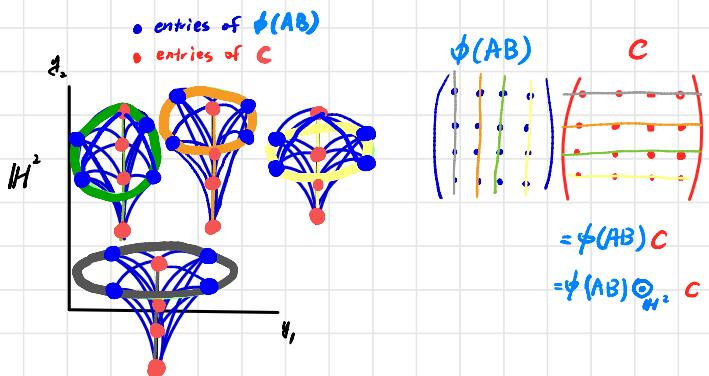
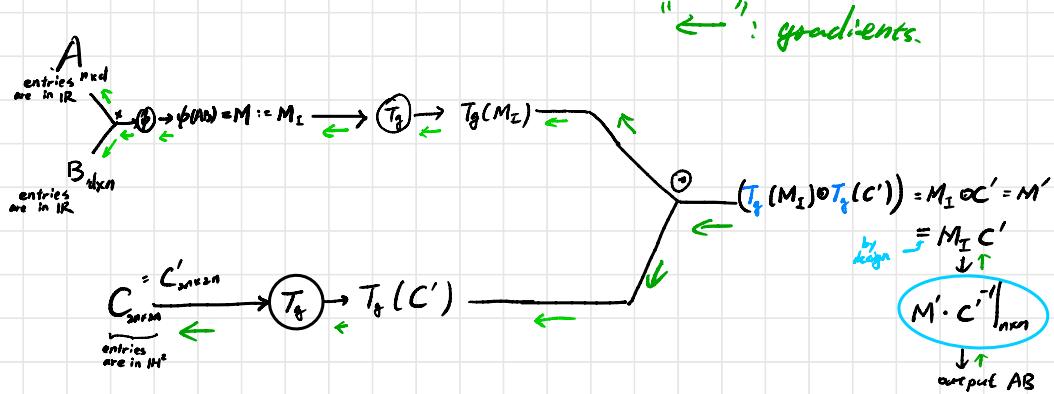
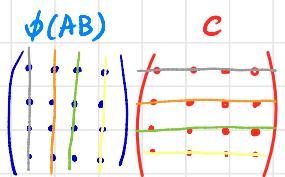


Case 2. Method 3.

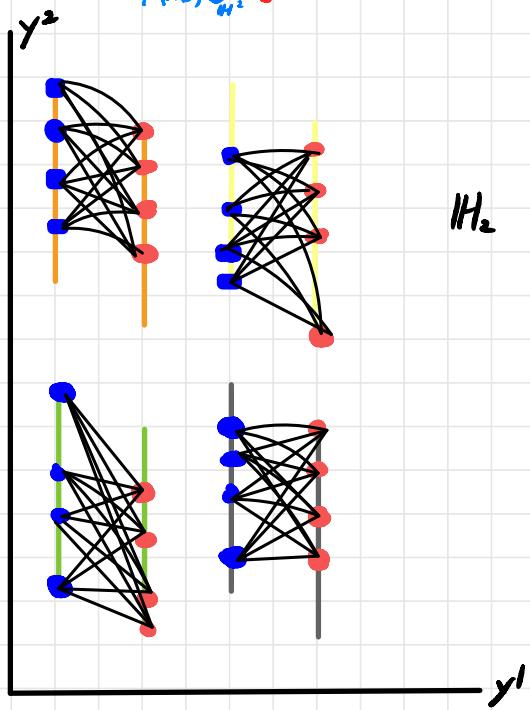


1. map M'_I entries to H^2 randomly.
2. randomly generate M'' (invertible and real)
3. $C' := M'^{-1}_I \cdot M''$



