Midterm 1: Python Problems

There are three python problems. Answer all the sections marked `#TODO`. Print to PDF. Submit the PDF only.

Loading Packages and Data

For the problems, you can use the following packages

In [411…

```
import numpy as np
import matplotlib.pyplot as plt
from sklearn.model_selection import train_test_split
from sklearn.linear_model import LinearRegression
import pickle
```

Run the following code to download the data for the midterm. This will retrieve three files -- one for each problem.

In [412…

```
import requests

def download_file_from_google_drive(id, destination):
    URL = "https://docs.google.com/uc?export=download"

    session = requests.Session()

    response = session.get(URL, params = { 'id' : id }, stream = True)
    token = get_confirm_token(response)

    if token:
        params = { 'id' : id, 'confirm' : token }
        response = session.get(URL, params = params, stream = True)

    save_response_content(response, destination)

def get_confirm_token(response):
    for key, value in response.cookies.items():
        if key.startswith('download_warning'):
            return value

    return None

def save_response_content(response, destination):
    CHUNK_SIZE = 32768

    with open(destination, "wb") as f:
        for chunk in response.iter_content(CHUNK_SIZE):
            if chunk: # filter out keep-alive new chunks
                f.write(chunk)

file_path = 'https://drive.google.com/file/d/10_1PxDIoSiuuOFC_iyVaoU9bDiQYHcTT/view?
file_id = '10_1PxDIoSiuuOFC_iyVaoU9bDiQYHcTT'

dst = 'midterm_data.zip'
download_file_from_google_drive(file_id, dst)


# Unzip the files
import zipfile
```

```
with zipfile.ZipFile(dst, 'r') as zip_ref:
    zip_ref.extractall('data')


# Move them to the top directory
import shutil
for fn in ['prob_linear.p', 'prob_model.p', 'prob_logistic.p']:
    src = 'data/midterm1_data/%s' % fn
    shutil.move(src, fn)
    print('%s loaded' % fn)
```

```
prob_linear.p loaded
prob_model.p loaded
prob_logistic.p loaded
```

Problem 1. Linear Regression

Run the following code to load the data

In [413…

```
with open('prob_linear.p', 'rb') as fp:
    X,y = pickle.load(fp)
```

Split the data into training and test. You may use the `train_test_split` function.

In [414…

```
# TODO
Xtr, Xts, ytr, yts = train_test_split(X, y, test_size=0.3)
```

In [415…

```
print(X.shape)
print(y.shape)
```

```
(500, 2)
(500,)
```

Suppose we want to fit a model of the form:

```
yhat[i] = b + w[0]*X[i,0] + w[1]*X[i,1] + w[2]*X[i,0]*X[i,1] +
w[3]*X[i,0]**2 + w[4]*X[i,1]**2
```

Complete the function `transform` below that creates a matrix `Z` whose columns are the basis functions for this model. You may use the `np.column_stack()` function. For example,

```
Z = np.column_stack((col1, col2, col3))
```

creates a matrix `Z` with columns `col1`, `col2`, and `col3`.

In [416…

```
def transform(X):
    # TODO
    Z = np.column_stack((X[:,0], X[:,1], X[:,0] * X[:,1], X[:,0]**2, X[:,1]**2))
    return Z
```

In [417…

```
# Testing on transform function
Z = transform(X)
print(Z.shape)
```

```
print(X[0, :])
print(Z[0, :])
```

```
(500, 5)
[-0.54002778 -0.81326207]
[-0.54002778 -0.81326207  0.43918411  0.29163     0.66139519]
```

Now fit and evaluate the model:

- Fit the model on the training data. You may use the `LinearRegression` object and the `transform` function above.
- Predict the values `y` on the test data
- Print the test MSE

In [418…

```
# TODO
# Transform Xtr and Xts
Ztr, Zts = transform(Xtr), transform(Xts)
# Fit Xtr with ytr
reg = LinearRegression()
reg.fit(Ztr, ytr)
# predict yhat from Zts
yhat = reg.predict(Zts)
# Compute MSE with yhat and yts
MSE = np.mean((yhat - yts)**2)
print("The Mean Squared Error is: ", MSE)
```

```
The Mean Squared Error is:  0.022120120586006018
```

