2020/9/20 Problem - 1006

# **Robotic Class**

Time Limit: 2000/1000 MS (Java/Others) Memory Limit: 262144/262144 K (Java/Others)
Total Submission(s): 0 Accepted Submission(s): 0

# **Problem Description**

Baby volcano is now at a robotic class. In this class, babies are required to program a special control system of a robot. This control system has a real-valued control variable x, which captures the behavior of this robot. In addition, this control system could be abstracted as an acyclic directed graph, with n node, the nodes are indexed from 1 to n. In this graph, the node n has no output edge, termed as the output node. Moreover, for each vertex  $t, 1 \le t < n$ , there is a number  $k_t$ , a set of integer-valued limits  $a_{t,0} < a_{t,1} < a_{t,2} < \cdots < a_{t,k_t-1} < a_{t,k_t} := +\infty$ , and a set of integer-valued coefficients, bias and destinations  $c_{t,0}, b_{t,0}, d_{t,0}, c_{t,1}, b_{t,1}, d_{t,1}, c_{t,2}, b_{t,2}, d_{t,2} \cdots, c_{t,k_t}, b_{t,k_t}, d_{t,k_t}$ . For every t and  $i, 0 \le i \le k_t, -1 \le c_{t,i} \le 1$ .

To use this system to control the robot, the user follows the steps below:

- 1. Choose  $x_0$  and initialize  $x := x_0$ , then choose some node  $s_0$  and set the currect node  $t := s_0$
- 2. If t is the output node(t = n), then output  $x_{out} := x$ , else go to step 3.
- 3. The user finds the smallest i such that  $a_{t,i} \ge x$  (Note that i always exists), then transform  $x := c_{t,i} \times x + b_{t,i}$ , and set  $t := d_{t,i}$ , and go back to step 2.

Note that for every fixed  $s_0$ , the output value  $x_{out}$  is a function with respect to the initial value  $x_0 \in \mathbb{R}$ , we call this function  $C_{s_0}(x_0)$ .

To precisely control the robot, it is required that for every initial node  $s_0$ ,  $C_{s_0}(x_0)$  is continuous with respect to  $x_0$ .

A function  $f(x), x \in \mathbb{R}$  is continuous with respect to x iff

$$\forall x \in \mathbb{R}, \forall \epsilon > 0, \exists \delta > 0, \forall x' \in \mathbb{R}, (|x - x'| \leq \delta \implies |f(x) - f(x')| \leq \epsilon)$$

You need to verify this requirement is satisfied or not. In other words, if for every initial node  $s_0$ ,  $C_{s_0}(x_0)$  is continuous with respect to  $x_0$ , you should output "YES". If there exists some node  $s^*$  such that  $C_{s^*}(x_0)$  is not continuous, you should output "NO".

### Input

In the first line there is one integer T, denotes the number of test cases.

The rest of input has T part, each part corresponds to a test case.

For each part, in the first line there is a number n, denotes the number of nodes.

 $\text{In the next } n-1 \text{ lines, the } i\text{-th line starts with } k_i \text{, follows with } 4k_i+3 \text{ integers, they are } c_{i,0}, b_{i,0}, d_{i,0}, a_{i,0}, c_{i,1}, b_{i,1}, d_{i,1}, a_{i,1}, \cdots, a_{i,k_i-1}, c_{i,k_i}, b_{i,k_i}, d_{i,k_i-1}, c_{i,k_i-1}, c_{i,k_i}, b_{i,k_i}, d_{i,k_i-1}, c_{i,k_i-1}, c_$ 

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It guarantees that 1 \leq T \leq 100, and in a single test cases, 1 \leq n \leq 500, 1 \leq \sum k_i \leq 2000, -1 \leq c_{i,j} \leq 1, -10^6 \leq b_{i,j} \leq 10^6, -10^9 \leq a_{i,j} \leq 10^9, i+1 \leq d_{i,j} \leq n. And it guarantees that a_{i,j-1} < a_{i,j} for every 1 \leq j < k_i.
```

### **Output**

For each test case, you should firstly output "Case #: "(without quotes), where t is the index of this test case, then if for every initial node  $s_0$ ,  $C_{s_0}(x_0)$  is continuous with respect to  $x_0$ , you should output "YES". If there exists some node  $s^*$  such that  $C_{s^*}(x_0)$  is not continuous, you should output "NO".

#### Sample Input

```
3 4 1 1 1 2 -4 -1 -7 3 0 -1 -2 4 0 1 4 4 4 4 1 1 1 2 -4 -1 -7 3 0 -1 -3 4 0 1 4 4
```

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# **Sample Output**

Case #1: YES Case #2: NO Case #3: YES

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