$$= \phi(AB)C$$

$$= \phi(AB) \otimes_{H^2} C$$



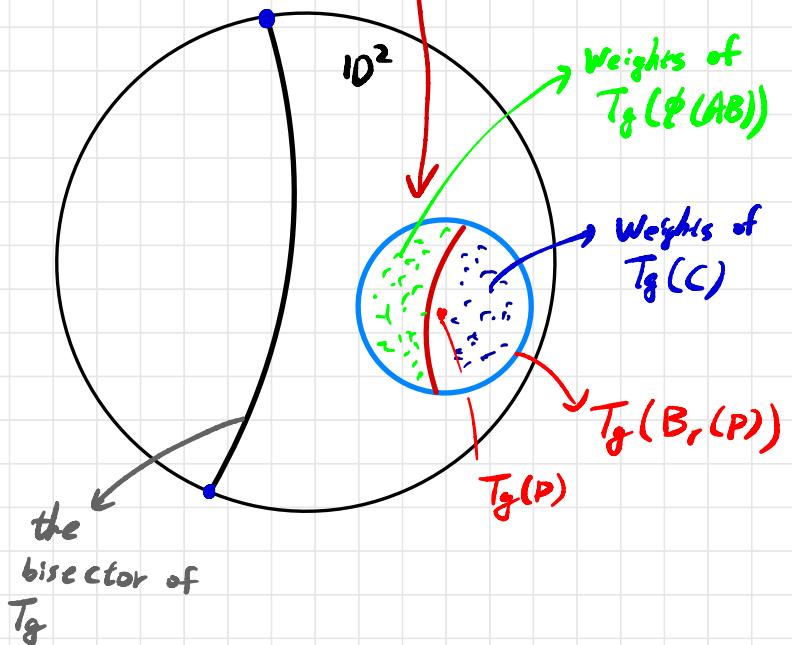
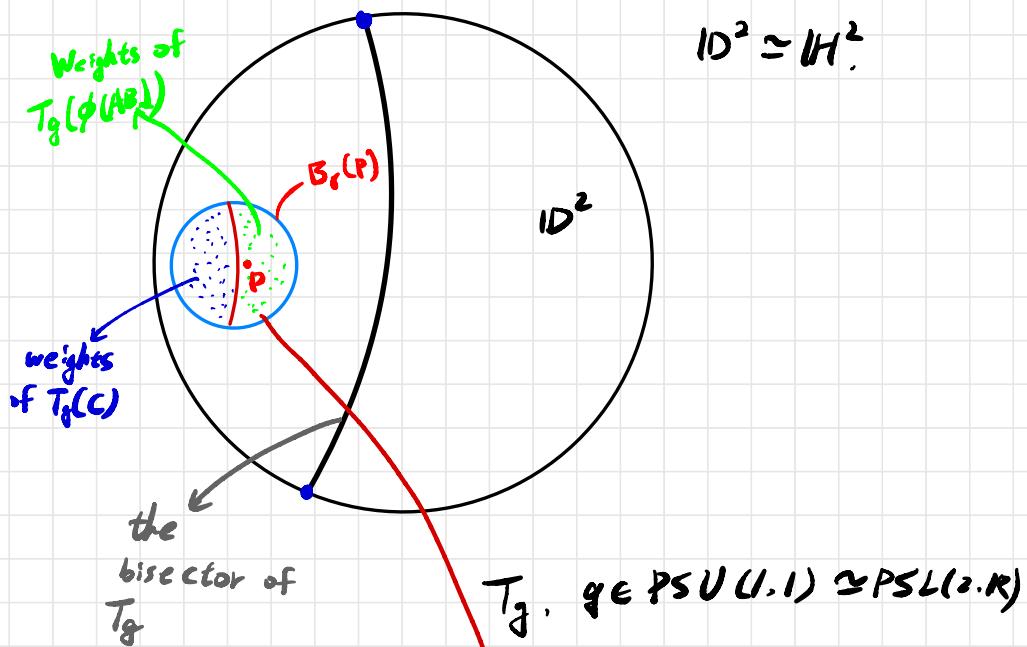
$$d_H(x, y) = \underbrace{d_H(S(x), S(y))}_{\text{on } H_2\text{-axis}} = \ln \left(\frac{s(x)}{s(y)} \right)$$