Problem 2. Model Selection

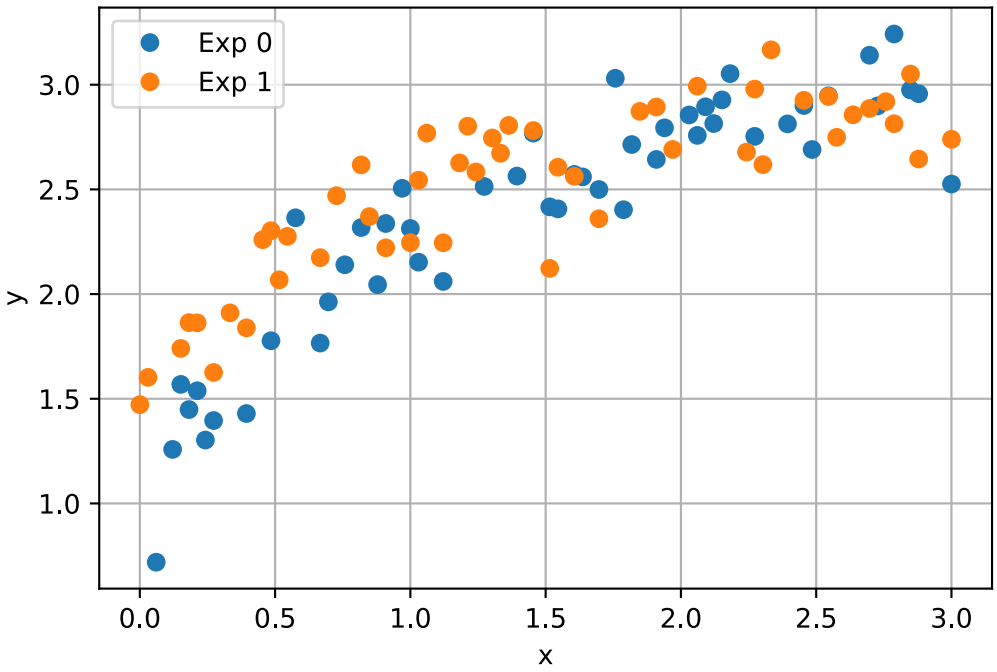
Run the code below to load and plot the data. The data is from two experiments:

- `Xtr[:,0], Ytr[:,0]` is the training data from experiment 0
- `Xtr[:,1], Ytr[:,1]` is the training data from experiment 1
- `Xts[:,0], Yts[:,0]` is the test data from experiment 0
- `Xts[:,1], Yts[:,1]` is the test data from experiment 1

In [419…

```
with open('prob_model.p', 'rb') as fp:
    Xtr, Xts, Ytr, Yts = pickle.load(fp)

plt.plot(Xtr[:,0], Ytr[:,0], 'o')
plt.plot(Xtr[:,1], Ytr[:,1], 'o')
plt.legend(['Exp 0', 'Exp 1'])
plt.xlabel('x')
plt.ylabel('y')
plt.grid()
```



In [420…

```
# Checking the shapes of objects
print(Xtr.shape, Xts.shape)
print(Ytr.shape, Yts.shape)
```

```
(50, 2) (50, 2)
(50, 2) (50, 2)
```

You want to learn the relation between `y` vs. `x`.

First, fit two *separate* models for each experiment of the form:

```
Y[:,0] ~= a0 + b0*exp(-X[:,0])
Y[:,1] ~= a1 + b1*exp(-X[:,1])
```

For the data in each experiment, fit the model and pint the test MSE.

You may use the `LinearRegression` function for the fitting. But, if `z` is a vector (not a matrix), you cannot use:

```
reg = LinearRegression()
reg.fit(z, y)   # WILL NOT WORK if z is a vector.
```

You must reshape `z` to a `n x 1` matrix first:

```
reg = LinearRegression()
reg.fit(z[:,None], y)   # This will work
```

In [421…

```
# TODO
nexp = Xtr.shape[1]  # number of experiments = 2
reg = LinearRegression()
for i in range(nexp):
    Ztr = np.exp(-Xtr[:,i])
    Zts = np.exp(-Xts[:,i])
    Ztr = Ztr[:,None]
```

```
    Zts = Zts[:,None]
    reg.fit(Ztr, Ytr[:,i])
    yhat = reg.predict(Zts)
    mse = np.mean((yhat-Yts[:,i])**2)
    print("The test Mean Square Error for experiment {} is {}".format(i, mse))
```

```
The test Mean Square Error for experiment 0 is 0.0339311556185114
The test Mean Square Error for experiment 1 is 0.041306971069426573
```

Now, fit a model of the form:

```
Y[:,0] = a + b0*exp(-X[:,0])
Y[:,1] = a + b1*exp(-X[:,1])
```

So, the two experiments have the same intercept term. Fit the model on the training data and measure the test MSE.

