_layout()
    plt.savefig("pickAName.png", dpi=400) ### update this line
    plt.show()
```

Appendix

0.1 q2a



H (*1.	= \$600de - = 0.636	31, (13)	$\frac{2}{3}\left(n\left(\frac{2}{3}\right)\right)$	
	1,1,X2):			
	El, U A(XzII)	H	(K2,0)	
Cain (X)	11, X2) = 0.6	365 - 3x0. 39317	6365 - 0	
	14	(X11) =	0.6365	
	(0,1) A(X3,1)		(1,T) + (X3,0)	
		0		
So it	doconit me	Her which	n one we	pic