$$\begin{aligned}\frac{\partial dH}{\partial y} &= \frac{\partial}{\partial y} \ln \left(\frac{sy}{sx} \right) \\&= \frac{sy}{sx} \cdot \frac{(-sx)(\frac{\partial s}{\partial y})}{(sy)^2} \\&= \frac{-1}{sy} \cdot \frac{\partial s}{\partial y} = \frac{-1}{sy} \cdot \frac{1}{(cy+d)^2} = \boxed{\frac{-1}{(ay+b)(cy+d)}} \\[10pt]\frac{\partial dH}{\partial x} &= \frac{sy}{sx} \cdot \frac{\frac{\partial s}{\partial x}}{(sy)^2} - 0 \\&= \frac{1}{sy} \cdot \frac{\frac{\partial s}{\partial x}}{(cy+d)^2} = \frac{1}{\frac{sy}{sx} \cdot \frac{1}{(cy+d)^2}} = \boxed{\frac{1}{(\frac{ax+b}{cx+d})(\frac{ay+b}{cy+d})(cy+d)}} \\[10pt]\frac{\partial s}{\partial x} &= \frac{a(cx+d) - c(ax+b)}{(cx+d)^2} \\&= \boxed{\frac{(cx+d)(a-c) - bc}{(cx+d)^2}}\end{aligned}$$

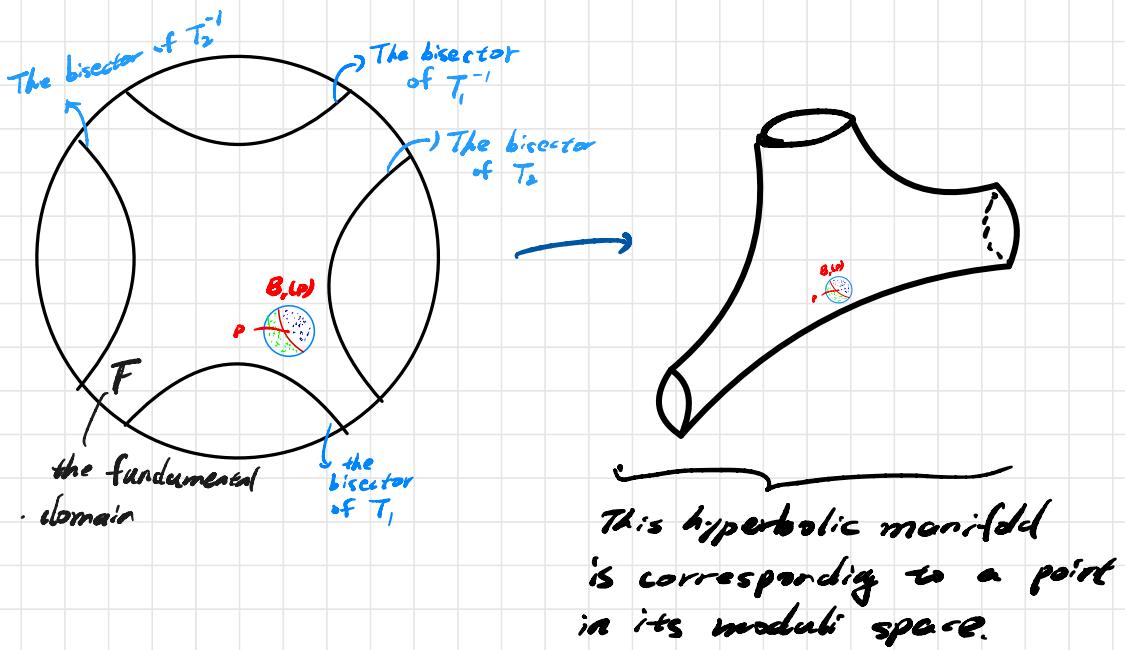
$$Sx = \frac{ax+b}{cx+d} \quad \frac{\partial S}{\partial x} = \frac{a(cx+d) - c(ax+b)}{(cx+d)^2}$$