For training, you will want to combine the data into a single feature matrix `Z` using `Xtr[:,0]` and `Xtr[:,1]` and single target vector `b` from `Ytr[:,0]` and `Ytr[:,1]`.

In [422…

```
# This is wrong
# Ztr = np.exp(-Xtr)
# Zts = np.exp(-Xts)

# reg.fit(Ztr, Ytr)
# Yhat = reg.predict(Zts)
# print(reg.coef_)
# print(reg.intercept_)
# MSE = np.mean((Yhat-Yts)**2)
# print("The Mean Square Error for two experiements having same intercept term is ",
```

In [ ]:

In [ ]:

Problem 3. Logistic Regression

Run the following code to load the data as follows:

In [423…

```
with open('prob_logistic.p', 'rb') as fp:
    X,y = pickle.load(fp)
```

In [424…

```
# Checking shape and content of X y
print(X.shape)
print(y.shape)
print(X[0:5, :])
print(y[:5])
```

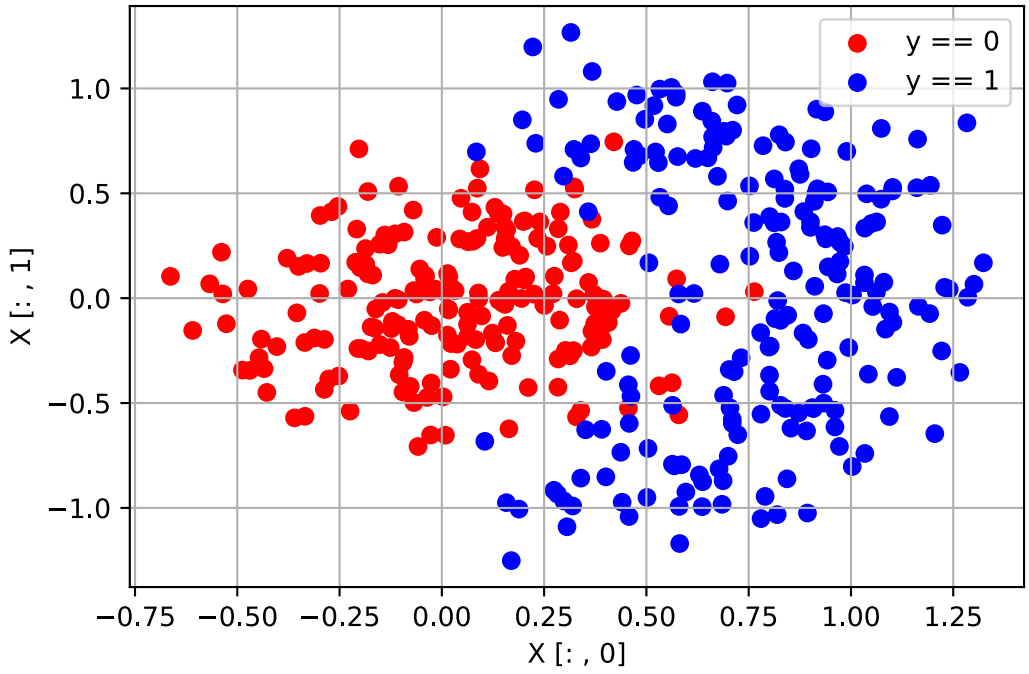
```
(400, 2)
(400,)
[[ 0.08294982 -0.19753769]
 [-0.06222682  0.01981546]
 [ 0.36398206  0.73624195]
 [ 0.13820735  0.40317062]
```

```
 [ 0.98679706  0.02633604]]
[0. 0. 1. 0. 1.]
```

Plot a scatter plot of the data with different colors for the two classes. You may use the `plt.scatter` function.

