

# General Physics: Mechanics, Heat, and Sound

William Darko

Fall 2021

# Contents

<b>1</b>	<b>Kinematics in 1D</b>	<b>3</b>
1.1	Reference Frames . . . . .	3
1.2	Displacement and Distance . . . . .	3
1.2.1	Displacement . . . . .	3
1.2.2	Distance . . . . .	3
1.3	Average Velocity, and Speed . . . . .	3
1.3.1	Average Speed . . . . .	3
1.3.2	Average Velocity . . . . .	4
1.3.3	Instantaneous Velocity . . . . .	4
1.4	Acceleration . . . . .	4
1.5	Motion at constant acceleration . . . . .	5
1.6	Falling objects . . . . .	6

# 1 Kinematics in 1D

Kinematics in 1 dimension refers to the motion of objects, on **1 spatial dimension**, not necessarily in a one dimensional space. One can still observe 1 dimensional kinematics of objects in multidimensional spaces.

## 1.1 Reference Frames

Measurements of **position, distance, speed** must be with respect to a **reference frame**.

## 1.2 Displacement and Distance

### 1.2.1 Displacement

**Displacement** is the measure of **how far an object is from its initial (starting) position, and its final position**. Measure of displacement isn't dependant on the actual path taken by the object, or the length of that path, all that matters is the starting position, and finishing position.

Displacement is defined as:

$$\Delta x = x_2 - x_1$$

where  $x_2$  and  $x_1$  are the final, and initial positions of the object, respectively. Displacement is represented as a vector; a quantity with a **magnitude, and direction**.

### 1.2.2 Distance

There's a difference between displacement, and distance. While displacement is only concerned with the absolute difference between the initial and final position of an object, **distance** is concerned about the **absolute length of the path taken by the object**. Distance is **represented as a scalar quantity**.

## 1.3 Average Velocity, and Speed

### 1.3.1 Average Speed

Defined as:

$$\text{avg speed} = \frac{\text{distance travelled}}{\text{time elapsed}} = \frac{d}{\Delta t}$$

### 1.3.2 Average Velocity

Velocity is the change in rate of change in position, thus we're concerned with directional information; in what direction is our object moving. Thus average velocity is defined as:

$$\text{avg velocity} = \frac{\text{displacement}}{\text{time elapsed}} = \frac{\Delta x}{\Delta t}$$

### 1.3.3 Instantaneous Velocity

Instantaneous velocity is the **average velocity as the time elapsed becomes infinitely small**. In other words, as the limit of average velocity as time elapsed approaches 0:

$$v = \lim_{\Delta t \rightarrow 0} \frac{\Delta x}{\Delta t}$$

## 1.4 Acceleration

Acceleration of an object is the **rate of change of that objects velocity**. Mathematically:

$$\text{avg acceleration} = \frac{\text{ROC of velocity}}{\text{time elapsed}} = \frac{\Delta v}{\Delta t}$$

acceleration is also a vector quantity. In a single spatial dimension we really only care about the sign.

**Negative acceleration** is acceleration in the negative direction as define by the spatial coordinate system.

**Deceleration** occurs when acceleration is opposite in direction to velocity.

**Instantaneous acceleration** is the average acceleration as the time elapsed becomes infinitely small. In other words, the limit of average velocity as the time interval approaches 0.

$$a = \lim_{\Delta t \rightarrow 0} \frac{\Delta v}{\Delta t}$$

## 1.5 Motion at constant acceleration

We know the average velocity of an object during a time interval  $t$  is:

$$\bar{v} = \frac{\Delta x}{\Delta t} = \frac{x_1 - x_0}{t_1 - t_0} = \frac{x_1 - x_0}{t}$$

in other words, ratio of displacement, to time elapsed. We also know that acceleration, assumed constant, is:

$$a = \frac{v_1 - v_0}{t}$$

where  $v_1$ ,  $v_0$ , and  $t$  are observed velocities and time elapsed, respectively. In other words, the acceleration when constant is the difference/change in two observed velocities, divided by the observed elapsed time.

We also know that the average of any two numerical quantities is the sum of them divided by two. Thus, we can observe that the average velocity can be defined as:

$$\bar{v} = \frac{v_1 + v_0}{2}$$

Now, combining the last three equations, we can see that the equation for the position  $x$  of a particle in rectilinear space is the initial position  $x_0$  plus the average rate of change of position (average velocity) over a certain time period. Thus:

$$\begin{aligned} x &= x_0 + \bar{v}t \\ x &= x_0 + \left(\frac{v_0 + v_1}{2}\right)t \\ x &= x_0 + \left(\frac{v_0 + v_0 + at}{2}\right)t \\ \therefore x &= x_0 + v_0t + \frac{1}{2}at^2 \end{aligned}$$

to get rid of  $t$ , we combine the equations to get:

$$v^2 = v_0^2 + 2a(x - x_0)$$

We can now solve any constant acceleration problem with the following equations:

$$\begin{aligned} v &= v_0 + at \\ x &= x_0 + v_0t + \frac{1}{2}at^2 \\ v^2 &= v_0^2 + 2a(x - x_0) \\ \bar{v} &= \frac{v_1 + v_0}{2} \end{aligned}$$

## 1.6 Falling objects

Near the earth's surface, all objects experience approximately the same acceleration due to the force of gravity; thus experience motion with constant acceleration.

In the absence of air resistance, like in a vacuum, objects fall with the same acceleration.

Acceleration due to earth's gravity is approximately  $\mathbf{g} = 9.8 \text{ m/s}^2$

With gravity introduced, all the equations we've developed for constant acceleration still hold; as we observe linear motion on the **proper spatial  $y$ -axis**, our equations become:

$$\begin{aligned}v_y &= v_{y0} + a_y t \\y &= y_0 + v_{y0} t + \frac{1}{2} a_y t^2 \\v_y^2 &= v_{y0}^2 + 2a(y - y_0) \\\bar{v}_y &= \frac{v_{y1} + v_{y0}}{2}\end{aligned}$$

where the  $y$  subscript represents the quantities observed on the spatial  **$y$ -axis**. Thus, our acceleration  $\mathbf{a}_y$  here since we're observing free falling objects along the spatial  **$y$ -axis** is:

$$\mathbf{a}_y = 9.8 \text{ m/s}^2$$

and negative, if moving in the negative direction along the coordinate system, as per the definition of negative acceleration.