$$sy = \frac{ay+bx}{cy+dx} = \frac{ad-bc}{(cx+dy)^2} = \frac{1}{(cx+dy)^2}$$

$$= \frac{1}{(cg+d)^2}$$

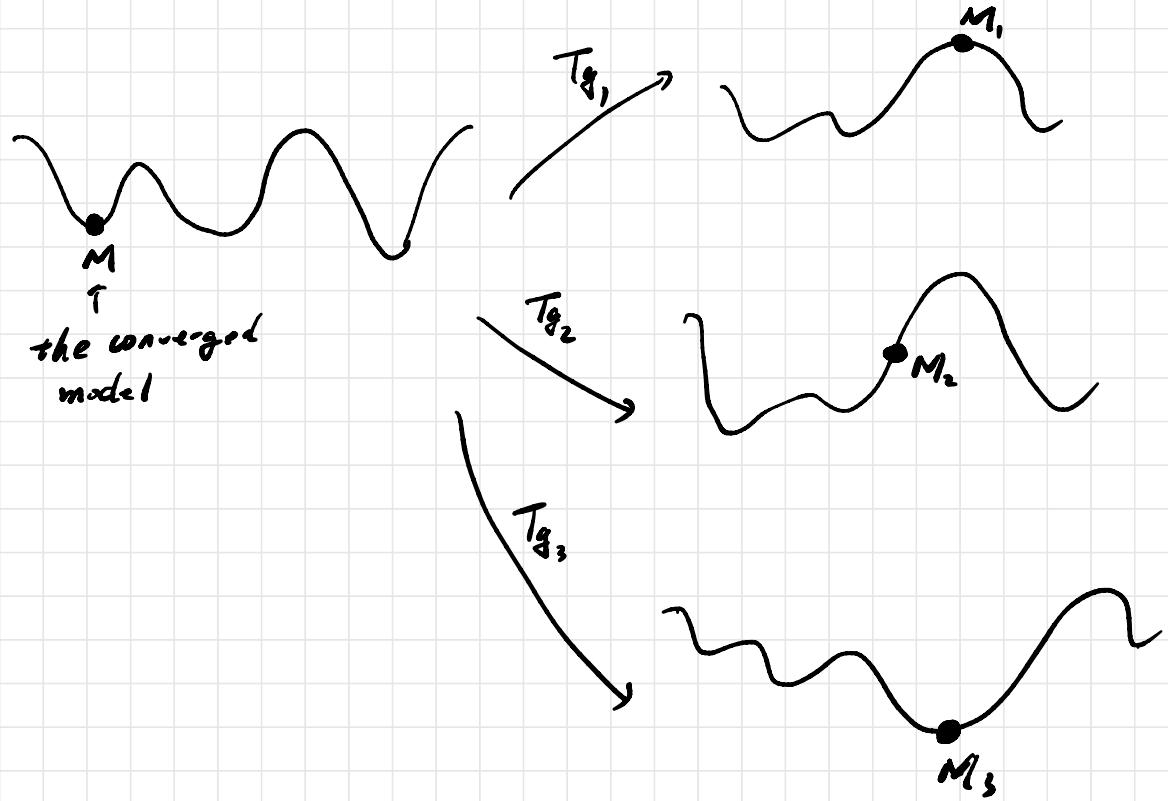


Assume $T_0 = T_1 \circ T_2$. Let T_1 and T_2 have the following configuration on their bisectors. Consider a subgroup of $\mathrm{PSU}(1,1) \cong \mathrm{PSL}(2, \mathbb{R})$ that is generated by T_1 and T_2 : $\langle T_1, T_2 \rangle$.



Using elements in $\langle T_1, T_2 \rangle$ to map $B_r(p)$ to a new place in F . to generate an equivalence of a given converged model. Using $B_r(p)$ as a device to detect the property of its corresponding loss surface.

Possible scenarios of loss surfaces :



Each possible scenario is corresponding to different location of $\Delta_r(p)$ in the hyperbolic space and manifold.