In [425…

```
# TODO
plt.scatter(X[(y==0),0], X[(y==0), 1], c='r')
plt.scatter(X[(y==1),0], X[(y==1), 1], c='b')
plt.legend(['y == 0','y == 1'],loc='upper right')
plt.grid(True)
plt.xlabel("X [: , 0]")
plt.ylabel("X [: , 1]")
plt.show()
```



Split the data into training and test. You may use the `train_test_split` method. Use `test_size=0.5` .

In [426…

```
# TODO
Xtr, Xts, ytr, yts = train_test_split(X, y, test_size=0.5)
```

Consider a classifier of the form:

```
yhat[i] = 1 when z[i] > t
yhat[i] = 0 when z[i] <= t
```

where `z[i] = X[i,0] + np.abs(X[i,1])` .

For each value `t` in `ttest` , compute the accuracy of the classifier on the *training* data. Plot the training accuracy as a function of `t` .

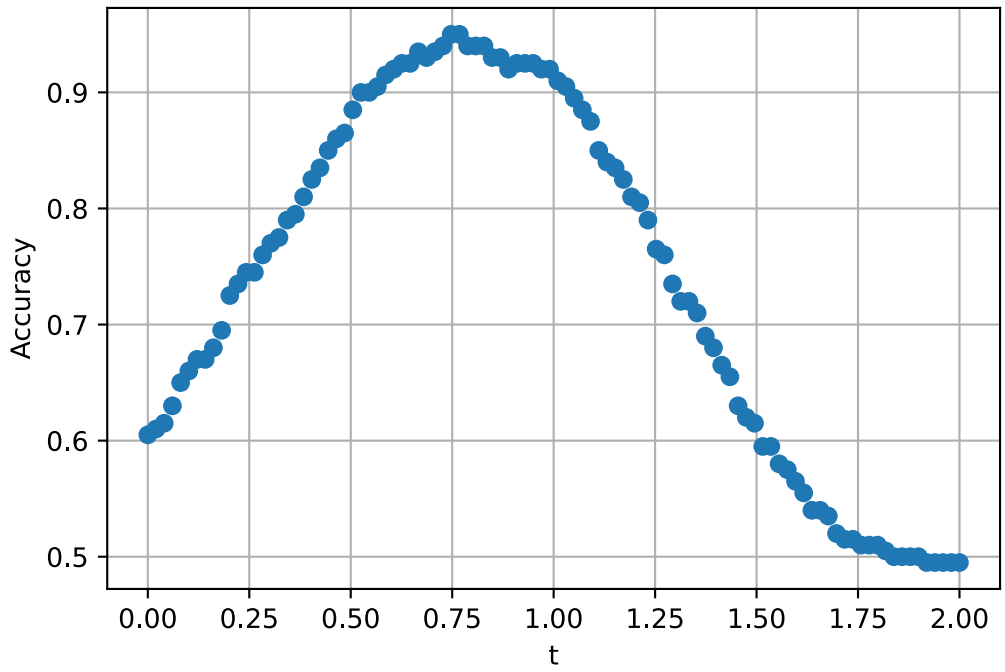
In [427…

```
ttest = np.linspace(0,2,100)
# vector of accuracy with size = len(ttest)
accuracy = np.zeros((100))
# make z vector
z = Xtr[:,0] + np.abs(Xtr[:,1])
```

```
for i, t in enumerate(ttest):
    yhat = z > t
    accuracy[i] = np.mean(yhat == ytr)

plt.plot(ttest, accuracy, 'o')
plt.grid()
plt.xlabel("t")
plt.ylabel("Accuracy")
```

Out[427… Text(0, 0.5, 'Accuracy')



Find the value of `t` with the highest training accuracy. Print the test accuracy for the classifier with that value of `t`.

In [428…

```
# TODO:
iopt = np.argmax(accuracy)
topt = ttest[iopt]

# TODO.
z = Xts[:,0] + np.abs(Xts[:,1])
yhat = z > topt
acc_ts = np.mean(yhat == yts)
print("The test accuracy with t {} is {}".format(topt, acc_ts))
```

```
The test accuracy with t 0.7474747474747475 is 0.965
```

In [ ]:

In [ ]: