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# 611. Valid Triangle Number



■ Description (/problems/valid-triangle-number/description/)

♀ Hints (/problems/valid-triangle-number/hints/)

# Solution

# Approach #1 Brute Force [Time Limit Exceeded]

The condition for the triplets (a,b,c) representing the lengths of the sides of a triangle, to form a valid triangle, is that the sum of any two sides should always be greater than the third side alone. i.e. a+b>c, b+c>a, a+c>b.

The simplest method to check this is to consider every possible triplet in the given nums array and checking if the triplet satisfies the three inequalities mentioned above. Thus, we can keep a track of the count of the number of triplets satisfying these inequalities. When all the triplets have been considered, the count gives the required result.

```
Сору
Java
   public class Solution {
2
      public int triangleNumber(int[] nums) {
         int count = 0;
3
4
         for (int i = 0; i < nums.length - 2; i++) {
5
            for (int j = i + 1; j < nums.length - 1; j++) {
               for (int k = j + 1; k < nums.length; k++) {
6
7
                   > nums[i])
8
9
10
            }
11
         } T
12
         return count;
13
14
15
```

## **Complexity Analysis**

- Time complexity :  $O(n^3)$ . Three nested loops are there to check every triplet.
- Space complexity : O(1). Constant space is used.

## Approach #2 Using Binary Search [Accepted]

#### **Algorithm**

If we sort the given nums array once, we can solve the given problem in a better way. This is because, if we consider a triplet (a,b,c) such that  $a \leq b \leq c$ , we need not check all the three inequalities for checking the validity of the triangle formed by them. But, only one condition a+b>c would suffice. This happens because  $c \geq b$  and  $c \geq a$ . Thus, adding any number to c will always produce a sum which is greater than either a or b considered alone. Thus, the inequalities c+a>b and c+b>a are satisfied implicitly by virtue of the property a < b < c.

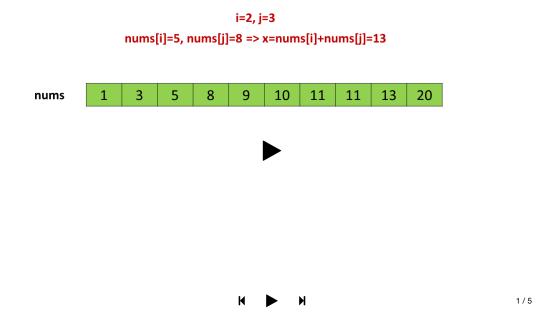
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From this, we get the idea that we can sort the given nums array. Then, for every pair (nums[i], nums[j]) considered starting from the beginning of the array, such that j>i(leading to  $nums[j]\geq nums[i]$ ), we can find out the count of elements nums[k](k>j), which satisfy the inequality nums[k]>nums[i]+nums[j]. We can do so for every pair (i,j) considered and get the required result.

We can also observe that, since we've sorted the nums array, as we traverse towards the right for choosing the index k(for number nums[k]), the value of nums[k] could increase or remain the same(doesn't decrease relative to the previous value). Thus, there will exist a right limit on the value of index k, such that the elements satisfy nums[k] > nums[i] + nums[j]. Any elements beyond this value of k won't satisfy this inequality as well, which is obvious.

Thus, if we are able to find this right limit value of k (indicating the element just greater than nums[i] + nums[j]), we can conclude that all the elements in nums array in the range (j+1,k-1) (both included) satisfy the required inequality. Thus, the count of elements satisfying the inequality will be given by (k-1)-(j+1)+1=k-j-1.

Since the nums array has been sorted now, we can make use of Binary Search to find this right limit of k. The following animation shows how Binary Search can be used to find the right limit for a simple example.



Another point to be observed is that once we find a right limit index  $k_{(i,j)}$  for a particular pair (i,j) chosen, when we choose a higher value of j for the same value of i, we need not start searching for the right limit  $k_{(i,j+1)}$  from the index j+2. Instead, we can start off from the index  $k_{(i,j)}$  directly where we left off for the last j chosen.

