SC2001/CX2101 Algorithm Design and Analysis

Tutorial 5
String Matching
(Week 12)

This tutorial helps you develop skills in the learning outcome of the course: "Able to design algorithms using suitable strategies (preprocessing, etc) to solve a problem, able to analyse the efficiencies of different algorithms for problems like string matching, etc".

Rewrite the simpleScan algorithm in the lecture slides to eliminate the variable i.

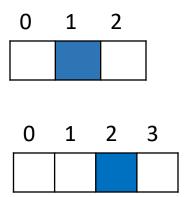
Original code

```
int SimpleScan (char [] P, char [] T, int m)
                                   ABABC
   int i, j, k;
   \dot{j} = k = 0;
 i = 0;
                                   ABABABCCAC
while (j < n) {
     if (T[j] != P[k]) {
          j = ++i;
                                         ABABC
         \mathbf{k} = 0; 
     else {
          j++;
          k++;
          if (k == m) return i; } ABABABCCAC
 return -1;
```

After removing i

```
int SimpleScan (char [] P, char [] T, int m)
   int \frac{1}{1}, j, k;
   j = k = 0;
 i = 0;
 while (j < n) {
      if (T[j] != P[k]) {
            j = ++i; j-k+1;
           \mathbf{k} = 0; 
      else {
            j++;
            k++;
            if (k == m) return \frac{i}{i}; j-k; }
 return -1;
```

How would you modify the Rabin-Karp algorithm to search for a given pattern with the additional condition that the middle character is a "wild card" (any text character at all can match it)?

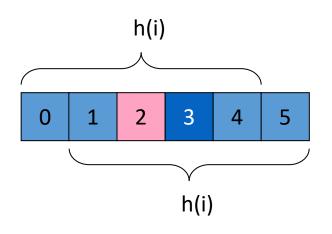


The hash function: Replace the middle digit by 0

```
int hash(Txt, m, d)
       int h = Txt[0] \% q;
       int middle = m/2;
       for (int i = 1; i < m; i++)
           if (i == middle)
               h = (h * d) % q;
           else
               h = (h * d + Txt[i]) % q;
       return h;
```

To rehash after moving the text window one character right:

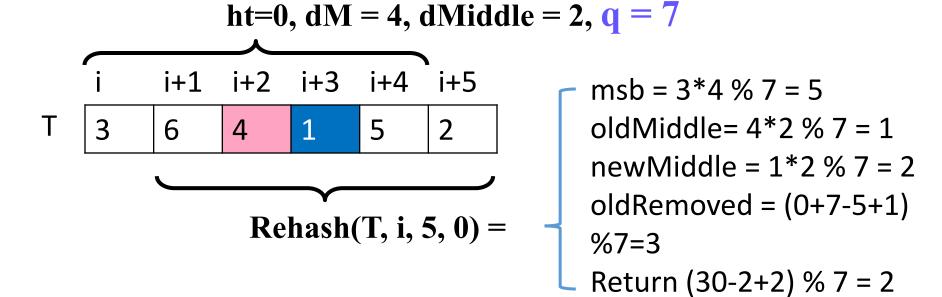
- Remove the MSB
- Add the middle digit in the old window
- Replace the middle digit in the new window by 0



```
In general,
new = (old - MSB * d<sup>m-1</sup>
+ MiddleB* d<sup>m/2</sup> )* d
- NewMiddleB* d<sup>m/2</sup>
+ LSB
```

```
// dM = d<sup>m-1</sup> % q
dM = 1;
For j = 1 to m-1
dM = dM*d % q
```

```
// dMiddle = d<sup>m/2</sup> % q
dMiddle = 1;
For j = 1 to m/2
   dMiddle = dMiddle*d % q;
```



Given pattern P = "AAA.....AB" (m-1 A's followed by one B and text string T = "AAA.....A" (n A's)

- 1) Show the values of CharJump and matchJump arrays for P computed by the Boyer-Moore string matching algorithm. Assume that alpahbet is {A,B,...,Z}.
- Find out exactly how many character comparisons are done by simpleBMScan and BMScan respectively to scan T for an occurrence of P.

3(1)

P = "AAA.....AB"

CharJump['A'] = 1 CharJump['B'] = 0 CharJump[x] = m

A A ... A B

A B

Matched = 0, Slide[m] = 1 MatchJump[m] = 1

A A ... A B

A A ... A B

Matched = 1, Slide[m-1] = m MatchJump[m-1] = m+1

A A ... A B

A ... A B

Matched = 2, Slide[m-2] = m MatchJump[m-2] = m+2





Matched = m-2, Slide[2] = m MatchJump[2] = 2m-2

Α	Α		А	В
---	---	--	---	---

A	Α		Α	В
---	---	--	---	---

Matched = m-1, Slide[1] = m MatchJump[1] = 2m-1

MatchJump

1	2	•••	m-2	m-1	m
2m-1	2m-2	•••	m+2	m+1	1

3(2) simpleBMScan

j += max(charJump[T[j]], m-k+1);

CharJump['A'] = 1, CharJump['B'] = 0, CharJump[x] = m

A A A.....B

A A A.....A 1st comparison then j+= max(1, m-m+1)=1

A A A....B

A A A......A 2nd comparison, j += 1

A A A.....B

A A A.....A (n-m+1)th comparison (the last)

• Therefore:

No. of Comparisons = n - m + 1

j += max(charJump[T[j]], matchJump[k]);

3(2) BMScan

A A A.....B

A A A.....A 1st comparison then $j+=\max(1, 1)$

A A A.....B

A A A.....A 2nd comparison, j += 1

A A A.....B

A A A.....A (n-m+1)th comparison (the last)

• Therefore:

No. of Comparisons = n - m + 1, the same as simpleBMScan

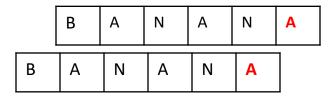
Question 4(1)

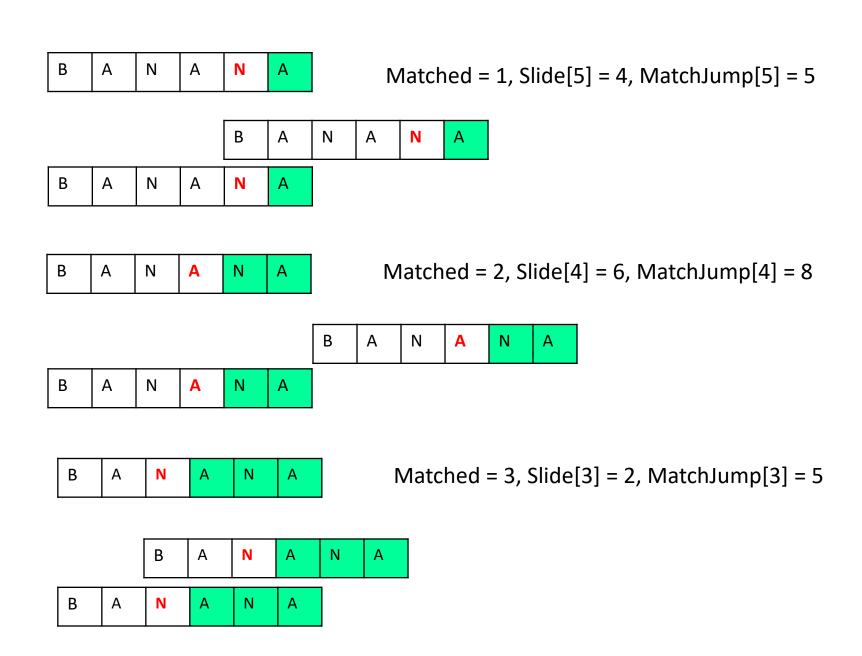
Show the values of CharJump and matchJump arrays for the following pattern, which are computed by the Boyer-Moore string matching algorithm, assuming alpahbet is {A,B,...,Z}.

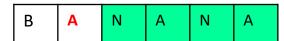
CharJump['A'] = 0, CharJump['B'] = 5, CharJump['N'] = 1, CharJump[x] = 6



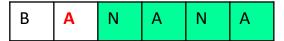
Matched = 0, Slide[6] = 1, MatchJump[6] = 1





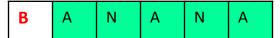


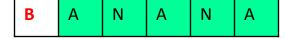
Matched = 4, Slide[2] = 6, MatchJump[2] = 10



B A N A N A

Matched = 5, Slide[1] = 6, MatchJump[1] = 11

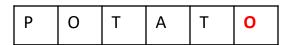




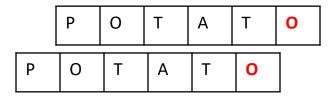
Question 4(2) – not covered if no time

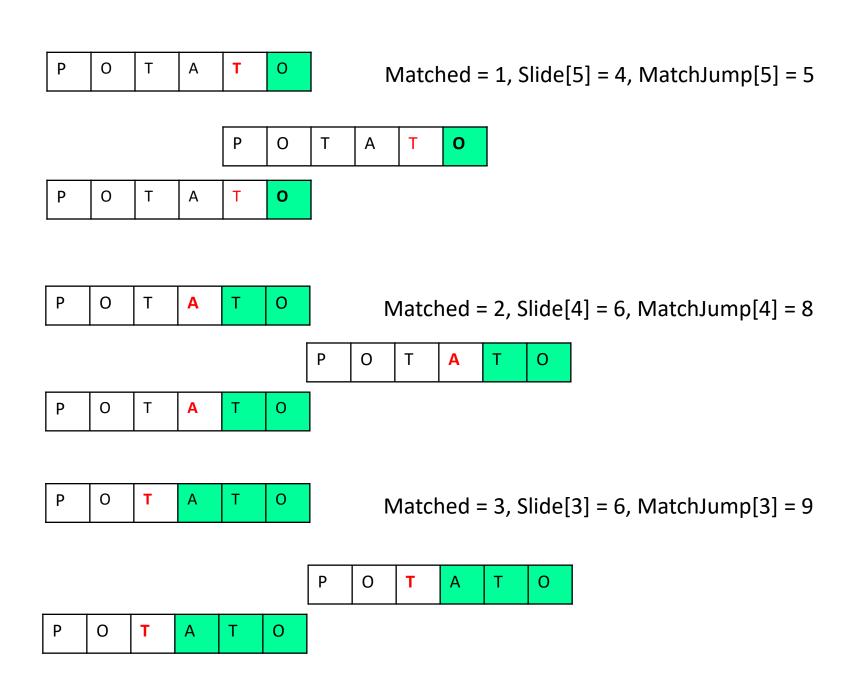
Show the values of CharJump and matchJump arrays for the following pattern, which are computed by the Boyer-Moore string matching algorithm, assuming alpahbet is {A,B,...,Z}.

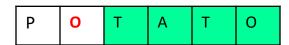
CharJump['A'] = 2, CharJump['O'] = 0, CharJump['P'] = 5, CharJump['T'] = 1 CharJump[x] = 6



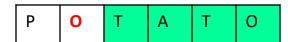
Matched = 0, Slide[6] = 1, MatchJump[6] = 1

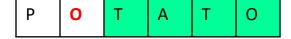


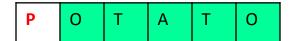




Matched = 4, Slide[2] = 6, MatchJump[2] = 10







Matched = 5, Slide[1] = 6, MatchJump[1] = 11