This holds correct because when we choose a higher value of j(higher or equal nums[j] than the previous one), all the nums[k], such that  $k < k_{(i,j)}$  will obviously satisfy nums[i] + nums[j] > nums[k] for the new value of j chosen.

By taking advantage of this observation, we can limit the range of Binary Search for k to shorter values for increasing values of j considered while choosing the pairs (i, j).

```
Сору
Java
    public class Solution {
        int binarySearch(int nums[], int l, int r, int x) {
2
            while (r \geq= 1 && r < nums.length) {
3
 4
                 int mid = (1 + r) / 2;
 5
                if (nums[mid] >= x)
                    r = mid - 1;
 6
                 else
7
                    1 = mid + 1;
8
9
10
            return 1;
11
12
        public int triangleNumber(int[] nums) {
13
            int count = 0;
14
            Arrays.sort(nums);
            for (int i = 0; i < nums.length - 2; i++) {
15
                int k = i + 2;
16
                for (int j = i + 1; j < nums.length - 1 && nums[i] != 0; <math>j++) {
17
18
                     k = binarySearch(nums, k, nums.length - 1, nums[i] + nums[j]);
19
                     count += k - j - 1;
20
                }
21
22
            return count;
23
24
    }
```

#### **Complexity Analysis**

- ullet Time complexity :  $O(n^2logn)$ . In worst case inner loop will take nlogn (binary search applied n times).
- Space complexity : O(logn). Sorting takes O(logn) space.

## Approach #3 Linear Scan [Accepted]:

### **Algorithm**

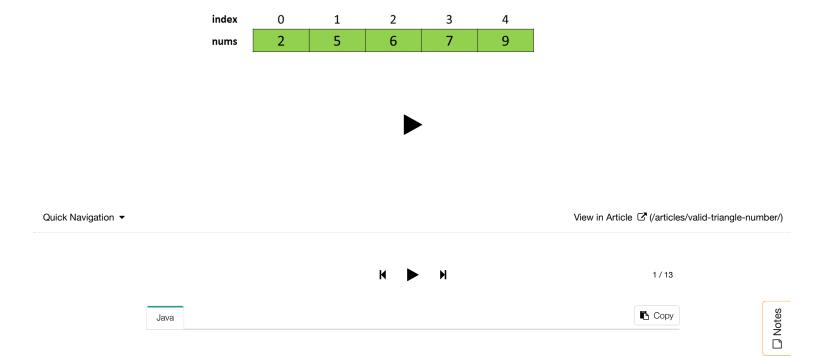
As discussed in the last approach, once we sort the given nums array, we need to find the right limit of the index k for a pair of indices (i,j) chosen to find the count of elements satisfying nums[i] + nums[j] > nums[k] for the triplet (nums[i], nums[j], nums[k]) to form a valid triangle.

We can find this right limit by simply traversing the index k's values starting from the index k=j+1 for a pair (i,j) chosen and stopping at the first value of k not satisfying the above inequality. Again, the count of elements nums[k] satisfying nums[i] + nums[j] > nums[k] for the pair of indices (i,j) chosen is given by k-j-1 as discussed in the last approach.

Further, as discussed in the last approach, when we choose a higher value of index j for a particular i chosen, we need not start from the index j+1. Instead, we can start off directly from the value of k where we left for the last index j. This helps to save redundant computations.

The following animation depicts the process:

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# **Complexity Analysis**

- Time complexity :  $O(n^2)$ . Loop of k and j will be executed  $O(n^2)$  times in total, because, we do not reinitialize the value of k for a new value of j chosen(for the same i). Thus the complexity will be  $O(n^2+n^2)=O(n^2)$ .
- ullet Space complexity : O(logn). Sorting takes O(logn) space.

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